An analysis of the halo and relic radio emission from Abell 3376 from Murchison Widefield Array observations


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ABSTRACT

We have carried out multiwavelength observations of the nearby (z = 0.046) rich, merging galaxy cluster Abell 3376 with the Murchison Widefield Array (MWA). As a part of the GaLactic and Extragalactic All-sky MWA Survey, this cluster was observed at 88, 118, 154, 188, and 215 MHz. The known radio relics, towards the eastern and western peripheries of the cluster, were detected at all the frequencies. The relics, with a linear extent of ∼1 Mpc each, are separated by ∼2 Mpc. Combining the current observations with those in the literature, we have obtained the spectra of these relics over the frequency range 80–1400 MHz. The spectra follow power laws, with $\alpha = -1.17 \pm 0.06$ and $-1.37 \pm 0.08$ for the west and east relics, respectively ($S \propto \nu^{\alpha}$). Assuming the break frequency to be near the lower end of the spectrum we estimate the age of the relics to be ∼0.4 Gyr. No diffuse radio emission from the central regions of the cluster (halo) was detected. The upper limit on the radio power of any possible halo that might be present in the cluster is a factor of 35 lower than that expected from the radio power and X-ray luminosity correlation for cluster haloes. From this we conclude that the cluster halo is very extended (>500 kpc) and/or most of the radio emission from the halo has decayed. The current limit on the halo radio power is a factor of 10 lower than the existing upper limits with possible implications for models of halo formation.

Key words: galaxies: clusters: individual: Abell 3376 – galaxies: clusters: intracluster medium.

1 INTRODUCTION

Galaxy clusters are some of the largest known gravitationally bound structures in the Universe composed primarily of dark matter along with galaxies and the X-ray-emitting intracluster medium (ICM) gas. Their masses are ∼10^{15} M_\odot while their sizes are ∼ Mpc. According to the theory of hierarchical structure formation, galaxy clusters are formed by mergers of several smaller sub-clusters and groups driven by gravity. The process of cluster evolution through mergers is still ongoing and is one of the most energetic phenomena in the Universe with energies 10^{53}–10^{64} erg (Hoeft et al. 2008).

In some merging clusters Mpc-scale diffuse synchrotron radio emission, in the form of radio haloes (in the central regions of the cluster) and/or radio relics (towards the peripheries), have been detected. The radio haloes have a typical surface brightness of a few mJy arcmin^{-2} at 1.4 GHz (see Feretti et al. 2012 and Brunetti & Jones 2014 for recent reviews). Radio haloes usually have a smooth
morphology while relics are found to be elongated or arc-like in nature. The fraction of galaxy clusters which host such structures is rather small. Of all the known galaxy clusters below a redshift of 0.2, ~5 per cent contain radio haloes and relics (Giovannini, Tordi & Feretti 1999). This fraction increases to ~35 per cent for higher X-ray luminosity clusters ($L_X \gtrsim 10^{45}$ erg s$^{-1}$) (Venturi et al. 2008) which have correspondingly higher radio power as well (Liang et al. 2000; Bacchi et al. 2003; Cassano, Brunetti & Setti 2006; Brunetti et al. 2007, 2009; Cassano et al. 2007; Rudnick & Lemmerman 2009). In a more recent study of galaxy clusters with redshift $0.2 < z < 0.4$, Kale et al. (2013) estimated that 23 per cent of galaxy clusters with X-ray luminosity $L_X > 5 \times 10^{44}$ erg s$^{-1}$ host radio haloes. For clusters with $L_X > 8 \times 10^{45}$ erg s$^{-1}$ the fraction increases to 31 per cent. It has been observed, however, that highly disturbed, merging clusters are much more likely to host haloes and relics than relaxed clusters (Buote 2001; Cassano et al. 2010). This led to the scenario that major cluster mergers could provide sufficient energy to the electrons in the ICM which, in the presence of existing magnetic field, produce synchrotron radiation that is detected as haloes and relics. It should be mentioned here that even though both haloes and relics are found predominantly in disturbed clusters, the processes responsible for their generation are thought to be different, as explained below.

