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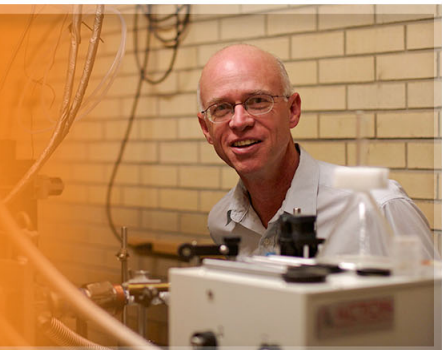
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On effective surface recombination parameters

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This paper examines two effective surface recombination parameters: the effective surface recombination velocity S_{eff} and the surface saturation current density J_{0s} . The dependence of S_{eff} and J_{0s} on surface charge Q , surface dopant concentration N_s , and interface parameters is derived. It is shown that for crystalline silicon at 300 K in low-injection, S_{eff} is independent of N_s only when $Q^2/N_s < 1900 \text{ cm}$ in accumulation and $Q^2/N_s < 1600 \text{ cm}$ in depletion; otherwise S_{eff} increases with N_s . These conditions are rarely satisfied in undiffused wafers but sometimes satisfied in heavily diffused wafers when coated with lowly charged films. Under the same conditions, J_{0s} is independent of N_s when $Q^2/N_s > 1.5 \times 10^7 \text{ cm}$ for accumulation and $Q^{1.85}/N_s > 1.5 \times 10^6 \text{ cm}$ for inversion. These conditions are commonly satisfied in undiffused wafers but rarely in diffused wafers. We conclude that for undiffused silicon, J_{0s} is superior to the conventional S_{eff} as a metric for quantifying the surface passivation, whereas for diffused silicon, the merit in using J_{0s} or S_{eff} (or neither) depends on the sample. Experimental examples are given that illustrate the merits and flaws of J_{0s} and S_{eff} . © 2014 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4886595>]

I. INTRODUCTION

The passivation of a semiconductor surface is commonly characterised by an “effective surface recombination velocity.”¹ This parameter combines a multitude of interface properties, making it simple to quantify and compare surface treatments.

The effective surface recombination velocity S_{eff} is defined by the equation

$$J_{rec} = qU_s = qS_{eff} \Delta n_d, \quad (1)$$

where J_{rec} is the current density that flows into the surface to recombine, q is the charge of an electron, U_s is the recombination rate at the surface in $\text{cm}^{-2}\text{s}^{-1}$, and Δn_d is the excess carrier concentration “near” the surface. As illustrated in Figure 1, the subscript d refers to the distance from the surface where the carrier concentrations are negligibly affected by surface charge. Usually, this distance is sufficiently close to the surface s that the difference between the doping concentrations at s and d is insignificant.

The merit in using a single parameter to quantify surface recombination is compromised when that parameter depends on properties unrelated to the passivation layer, such as the surface dopant concentration N_s or the excess carrier concentration away from the surface Δn_d . This is unfortunately the case for S_{eff} under most practical conditions. There are two reasons.

The first reason is that when surface charge is significant, S_{eff} depends on N_s and Δn_d .¹⁻⁴ In fact, for undiffused silicon wafers, very little surface charge is required to introduce this dependence (see Sec. VI). Without an appreciation of this effect, one might easily misinterpret the many observations of S_{eff} increasing with N_s [Refs. 5–12] as necessarily being caused by an underlying change to the interface (e.g., more defect states or increased capture cross sections).

The second reason is that S_{eff} necessarily depends on Δn_d over a large range of Δn_d as a result of recombination carrier statistics. This dependence arises when U_s transitions from being limited by the supply of minority carriers to being limited by the supply of both carrier species, as is evident from an examination of the Shockley–Read–Hall (SRH) equation for recombination through defect states.^{1,13,14} The resulting variation in S_{eff} has a complicated dependence on the doping concentration, the electron and hole capture cross sections, and the energy of the defect. Under certain conditions, the dependence of S_{eff} on Δn_d is negligible; this is the case for defects not near the band edges when the majority carrier capture cross section greatly exceeds the minority