One of the currently accepted models for the generation of radio haloes is turbulent acceleration (Brunetti et al. 2001; Petrosian 2001). During the process of a cluster merger, turbulence in the ICM gas re-accelerates the electron population of the ICM to ultra-relativistic energies ($\gamma \gtrsim 1000$, where $\gamma$ is the Lorentz factor). This turbulence also amplifies the magnetic field to a few $\mu$G (Carilli & Taylor 2002; Subramanian, Shukurov & Haugen 2006). The synchrotron radiation from these electrons could be seen in the form of radio haloes from the cluster centre.

An alternative to the turbulent acceleration model is the hadronic (secondary) model (Dennison 1980; Blasi & Colafrancesco 1999; Pfrommer & Enßlin 2004), which posits that collisions between relativistic and thermal protons in the ICM are responsible for the generation of relativistic electrons. Proton–proton collisions result in the formation of pions. Neutral pions decay to produce gamma rays whereas charged pions decay to produce electrons and positrons. Since relativistic protons in galaxy clusters have a lifetime greater than that of the cluster itself, there will always be a fraction of the relativistic electrons in the ICM produced in such a manner. However, based on radio observations of massive, X-ray-luminous galaxy clusters, Brunetti et al. (2007) claimed that relativistic protons contribute less than a few per cent of the energy in particles in galaxy clusters. Recently, observations of galaxy clusters at GeV energies were carried out using the Fermi and Cherenkov telescopes (Aharonian et al. 2009a,b; Ackermann et al. 2010; Aleksić et al. 2010). No gamma rays were detected and only upper limits to the emission were placed. Therefore, any contribution to synchrotron emission due to relativistic protons (indirectly) would be very small. It is believed that the level of radio emission produced in this process (secondary model) is about a factor of 10 below the radio emission produced in the turbulence model (Brunetti & Lazarian 2011).

Radio relics, on the other hand, are created as a consequence of shock fronts travelling outwards from the cluster centre after a merger. The acceleration of electrons in the periphery of the cluster is best explained by the diffusive shock acceleration (DSA) theory (Blandford & Eichler 1987; Jones & Ellison 1991). According to the theory, shock acceleration is essentially a first-order Fermi acceleration process in which thermal particles are accelerated diffusively. They scatter elastically across the two fronts of a shock repeatedly, gaining energy at each crossing of a front until they get accelerated to very high energies (Feretti et al. 2012). The best examples for the validity of this theory come in the form of a special class of relics, known as double relics, where two arc-like structures are seen on the opposite sides of the cluster centre. However there are very few of these double relics [e.g. Abell 3667 (Johnston-Hollitt 2003), Abell 3376 (Bagchi et al. 2006), CIZA J2242.8+5301 (van Weeren et al. 2011), etc.] known. Rarer still are clusters that host both haloes and double relics, even though both are thought to be a consequence of the same merger process [e.g. RXC J1314.5-2515 (Feretti et al. 2005), CIZA J2242.8+5301, El Gordo (Lindner et al. 2014), etc.]. The reason for the absence of haloes in merging systems is not well understood. One possibility is that the halo was created at the time of the merger but faded away over time.

Radio haloes and relics are systems where different physical processes come into the picture. Detection or non-detection of diffuse radio emission depends on many factors such as the mass ratio of the merging clusters, impact parameter of collision between the clusters, time since the merger, turbulence decay time-scales, and synchrotron lifetime of the radiating electrons (Brunetti & Jones 2014). In the case of radio relics, the inhomogeneity of the ICM also plays an important part. The dearth of detections of radio haloes and radio relics can be explained in many ways. Clusters with lower X-ray luminosity have correspondingly lower radio power and may not be bright enough to be detected by existing telescopes. Additionally, if one assumes the turbulent acceleration model that produces the radio haloes, then the diffuse radio emission should display an exponential cut-off at higher radio frequencies ($\gtrsim 1.4$ GHz). As a result most of the extended, diffuse emission will be fainter at higher frequencies (Cassano 2010). Furthermore, large angular extent diffuse emission is also likely to be resolved out at higher frequencies. This is why it is necessary to observe and image galaxy clusters at low radio frequencies with greater surface brightness sensitivity than what GHz receivers can currently offer. Telescopes such as the MWA (Murchison Widefield Array; Lonsdale et al. 2009; Bowman et al. 2013; Tingay et al. 2013), LOFAR (LOw Frequency ARray; van Haarlem et al. 2013), and the upcoming SKA (Square Kilometre Array; Dewdney et al. 2013) will be crucial in this endeavour.