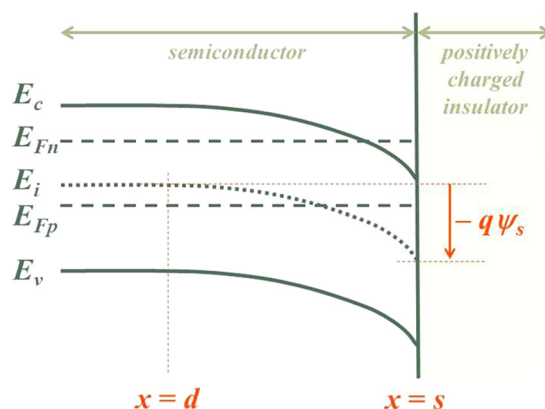


FIG. 1. Energy band diagram of a semiconductor–insulator interface under illumination, where the semiconductor is n-type and the insulator is positively charged. The diagram shows the energy of the conduction band E_c , the valence band E_v , the intrinsic Fermi level E_i , as well as the quasi-Fermi energy of electrons E_{Fn} and holes E_{Fp} . The location $x = s$ represents the surface of the semiconductor (i.e., the interface) and $x = d$ is the point at which the energy bands are unaffected by charge in the insulator or at the interface. The potential is defined to be zero at E_{id} (that is, E_i at $x = d$) and therefore band bending at the surface is given by $-q\psi_s = (E_{id} - E_{is})$.

carrier capture section. Under other conditions, S_{eff} varies over a range of Δn_d that is of no practical relevance, such as can occur when surface charge is large. But under many conditions, the dependence of S_{eff} on Δn_d is both significant and practically relevant, particularly when the minority carrier capture cross section exceeds the majority carrier cross section.

In this paper, we first introduce an alternative to S_{eff} called the surface saturation current density J_{0s} , which is analogous to the well-known emitter saturation current density J_{0e} . Like S_{eff} , J_{0s} suffers from being dependent on Δn_d and N_s due to SRH recombination statistics. It also depends on N_s when the surface charge is small. However, unlike S_{eff} , J_{0s} is independent of N_s and Δn_d when the surface charge is large, making it a superior metric for quantifying surface passivation.

After defining J_{0s} , we next derive S_{eff} and J_{0s} in terms of SRH recombination parameters for various special cases. For each case we show the ranges of surface charge and N_s over which S_{eff} and J_{0s} are independent of N_s . We can therefore conclude when it is preferable to use S_{eff} rather than J_{0s} , and vice versa. We find that for undiffused silicon, it is preferable to use J_{0s} under most practical conditions, whereas for diffused silicon, the benefit of using S_{eff} or J_{0s} (or neither) depends on the sample; we give examples of both.

II. DEFINITION OF J_{0s}

The surface saturation current density J_{0s} is analogous to the emitter saturation current density J_{0e} (Ref. 15) and is defined by the equation

$$J_{rec} = q U_s = J_{0s} \left[\frac{p_s n_s}{p_{0s} n_{0s}} - 1 \right]. \quad (2)$$

Equation (2) relates the recombination current to the concentration of holes and electrons in steady state (p and n) and at equilibrium (p_0 and n_0). As depicted in Figure 1, the subscript s refers to the actual surface of the semiconductor (i.e., the semiconductor–insulator interface), not some position near the surface.

The square-root of the product of the equilibrium concentrations is often called the effective intrinsic carrier concentration, $n_{ie} = \sqrt{p_{0s} n_{0s}}$. This parameter is dependent on the net doping concentration, $N = N_A - N_D$, due to band gap narrowing (BGN) and degeneracy.⁸ It is equal to n_i when $N = 0$, that is, when the semiconductor is intrinsic. For the equations that follow, we assume that n_{ie} is the same at s and d (i.e., that $p_{0s} n_{0s} = p_{0d} n_{0d}$), and Appendix A describes how those equations can be rewritten when $p_{0s} n_{0s} \neq p_{0d} n_{0d}$.

The first term in the square brackets of Eq. (2) relates to the separation of quasi-Fermi levels at the surface V_s . When Boltzmann statistics apply (i.e., in non-degenerate semiconductors), the equation can be rewritten in the familiar form of the diode equation

$$J_{rec} = J_{0s} \left[\exp \left(\frac{V_s}{V_T} \right) - 1 \right], \quad (3)$$

where V_T is the thermal voltage and equal to kT/q , k is Boltzmann's constant, and T is the absolute temperature.

It is not immediately apparent how or when J_{0s} offers an advantage over S_{eff} since its definition by Eq. (2) is more complicated than Eq. (1). It will be shown, however, that for undiffused silicon, J_{0s} is independent of N_s under most practical conditions, whereas S_{eff} is constant only when there is an impractically small surface charge and in low injection. The J_{0s} also has the advantage that for “transparent” emitters, it relates directly to the emitter saturation current density J_{0e} of a diffused surface.