With the above motivations in mind, recently, Hindson et al. (2014) used commissioning data from the MWA to observe the galaxy cluster Abell 3667 at low frequencies (120, 149, 180, and 226 MHz). A3667 has long been known to host two radio relics. Its northernmost relic has been discussed in a number of papers spanning 45 years (Ekers 1969; Schilizzi & McAdam 1975; Goss et al. 1982; Rottgering et al. 1997), whilst the weaker second relic, though visible in the published 843 MHz images in Rottgering et al. (1997), was overlooked at that time, and not first mentioned in the literature until it was rediscovered in the 1.4 GHz data and the entire cluster reimaged (Johnston-Hollitt et al. 2002; Johnston-Hollitt 2003) thus making A3667 the first double relic cluster. Imaging between 1.4 and 2.4 GHz has given rise to suggestions of a radio halo (Johnston-Hollitt et al. 2002; Johnston-Hollitt 2003; Carretti et al. 2013), a possible bridge connecting the two relics (Carretti et al. 2013) or more recently a mini-halo off-set from the cluster centre (Riseley et al. 2015). Assuming typical spectral characteristics, the putative halo and bridge were expected to be easily visible in the lower frequency MWA imaging. However, the MWA imaging did not confirm the detection of either structure. Based on this MWA imaging, it has been suggested that A3667 is seen in projection through a large diffuse spur of Galactic emission, which in turn might be responsible for these features (Hindson et al. 2014). At the sensitivity of the MWA commissioning observations it was not
observations (Escalera et al. 1994; Durrer et al. 2013) indicate the $39 \pm 3$ arcsec and a virial mass of $M = 1.1 \times 10^{14} M_{\odot}$ that is a factor of 5 better than the commissioning observations. For a morphologically similar system, A3376, we expect to reach a sensitivity of $5 \times 3.64 \times 10^{14} M_{\odot}$ (Girardi et al. 1998). Optical galaxies (BCG) on the opposite ends of the cluster with the X-ray merging status of the cluster by showing the two brightest cluster galaxies (BCG) on the opposite ends of the cluster with the X-ray peak at BCG2 (MRC0600-399) (Fig. 1). The BCG1 is a cD galaxy and is considered to be the centre of the main cluster. The BCG2 is an elliptical and its radio counterpart is a bent-jet galaxy. Machado & Lima Neto (2013) simulated the merger of A3376 and compared their simulation results with the X-ray morphology of the cluster. Based on these comparisons they suggest that the merger in A3376 occurred $\sim 0.5$ Gyrs ago between sub-clusters having a mass ratio of $6:1$. Very Large Array (VLA) observations of this cluster at 1.4 GHz (Bagchi et al. 2006) showed the presence of two arc-like structures in the eastern and western peripheries of the cluster, $\sim 1$ Mpc away from the cluster centre. These relics are assumed to be due to synchrotron emission from the ICM as a consequence of shock waves travelling outwards from the cluster centre soon after the merger. Further radio observations at lower frequencies (150 and 325 MHz) using the Giant Meterwave Radio Telescope (GMRT; Kale et al. 2012) detected the relics but not a radio halo from the central regions of the cluster (Fig. 1). The east relic is found to be polarized up to 30 per cent with aligned magnetic field vectors, whereas the west relic is polarized between 5 and 20 per cent and the field vectors are not aligned in any particular direction (Kale et al. 2012).

Figure 1. GMRT 325 MHz contours (Kale et al. 2012) on the ROSAT X-ray (0.1–2.4 keV) broad-band image. The units of the X-ray image are in counts s$^{-1}$ arcmin$^{-2}$. The contour levels start from 5.8 mJy beam$^{-1}$ (3$\sigma$) and increase by a factor of $\sqrt{2}$. The resolution of the radio image is $39 \pm 3$ arcsec. The $\times$ and the $+$ represent the BCG2 and BCG1 galaxies, respectively. The yellow solid line (drawn by the authors) marks the boundaries of the east and west relics.

possible to distinguish the Galactic features from a weak halo or bridge that might also be present, though strong limits were placed on the possible emission. In our current observations of the morphologically similar system, A3376, we expect to reach a sensitivity that is a factor of 5 better than the commissioning observations.