III. DEPENDENCE OF J_{0s} ON SRH PARAMETERS

To show how J_{0s} depends on defect parameters, we begin with the SRH equation for a single defect energy,¹

$$U_s = \frac{p_s n_s - n_{ie}^2}{\frac{p_s + p_1}{S_{n0}} + \frac{n_s + n_1}{S_{p0}}}. \quad (4)$$

The terms p_1 and n_1 , which incorporate the thermal emission of carriers from the defect energy, are given by $n_1 = n_{ie} \exp[(E_t - E_i)/kT]$ and $p_1 = n_{ie} \exp[(E_i - E_t)/kT]$, where E_t is the energy of the defect state. The parameters S_{n0} and S_{p0} are the surface recombination velocity parameters of electrons and holes, respectively, and given by $S_{n0} = v_{thn} N_{it} \sigma_n$ and $S_{p0} = v_{thp} N_{it} \sigma_p$, where v_{thn} and v_{thp} are the thermal velocity of electrons and holes, σ_n and σ_p are the capture cross sections of electrons and holes, and N_{it} is the defect density in cm^{-2} .

Equation (4) is then rearranged to

$$U_s = \left[\frac{n_{ie}^2}{\frac{p_s + p_1}{S_{n0}} + \frac{n_s + n_1}{S_{p0}}} \right] \times \left[\frac{p_s n_s}{n_{ie}^2} - 1 \right], \quad (5)$$

and combined with Eq. (2) to give J_{0s} for a single SRH defect level

$$J_{0s} = \frac{q n_{ie}^2}{\frac{p_s + p_1}{S_{n0}} + \frac{n_s + n_1}{S_{p0}}}. \quad (6)$$

Equation (6) can be extended to a continuum of defect energies in the manner of Refs. 13 and 16. Appendix B describes how the accommodation of this continuum need not involve numerical integration across the band gap.

Thus, like U_s , J_{0s} depends on the equilibrium and steady-state carrier concentrations at the surface s . We now describe how they depend on surface doping and surface charge.

IV. SIMPLIFICATIONS TO THE SRH EQUATION

To illustrate the difference between S_{eff} and J_{0s} , we apply the SRH equation to n-type silicon and impose the restrictions that $n_s \gg n_1$, and $(n_s + n_1) / S_{p0} \gg (p_s + p_1) / S_{n0}$. This describes the situation where the defect is not very close to the band edges, where the sample is not highly depleted or in mild inversion, and where there is no great asymmetry in the capture cross sections. We also impose the restriction

that $p_s n_s \gg n_{ie}^2$, which is valid in all but very low injection. (This latter restriction is unnecessary in the following equations for J_{0s} but it does simplify S_{eff} .) The aforementioned conditions arise regularly, particularly when the doping or surface charge is high.

Under these assumptions Eq. (4) simplifies to

$$U_s = S_{p0} p_s. \tag{7}$$

S_{eff} for this simplified SRH equation is found by substituting Eq. (7) into Eq. (1) and by insisting that the equilibrium minority carrier concentration at d is negligible, and hence

$$n_d = N_D + \Delta n_d, \tag{8}$$

$$p_d \sim \Delta n_d, \tag{9}$$

which therefore gives

$$S_{eff} = S_{p0} \frac{p_s}{p_d}. \tag{10}$$

Thus, under the aforementioned conditions, S_{eff} equals S_{p0} only when $p_s = p_d$, that is, when there is negligible band bending at the surface. When positive surface charge is applied, $p_s < p_d$, making $S_{eff} < S_{p0}$. The converse also occurs for negative charge although either a very small or high negative charge is required to satisfy the aforementioned assumptions. It will be shown in Sec. V that when the charge is high enough, S_{eff} becomes proportional to n_d .

J_{0s} for the simplified SRH conditions is found by substituting Eq. (7) into Eq. (2) to give

$$J_{0s} = \frac{q S_{p0} n_{ie}^2}{n_s}, \tag{11}$$

where the value of this equation will become apparent once the dependence of n_s and p_s on charge has been described.

V. DEPENDENCE OF S_{eff} AND J_{0s} ON DOPING AND SURFACE CHARGE

The relationship between the carrier concentrations, band bending, and surface charge is governed by the well-known equation¹⁷

$$p_s - p_d + n_s - n_d + (N_A - N_D) \frac{\psi_s}{V_T} = \frac{Q^2}{2q\epsilon_{Si} V_T}, \tag{12}$$

where ψ_s is the surface potential relative to $\psi_d = 0$ (see Figure 1), ϵ_{Si} is the permittivity of the semiconductor, and Q is the charge within the semiconductor that is invoked to balance the sum of the charge in the insulator and at the insulator–semiconductor interface.¹⁶ The dimensions for Q are C/cm². Equation (12) assumes that the quasi-Fermi levels between s and d are flat.

The carrier concentrations can also be related to the band bending ψ_s . When Boltzmann statistics are applicable and the quasi-Fermi levels are flat, n_s and p_s can be written as

$$n_s = n_d \exp\left(\frac{\psi_s}{V_T}\right) \text{ and} \tag{13}$$

$$p_s = p_d \exp\left(-\frac{\psi_s}{V_T}\right), \tag{14}$$

and hence

$$p_s n_s = p_d n_d. \tag{15}$$

(More generally, the exponential functions can be replaced with the Fermi–Dirac function, as is required when Boltzmann statistics do not apply.)

Thus, in the manner described by Girisch *et al.*¹⁶ and its extension by Aberle *et al.*,¹³ one can combine Eqs. (4) and (12)–(14) to determine p_s and n_s , and then determine S_{eff} with Eq. (1) and J_{0s} with Eq. (2), or when applicable, with Eqs. (10) or (11). Girisch *et al.* show how to account for interface charge, which is also dependent on ψ_s .¹⁶

Since Eq. (12) is implicit, it must be solved numerically except when certain special cases are applicable. Solving Eq. (12) numerically is not difficult but it is instructive to derive explicit equations for U_s . We consider four special cases, all of which lead to a simple analytical equation for U_s and therefore for S_{eff} and J_{0s} . The main purpose of deriving these analytical equations is to help explain when S_{eff} and J_{0s} are independent of N_D .

The derivation of S_{eff} for the four special cases is similar to those derived by Kuhlmann,² Brody and Rohatgi,³ and Steingrube *et al.*,⁴ except that it includes the extensions of including Case 2 and of removing the requirement that there be either low- or high-injection in the remaining cases (though they remain predicated on the validity of Eq. (7)).

The four special cases are these

- (1) Q is negligibly small, and hence $\psi_s \sim 0$ and

$$n_s = n_d. \tag{16}$$

- (2) Q is sufficiently small that only the $k=2$ term in Eq. (C2) is significant (see derivation in Appendix C), and the sample is in low injection, $n_d \sim N_D$, and hence

$$n_s = n_d \exp\left[\frac{Q}{\sqrt{kT\epsilon_{Si} N_D}}\right]. \tag{17}$$

- (3) Q is sufficiently positive that the LHS of Eq. (12) equals n_s (i.e., $n_s \gg n_d, p_s, p_d$), and hence

$$n_s = \frac{Q^2}{2kT\epsilon_{Si}}. \tag{18}$$

- (4) Q is sufficiently negative that the LHS of Eq. (12) equals p_s (i.e., $p_s \gg n_s, n_d, p_d$), and hence

$$p_s = \frac{Q^2}{2kT\epsilon_{Si}}. \tag{19}$$

Notice that in Cases 3 and 4, n_s and p_s are independent of the doping N_D and the excess carriers Δn_d at d . In fact, for undiffused silicon, either Case 3 or 4 holds in most practical situations. (Also note that for Case 4, the inversion of the surface polarity converts Eqs. (7), (10), and (11) into $U_s = S_{n0} n_s$, $S_{eff} = S_{n0} n_s / p_d$, and $J_{0s} = q S_{n0} n_{ie}^2 / p_s$, respectively.)

TABLE I. Solutions for S_{eff} and J_{0s} in terms of SRH recombination parameters, surface charge Q and electron concentration at d ($n_d = N_D + \Delta n_d$) for n-type silicon under the restrictions required for Eq. (7) to be valid. With the exception of Case 2, the equations for S_{eff} have been derived previously for low injection ($n_d = N_D$) and $n_{is} = n_{id} = n_{ie}$ [Refs. 2–4]; Brody and Rohatgi also derive Case 4 for high injection.³

Case	Approximation	S_{eff}	J_{0s}
1	Negligible Q such that $n_s = n_d$	S_{p0}	$q \frac{S_{p0}}{n_d} n_{ie}^2$
2	Low Q , low injection	$S_{p0} \exp \left[\frac{-Q}{\sqrt{kT\epsilon_{Si}N_D}} \right]$	$q \frac{S_{p0}}{n_d} \exp \left[\frac{-Q}{\sqrt{kT\epsilon_{Si}N_D}} \right] n_{ie}^2$
3	Large positive Q (strong accumulation)	$S_{p0} n_d \frac{2kT\epsilon_{Si}}{Q^2}$	$q S_{p0} \frac{2kT\epsilon_{Si}}{Q^2} n_{ie}^2$
4	Large negative Q (strong inversion)	$S_{n0} n_d \frac{2kT\epsilon_{Si}}{Q^2}$	$q S_{n0} \frac{2kT\epsilon_{Si}}{Q^2} n_{ie}^2$

Section VI will define when these four special cases are valid, but before then, we examine how they simplify S_{eff} and J_{0s} . Table I lists the analytical expressions for S_{eff} and J_{0s} derived for each case. There are many other ways to manipulate the expressions; those given in Table I highlight the dependencies on N_D and Q .