1.1 Abell 3376

Abell 3376 is a rich, merging galaxy cluster at a redshift of $z = 0.046$ (Struble & Rood 1999). It has an X-ray luminosity of $L_{X0.1 - 2.4 keV} = 2.2 \times 10^{44}$ erg s$^{-1}$ (Reiprich & Böhringer 2002) and a virial mass of $\sim 3.64 \times 10^{14} M_{\odot}$ (Girardi et al. 1998). Optical observations (Escalera et al. 1994; Durret et al. 2013) indicate the merging status of the cluster by showing the two brightest cluster galaxies (BCG) on the opposite ends of the cluster with the X-ray peak at BCG2 (MRC0600-399) (Fig. 1). The BCG1 is a cD galaxy and is considered to be the centre of the main cluster. The BCG2 is an elliptical and its radio counterpart is a bent-jet galaxy. Machado & Lima Neto (2013) simulated the merger of A3376 and compared their simulation results with the X-ray morphology of the cluster. Based on these comparisons they suggest that the merger in A3376 occurred $\sim 0.5$ Gyrs ago between sub-clusters having a mass ratio of $6:1$. Very Large Array (VLA) observations of this cluster at 1.4 GHz (Bagchi et al. 2006) showed the presence of two arc-like structures in the eastern and western peripheries of the cluster, $\sim 1$ Mpc away from the cluster centre. These relics are assumed to be due to synchrotron emission from the ICM as a consequence of shock waves travelling outwards from the cluster centre soon after the merger. Further radio observations at lower frequencies (150 and 325 MHz) using the Giant Meterwave Radio Telescope (GMRT; Kale et al. 2012) detected the relics but not a radio halo from the central regions of the cluster (Fig. 1). The east relic is found to be polarized up to 30 per cent with aligned magnetic field vectors, whereas the west relic is polarized between 5 and 20 per cent and the field vectors are not aligned in any particular direction (Kale et al. 2012).

The motivations for the current study are twofold. First, to detect the radio relics at low frequencies and establish their spectra over 80–1400 MHz. Secondly, to detect or put stringent upper limits on the radio power of a possible halo in the central regions of the cluster, which has eluded detection so far. The paper is organized as follows: in Section 2, we discuss observations and data analysis. Section 3 contains the results and in Section 4, we discuss the implications of these results. We conclude with the summary in Section 5. In this paper we adopt a $\Lambda$-cold dark matter cosmology with $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_M = 0.3$, and $\Omega_{\Lambda} = 0.7$.

2 OBSERVATIONS AND ANALYSIS

2.1 The GLEAM Survey

The observations of A3376 were carried out as part of GaLactic and Extragalactic All-Sky MWA (GLEAM) Survey (Wayth et al. 2015). There are five observing frequency ranges: 72.3–103.04 MHz, 103.04–133.76 MHz, 138.88–169.6 MHz, 169.6–200.32 MHz, and 200.32–231.04 MHz, each having a bandwidth of 30.72 MHz. The data were recorded with an integration time of 0.5 s and a spectral resolution of 40 kHz. The frequency range 134–138 MHz was avoided due to the presence of satellite Radio Frequency Interference (RFI) in that range.

The GLEAM Survey was carried out in the drift-scan mode with the antennas pointing to one of the seven declination settings ($\delta = +18.6, +1.6, -13.0, -26.7, -40.0, -55.0, -72^\circ$) and letting the sky drift overhead. A single scan consists of observations for 112 s at each of the five frequencies available and then cycling through them. The data used for imaging A3376 in this paper were taken during 2013 November 6–7 while covering the RA range 0–8 h at declination $\delta = -40^\circ$. This declination pointing is within a few arcmin of the centre of the cluster (Fig. 1).

2.2 Data reduction

In principle, one could use the specialized pipeline software that has been set up to analyse the observations from the GLEAM Survey (Hurley-Walker, in preparation). However, with the scope to try to analyse the MWA observations using a standard radio astronomy software, we imaged the cluster at two frequencies viz. 154 and 215 MHz using CASA (Common Astronomy Software Applications). We chose these two frequencies because at 215 MHz the highest angular resolution in the GLEAM frequency range is achieved (151 arcsec $\times$ 145 arcsec) and at 154 MHz the MWA images obtained can be directly compared with the existing GMRT observations at 150 MHz. The images at 154 and 215 MHz, processed with CASA, are further compared with the pipeline processed images at the same frequencies. For the remaining frequencies (88, 118, and 188 MHz) we use the pipeline processed images.

The raw data from A3376 scans were converted to measurement sets readable by CASA using the cotter software (Offringa et al. 2015). This software also performed some initial flagging and RFI removal using the AOFlagger library (Offringa et al. 2010; Offringa, van de Gronde & Roerdink 2012). The source 3C161 was used to create the normalized bandpass tables (task BANDPASS in CASA) which were applied to all the A3376 scans. In all, a total of seven scans of A3376 were used – the transit scan and three scans on either side of the source’s transit through the meridian – which covered a total time range of $\pm 30$ min around transit at each frequency.

http://casa.nrao.edu
The scans beyond this time range were not considered due to the falling gain of the primary beam (i.e. the beam response was falling < 50 per cent). Note that the full widths at half-maxima of the primary beams of the MWA tiles are \( \sim 25^\circ \) at 154 MHz (Hurley-Walker et al. 2014). The bandpass corrected measurement sets were then averaged in time and frequency to 8 s and 400 kHz, respectively. Each scan was then individually imaged and deconvolved in CASA using the task CLEAN. Each image produced \( (2048 \times 2048 \text{ pixels}) \) covered an area of \( 34.13 \times 34.13 \text{ deg}^2 \) in each axis with a pixel size of 1 arcmin. Deconvolution was performed using the Cotton–Schwab algorithm (Schwab 1984) and widefield effects were taken into account using the w-projection algorithm (Cornwell, Golap & Bhatnagar 2008) by setting the number of projection planes in CLEAN to 256.

A variety of robust weighting schemes were tried to make images of A3376. In order to reach a balance between sensitivity and resolution we used ‘Briggs’ weighting (Briggs 1995) with robust value 0 for each scan at both polarizations. Note that Briggs weighting with values −5 and +5 correspond to purely uniform and purely natural weighting, respectively. The images were then sent through four rounds of phase self-calibration, at the end of which the phase errors had reduced to an rms of 0.2. No further improvement was seen with subsequent phase and amplitude self-calibration. The XX and YY polarizations were imaged separately for each scan. They were then corrected for primary beam effects (Sutinjo et al. 2015).

Following the above procedure, a total of seven images were produced for A3376 for each polarization. These images were examined separately and their rms values were estimated. Furthermore, the positions of unresolved sources in the GMRT 150 MHz image within a degree from A3376 were compared with their respective positions in the seven MWA 154 MHz images. Across these seven images, the positional offsets for all these sources were constant to within 10 per cent of the MWA synthesized beam size at 154 MHz. At each frequency, the individual primary beam-corrected XX and YY images were weighted using the inverse variance of the rms in the respective images and then combined. The final XX and YY images were weighted using the inverse variance of the rms in the respective images and then combined. The final XX and YY images were added together to produce the full total intensity (Stokes I) image.

For the remaining frequencies (88, 118, and 188 MHz), we utilized the pipeline-processed GLEAM images, described in detail in Hurley-Walker et al. (in preparation). For each scan, the basic steps of this pipeline are as follows:

(i) perform a first-pass calibration using a single bright source, applied to all observations (Hurley-Walker et al. 2014);
(ii) using wsclean (Offringa et al. 2014), invert and clean multifrequency-synthesis images in instrumental Stokes, across the full bandwidth, stopping at the first negative clean component;
(iii) use the MWA primary beam model (Sutinjo et al. 2015) to transform to astronomical Stokes;
(iv) set Q, U, and V to zero (i.e. assume that the sky is unpolarized) and use the same beam model to transform back to instrumental Stokes;
(v) use the sky model in a self-calibration loop to update the gain solutions;
(vi) form new multifrequency synthesis images.

These individual images were then combined to produce the final total intensity images exactly as described earlier.

### 2.3 Calibration

The absolute flux density calibration of the MWA images was tied to those of the GMRT images at 150 and 325 MHz (Kale et al. 2012). For GMRT calibration, 3C147 and 3C48 as primary calibrators. The Perley & Butler (2013) scale was used for absolute flux density calibration. The secondary calibrators used in the GMRT 150 and 325 MHz observations were 0521-207 and 0837-198, respectively. The flux densities of these two calibrators obtained from GMRT at the two frequencies agree to within 10 per cent of their expected values based on the VLA calibrator list (Kale et al. 2012).