In regards to S_{eff} , and keeping in mind that the derivations relied on the validity of Eq. (7), the most important features in Table I are these

- When Q and therefore band-bending is negligible, S_{eff} equals S_{p0} . Under this scenario (which rarely occurs for silicon), the common approach of employing S_{eff} to define surface passivation is substantiated because it is independent of n_d .
- When Q is not negligible, S_{eff} is linearly related to S_{p0} (or S_{n0}) but is also dependent on n_d and hence the doping and excess carriers at d .
- When Q is large, S_{eff} is proportional to $S_{p0}n_d$ (for positive Q) or $S_{n0}n_d$ (for negative Q).

It is evident, therefore, that unless Q is negligible, S_{eff} should not be stated without also stating n_d ; i.e., without stating the bulk doping and the excess carriers at d . This limits the applicability of using a measured S_{eff} as a boundary condition for simulating surfaces that do not have the same n_d .

In some experimental studies,^{5–12} S_{eff} is found to increase with N_D , making it look curiously like Q is not negligible in those experimental samples; in several of those works, Q is definitely not negligible and its influence on S_{eff} is described. There is evidence, however, from alternative experimental techniques that interface state densities can increase with N_s .^{18–20} Consequently, little can be concluded from experimental trends in $S_{eff}(N_s)$ without detailed investigation into the experimental samples.

Table I also gives equations for J_{0s} for each special case. The dependence of J_{0s} on Q exhibits the opposite trend to S_{eff} . That is, when Q is negligible, J_{0s} is inversely proportional to n_d . And when Q is large, J_{0s} is independent of doping (neglecting any influence on n_{is}) and it depends simply on S_{p0}/Q^2 or S_{n0}/Q^2 . This latter dependence can also be construed from (Ref. 2) using Eq. (3).

It is worth noting here that it would be preferable to treat J_{0s} as $J_{0s}/(qn_{ie}^2)$, which is common to all solutions in Table I, and which is measured by standard lifetime experiments before n_{ie} is unnecessarily estimated and extracted. Since the photovoltaics industry is already very familiar with the dimensions and typical magnitudes of J_0 , we do not present our results as $J_{0s}/(qn_{ie}^2)$ and do not mention it again.

VI. CONDITIONS WHEN J_{0s} AND S_{eff} ARE INDEPENDENT OF n_d

We now determine when the special cases are valid by evaluating the relative error that their underlying assumptions introduce into the minority carrier concentration at the surface. This is equivalent to the relative error in U_s for the conditions that give Eq. (7).

To demonstrate the difference between the above special cases, Figure 2 plots the relative error in p_s for Cases 1–3 and in n_s for Case 4. They are plotted as a function of band bending ψ_s for n-type silicon with $N_D = 10^{15} \text{ cm}^{-3}$ in low injection at 300 K using $n_{ie} = 10^{10} \text{ cm}^{-3}$ and Boltzmann statistics. Figure 2(a) includes all four cases and Figure 2(b) gives a “close up” of Cases 1–3 for clarity. Note that the doping concentration is only relevant for Case 4 for which the relative error increases with N_D .

The results of Figure 2 are now compared in terms of the range of ψ_s over which the relative error in p_s is less than