The MWA 154 MHz image was calibrated using the GMRT 150 MHz image. Unresolved sources in the GMRT 150 MHz image within a degree from A3376 were used to estimate an average scaling factor between the GMRT 150 MHz and the MWA 154 MHz images.

To calibrate the MWA 215 MHz image, the spectral indices of the same unresolved sources were estimated between the GMRT 150 MHz and 325 MHz images. The extrapolated flux densities at 215 MHz were estimated for these sources. The MWA 215 MHz image was then scaled according to the average value of the scaling factor. The images at 88, 118, and 188 MHz were also calibrated in a manner similar to the one used for calibrating the MWA 215 MHz image.

The images at 154 and 215 MHz made from CASA and from pipeline processing were compared. At 154 MHz, the rms of the CASA processed image was 18 mJy beam\(^{-1}\) (Table 1) while that of the pipeline processed image was 13 mJy beam\(^{-1}\). At 215 MHz, the rms of the CASA image was 11 mJy beam\(^{-1}\) (Table 1) while the pipeline image had an rms of 10 mJy beam\(^{-1}\). The rms of the pipeline images could be expected to reduce further by mosaicking in narrower frequency channels, resulting in fewer excluded images and thus a higher signal-to-noise ratio (Hurley-Walker et al., in preparation).

### 3 RESULTS

The MWA images of the Abell 3376 region at 154 and 215 MHz are shown in Fig. 2. The images at the other MWA frequencies are
not presented here as they are essentially convolved versions of the above images. The Abell 3376 images at 154 and 215 MHz show two prominent relics just outside the region of X-ray emission: one towards the east and the other towards the west of the X-ray emission (compare Figs 1 and 2). The two relics are separated by \( \sim 2 \) Mpc (\( \sim 30 \) arcmin) from each other. Both the east and west relics were detected at all the MWA frequencies. No diffuse radio emission in the central regions of the cluster (halo) was detected down to the GLEAM sensitivity. Table 1 lists the integrated flux densities of the relics and the upper limits on the flux densities of a possible halo in the region between the relics.

There are two primary sources of errors in the estimation of the flux densities of the relics in the MWA images. First, there is an error due to the uncertainties in the flux densities of the unresolved sources used for calibration of the MWA images. This error is estimated to be \( \sim 10 \) per cent. Secondly, since the relics are extended sources in the MWA observations, the errors in their flux density estimations will be the rms in the image multiplied by the square root of the ratio of the solid angle of the relic to that of the synthesized beam. Since these two sources of errors are unrelated, they are added in quadrature to estimate the final error on the flux densities of the relics that are quoted in Table 1.

The left- and the right-hand panels in Fig. 3 show the spectra over the frequency range 80–1400 MHz, for the east and the west relics, respectively. The spectral index of the east relic is \( -1.37 \pm 0.08 \) while that of the west relic is \( -1.17 \pm 0.06 \). A least-squares fitting method was used to estimate the spectral index values from the flux density values given in Table 1. The reduced-\( \chi^2 \) values for the fits on the east and west relics were 1.7 and 3.4, respectively.

4 DISCUSSION

Abell 3376 shows two arc-like radio relics on either side of the X-ray emission from the cluster. The arcs are oriented roughly perpendicularly to the merger axis of the cluster. Such a scenario is in agreement with the models that predict two outgoing shocks in the aftermath of the merger which are responsible for the radio emission seen from the arcs.

According to the DSA theory (Blandford & Eichler 1987), the slope of the power-law spectrum of the number density of electrons, \( p \), as a function of energy \( (N(E) \propto E^p) \), is related to the Mach number of the shock, \( M \), by

\[
p = -2\frac{M^2 + 1}{M^2 - 1} - 1. \tag{1}
\]

This includes the effects of particle ageing due to inverse Compton and synchrotron radiation losses under the assumption of continuous injection (Sarazin 1999; Giacintucci et al. 2008). The slope is related to the spectral index \( (\alpha) \) of the synchrotron radiation by

\[
\alpha = \frac{p + 1}{2}. \tag{2}
\]

The spectral index is related to the flux density, \( S \), by the standard relation, \( S \propto \nu^\alpha \), where \( \nu \) is frequency. For the east relic, the spectral index is estimated to be \( -1.37 \pm 0.08 \) which gives the Mach number \( 2.53 \pm 0.23 \). For the west relic, the spectral index is estimated to be \( -1.17 \pm 0.06 \), which gives the Mach number \( 3.57 \pm 0.58 \).