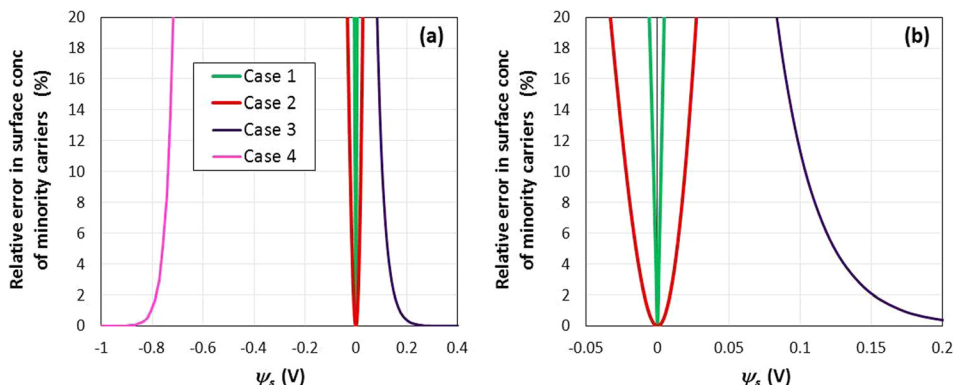


FIG. 2. Relative error in the minority carrier concentration at the surface as a function of the band bending ψ_s for the four special cases simulated for an n-type semiconductor. Thus, Cases 1–3 plot the error in p_s and Case 4 plots the error in n_s . Simulations conducted with $N_D = 10^{15} \text{ cm}^{-3}$, low injection ($\Delta n_d \ll N_D$), $n_{is} = n_{id} = 10^{10} \text{ cm}^{-3}$, and Boltzmann statistics. Figure (b) displays the results with a smaller x -axis range than (a) so that the results for Cases 1–3 are more easily discerned.

10%. For Case 1, this only occurs when ψ_s is very close to zero: $-2.72 \text{ mV} < \psi_s < 2.46 \text{ mV}$. Hence, band bending must be very small for S_{eff} to be independent of n_d . The asymmetry is genuine. It can be shown that for the assumptions contained in Figure 2, the relative error in p_s equals $\exp(\psi_s/V_T) - 1$.

For Case 2, the relative error in p_s is less than 10% when $-22.0 \text{ mV} < \psi_s < 19.3 \text{ mV}$. This range is almost 10 times greater than for Case 1. Case 2 therefore provides a useful explicit expression that can be applied in low injection when the charge is small, but it does not mean that S_{eff} is independent of N_D .

For Case 3, the valid range is $\psi_s > 103.7 \text{ mV}$. This is an important case. When it holds, S_{eff} is proportional to n_d , and J_{os} is independent of n_d . It can be shown that the relative error in p_s equals $[\exp(\psi_s/V_T)/(\exp(\psi_s/V_T) - (\psi_s/V_T) - 1)] - 1$.

And finally, for Case 4 (strong inversion) the valid range is $\psi_s < 0.738 \text{ V}$. This limit is strongly dependent on N_D (whereas the limit is independent of N_D for the first three cases). The dependence on N_D is introduced by the p_s term on the LHS of Eq. (12). The equation for the relative error in n_s is $[1 + N_D^2/n_i^2 \times \exp(\psi_s/V_T) \times (\exp(\psi_s/V_T) - (\psi_s/V_T) - 1)]^{-1} - 1$, which assumes p_d is negligible; notice the dependence on N_D in this equation.

Thus, the validity of the various special cases, and therefore the relevance of S_{eff} and J_{os} , depends on ψ_s , which itself depends on Q , N_D and Δn_d .

In Figure 3, we show when each special case is valid at 300 K for c-Si in low injection as a function of Q and N_s for both accumulation and depletion/inversion. We adopt the symbol N_s to represent the surface dopant concentration, because the figure is independent of whether the sample is n -type or p -type. In Figure 3, the x-axis is N_s , which is equivalent to n_d for n -type or p_d for p -type since low-injection requires $\Delta n_d \ll N_s$. The results for non-negligible Δn_d are discussed later with reference to Figure 4.

In Figure 3, the yellow contour shows the range of Q and N_s where Case 1 is applicable; i.e., where the approximation that $n_s = n_d$ and $p_s = p_d$ is correct to within 10% error. Thus, at all points shaded yellow in Figure 3, one can reliably assume that in low injection, S_{eff} equals the minority carrier recombination velocity, either S_{p0} or S_{n0} (provided the assumptions entailed in Eq. (7) are valid). One can also reliably assume that S_{eff} is independent of N_s (provided the simplified SRH equation is applicable). These lines are governed by the equations $(Q/q)^2 = N_s \times 1900 \text{ cm}$ for accumulation and $(Q/q)^2 = N_s \times 1600 \text{ cm}$ for depletion.

The red contour shows the range of Q and N_D where Case 2 is applicable. At points where $|Q|$ is less than this line (either the red or yellow shaded regions), the approximation that $n_s = n_d \exp[Q/\sqrt{qV_T\epsilon_{Si}N_D}]$ is correct to within 10% error for c-Si in low injection.

The blue contours indicate the range of Q and N_D where Cases 3 and 4 are applicable for accumulation and for inversion, respectively. That is, at all points above the blue line for accumulation, or below the blue line for inversion (shaded in blue), the approximation that either n_s or p_s equals $Q^2/2q\epsilon_{Si}V_T$ is correct to within 10% error. In these regions, it can be reliably assumed that J_{os} is independent of N_s (provided the simplified SRH equation is applicable). These lines

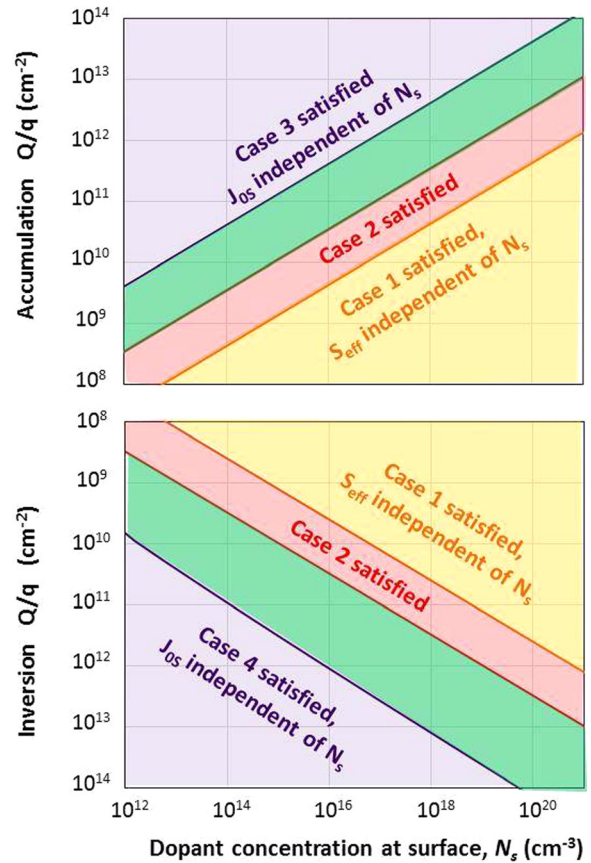


FIG. 3. Contours show where the given assumption represents a 10% error in the calculation of surface dopant concentration in low injection for c-Si at 300 K; valid for either p-type or n-type c-Si.

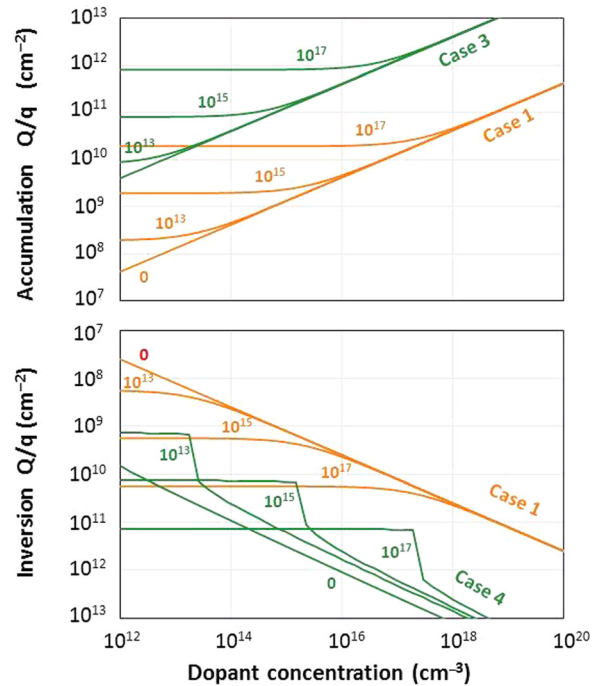


FIG. 4. Contours show where Cases 1, 3, and 4 give a 10% error in the calculation of the minority carrier surface concentration for c-Si at 300 K; valid for either p-type or n-type c-Si. The contours show Δn_d , the excess carrier concentration in cm^{-3} at d , where the lines for $\Delta n_d = 0 \text{ cm}^{-3}$ are identical to those shown in Figure 3. S_{eff} is independent of N_s when $|Q|$ is smaller than the orange lines, and J_{os} is independent of N_s when $|Q|$ is larger than the green lines.

are governed by the equations $(Q/q)^2 = N_s \times 1.5 \times 10^7$ cm for accumulation and $(Q/q)^{1.85} \sim N_s \times 1.5 \times 10^6$ cm for inversion.

When comparing accumulation to inversion, there is a slight asymmetry in the yellow and red contours; this asymmetry is smaller when a smaller error limit is applied. By contrast, there is a larger difference between the accumulation and inversion between Case 3 and Case 4, which represent the conditions under which n_s and p_s are independent of N_s . In inversion, a significantly higher Q is required to meet the same error limit, where the relative increase in Q increases with N_D .