Suzaku X-ray observations by Akamatsu et al. (2012) estimate the Mach number of the east and west relics to be \( 2.91 \pm 0.91 \). This number agrees with the value obtained from simulations (Machado & Lima Neto 2013) as well. The Mach numbers estimated here for both the relics are consistent with the X-ray estimates.

The spectra of the relics show no breaks in the frequency range 80–1400 MHz. The shock acceleration is expected to produce an initial injection index for the synchrotron radiation close to \( -0.8 \). Radiation losses induce a break such that the spectral index after the break steepens by 0.5 to \( -1.3 \) (see for example, the relic radio galaxies in Slee et al. 2001). The average spectral index of the two relics is \( -1.3 \). This is consistent with the break frequency being close to or lower than the lower end of the spectrum (\( \sim 80 \) MHz) shown in Fig. 3. The magnetic field in the cluster can be assumed to be \( \sim 1 \) \( \mu \)G (Govoni et al. 2013). We can estimate the spectral ages of the relics as

\[
t = \frac{1060}{B^{0.5}} \frac{B_{IC}^{0.5}}{B^2 + B_{IC}^2} (1 + z)^{-0.5}, \tag{3}
\]

where \( B \) is the magnetic field in the source, \( B_{IC} \) is the effective inverse Compton magnetic field, \( z \) is the redshift of the source and \( \nu \) is the break frequency (Slee et al. 2001). Based on these values, the spectral ages of the relics is \( \sim 0.4 \) Gyr.

We have made the assumption here that the break frequency is \( 80 \) MHz. In reality, this break could be lower than this which would...
imply that the spectral age is greater than 0.4 Gyr. This estimated spectral age of the relics is, nevertheless, consistent with the age of the cluster ($\sim$0.5 Gyr) as obtained from simulations discussed later in this section.

The cluster merger responsible for the generation of the observed relics also generates turbulence in the ICM which is believed to be able to re-accelerate electrons in the region between the relics (Brunetti et al. 2001; Petrosian 2001). The region between the relics is then expected to host a radio halo. No such radio halo is detected at the MWA frequencies. However, we have been able to put an upper limit to the flux density from a possible halo in the central region of A3376. Table 1 lists the mean flux densities observed in the central regions of A3376 in the MWA images. The mean value of the spectral index of haloes is $\alpha = -1.34 \pm 0.28$ (Feretti et al. 2012). An upper limit to the radio power of a halo at 1.4 GHz can be estimated using the upper limit at 154 MHz (Table 1) and extrapolating it to 1400 MHz using the mean value of the spectral index quoted here. This power corresponds to $6 \times 10^{21}$ W Hz$^{-1}$.

The upper limit is plotted in Fig. 4 where the radio powers at 1.4 GHz and the corresponding X-ray luminosities of known haloes and relics are also plotted (Brunetti et al. 2009). The solid line represents the best fit to the known haloes. The upper limit on the radio power of the A3376 halo is lower by a factor of $\sim$35 compared to that expected from the best-fitting line.

The upper limit on the radio power of the halo corresponds to a halo size of $\sim$160 kpc ($\sim$3 arcmin) at 154 MHz. This corresponds to the beam size at 154 MHz. If the halo is more extended than this, even with higher total radio power, it will be undetected because of limits on surface brightness sensitivity. For a canonical halo as extended as 500 kpc, the upper limit on the radio power would still be lower by a factor of $\sim$4 as compared to that expected from the best-fitting value.

In order to explain why no radio halo is detected in this cluster we first need to discuss some of the time-scales involved in the merger process. The separation between the two relics of A3376 is $\sim$2 Mpc. Simulations by Machado & Lima Neto (2013) estimate that the shock velocity, $v_s$, is $\sim$2000 km s$^{-1}$ with an estimated dynamical time-scale, $t_{dyn} \sim 0.49$ Gyr. This agrees with their simulations of the gas morphology which puts the cluster at approximately 0.5 Gyr after central passage.

MHD turbulence generated in cluster mergers has a decay time associated with it which is given by Cassano & Brunetti (2005),

$$\tau_{visc}(\text{Gyr}) \sim \left( \frac{v_i}{2000 \text{ km s}^{-1}} \right)^{-1} \left( \frac{L_{\text{inj}}}{1 \text{ Mpc}} \right) \left( \frac{\eta_i}{0.25} \right)^{-1}, \quad (4)$$

where $v_i$ is the relative velocity of the merging clusters at the time of impact and $\eta_i$ is defined as the fraction of energy in the form of turbulence that is converted into magnetosonic (MS) waves. This means that the value of $\eta_i$ defines the efficiency with which the electron population is re-accelerated. The value of $\eta_i$ can be approximated to 0.25 by using the constraint that the slope of the radio spectrum of the haloes is in the range, $\alpha = 1.1$–1.5 (Kempner & Sarazin 2001). The value of $v_i$ is estimated from simulations (Machado & Lima Neto 2013) to be $\sim$1500 km s$^{-1}$. The typical injection length-scale ($L_{\text{inj}}$) of turbulence in galaxy clusters is 200–300 kpc (Brunetti & Lazarian 2011). With these values in the above equation, the decay time of turbulence for a cluster like A3376 is estimated to be 0.25–0.4 Gyr. Considering that it is now $\sim$0.5 Gyr since core passage of the cluster, most of the turbulence that would have been generated at the time of merger would have dissipated. Furthermore, the half-life of these radio emitting electrons is short, $\sim$0.3 Gyr (Slee et al. 2001). Any radio halo that was generated during the cluster merger is likely dissipated.

It has been postulated that in galaxy clusters there should be a long-lived component of cluster-wide diffuse radio emission that is generated by relativistic electrons which are continuously injected into the IGM by relativistic proton–thermal proton collisions (Brunetti & Lazarian 2011). The radio power of diffuse emission expected from these secondary particles is expected to be at a level that is about an order of magnitude lower than that of the radio powers in haloes that are detected. The upper limit on the radio power of a halo in Abell 3376 is nearing such levels. While the current limit is close to such a level, further lowering of these limits either in this cluster or in other clusters will have implications for the secondary models of halo production.

5 SUMMARY

In this paper, we present low frequency radio observations of Abell 3376 using the MWA at 88, 118, 154, 188, and 215 MHz. The
observations were carried out as part of the GLEAM survey. The observations were analysed using CASA tools as well as specialized software packages written to process the GLEAM data. Images were produced at all frequencies. Towards the east and west peripheries of the cluster, bright arcs of radio emission (relics) were detected at all frequencies. These arcs, with a linear extent of ~1 Mpc each, are a result of outgoing shocks produced by the merger event and are separated by ~1 Mpc from the cluster centre. Spectra for both the relics were estimated using the flux densities estimated from the MWA images along with those from previous observations of GMRT at 150 and 325 MHz and of VLA at 1400 MHz. The spectral indices of the east and west relics over the frequency range 80–1400 MHz are $-1.37 \pm 0.08$ and $-1.17 \pm 0.06$, respectively. The Mach numbers of the shocks estimated from these indices are consistent with those estimated from Suzaku X-ray observations. Assuming that the break frequency due to radiation losses corresponds to the lower end of the spectrum, the age of the relics can be estimated to be $\sim 0.37$ Gyr. This age is consistent with the age of the cluster estimated from simulations to be $\sim 0.5$ Gyr.

No diffuse radio emission was detected in the region between the relics. The upper limit on the radio power of any possible halo of 160 kpc size is $\sim 6 \times 10^{21}$ W Hz$^{-1}$ at 1.4 GHz. This is a factor of 35 lower than that expected from the correlation between radio powers and X-ray luminosities of cluster haloes. It is very likely that the radio emission from the halo has substantially decayed over its age ($\sim 0.37$ Gyr) considering that this time-scale is comparable to the lifetime of the radiating electrons at the MWA observing frequencies. The upper limit on the radio power of a halo in Abell 3376 is a factor of 10 lower than most upper limits available so far and is nearing levels at which radio emission from secondary electrons produced in relativistic proton–thermal proton collisions is expected. Given the uncertainties in the hadronic model (Brunetti & Lazarian 2011) it is not possible to discuss the validity of the model based on the observations of the cluster alone. However, observations of a large number of clusters with MWA and LOFAR at the current limits of detection or using the SKA at improved sensitivities will have implications on the hadronic model.

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