Figure 3 shows that for some ranges of N_s and Q , none of the special cases are justified. This is the region shaded in green. The complicated effects of Q on $U_s(\Delta n_d)$ within this range have been examined elsewhere.^{1,3,13,21}

We conclude from Figure 3 that for undiffused c-Si, which typically has $N_s < 10^{16}$ cm⁻³, Case 1 is unjustified unless $|Q|$ is impractically small (less than 5×10^9 cm⁻²). For diffused c-Si, Case 1 might become valid for dielectrics with a small $|Q|$ when $N_s > 10^{19}$ cm⁻³. To our knowledge, no experimental studies justify the application of Case 1, and it is therefore not recommended that S_{eff} be assumed equal to S_{n0} or S_{p0} , or constant with doping for silicon at 300 K.

Figure 3 shows that Case 2 can be used to solve Eq. (12) as an explicit analytical solution over a significantly larger range of Q than Case 1. In practise, it would likely be limited to diffused samples with lowly charged dielectrics.

Figure 3 also shows that Cases 3 and 4 will often be justified for undiffused c-Si. A charge density great than 3×10^{11} cm⁻² for accumulation, and 1×10^{12} cm⁻² for inversion, is required when $N_s < 10^{16}$ cm⁻³, but these limits decrease as N_s decreases. In such case, J_{os} is independent of N_s , making it a much more useful effective recombination parameter than S_{eff} . We also see that very high charge densities are required to justify Cases 3 or 4 for diffused silicon. Recent experiments with Al₂O₃ on p-type Si with $Q/q \sim -2 \times 10^{12}$ cm⁻² clearly showed that Case 3 was unjustified for $N_s > 10^{18}$ cm⁻³,¹² consistent with Figure 3.

Finally, we conclude that for diffused silicon and typical charge densities of dielectrics, the most likely scenario is that neither S_{eff} nor J_{os} will be independent of N_s . That is, as N_s increases for diffused silicon, S_{eff} would increase and J_{os} would decrease, even when S_{p0} (or S_{n0}) are constant.

For simplicity, Figure 3 was restricted to low-injection at d ; that is $\Delta n_d \ll N_D$. This condition is readily justified for diffused silicon surfaces. (Note that requiring low-injection

at d is a substantially more lenient requirement for diffused surfaces than for undiffused surfaces.)

Figure 4 presents the equivalent situation for several values of Δn_d . In this figure, we do not include the same shading as Figure 3, and we omit the contours for Case 2, which necessarily required low injection. The figure shows that as Δn_d increases, the range over which Case 1 is valid increases. That is, at small N_s , Case 1 is valid at higher Q as Δn_d increases. Nevertheless, it does not change the major conclusion that Case 1 will rarely hold in practical situations. For Case 3, the range of validity decreases, but nevertheless, it should remain valid for most practical cases for undiffused silicon (except for very high Δn_d).

VII. EXPERIMENTAL-UNDIFFUSED SILICON

There are many published examples where the surface recombination of undiffused c-Si is better represented by a J_0 than an S_{eff} [e.g., Refs. 22 and 23]. In these cases, U_s is proportional to $p_d n_d$ rather than to either p_d or n_d over a wide range of Δn_d . This is equivalent to stating that the surface recombination follows Eq. (2) rather than Eq. (1), and hence, that there is sufficient surface charge for either Case 3 (accumulation) or Case 4 (strong inversion) to be valid.

In Figure 5, we present lifetime measurements that represent Case 4 (strong inversion). The experimental sample is a planar n-type silicon wafer ($N_D = 3.0 \times 10^{15}$ cm⁻³) coated with Al₂O₃ on both surfaces. Its effective lifetime was measured as a function of Δn_d by photoconductance using a Sinton Instruments WCT-120 lifetime tool.²⁴

Figure 5(a) plots the effective lifetime of the sample before and after the sample was annealed at 425 °C for 30 min. The anneal caused a significant increase in the effective lifetime, which can be attributed to improved surface passivation by the Al₂O₃.^{12,25}

Figure 5(b) plots the inverse effective lifetime against Δn_d , where the Auger recombination in the bulk of the wafer has been extracted in the conventional way²⁶ using the parameterisation of Richter *et al.*²⁷ As is well documented [e.g., Refs. 26 and 28], a J_0 of the sample can be extracted from the slope of the data in Figure 5(b) provided that the slope is constant over a wide range of Δn_d . This provision is satisfied for the pre-annealed sample, for which $J_{os} = 12$ fA/cm². By applying the appropriate equation in Table I, J_{os} can then be converted to $S_{p0}/Q^2 = 8.6 \times 10^{16}$ cm⁴C⁻²s⁻¹.

For the post-annealed sample, the slope of the data in Figure 5(b) is clearly not straight. Consequently, J_{os} cannot

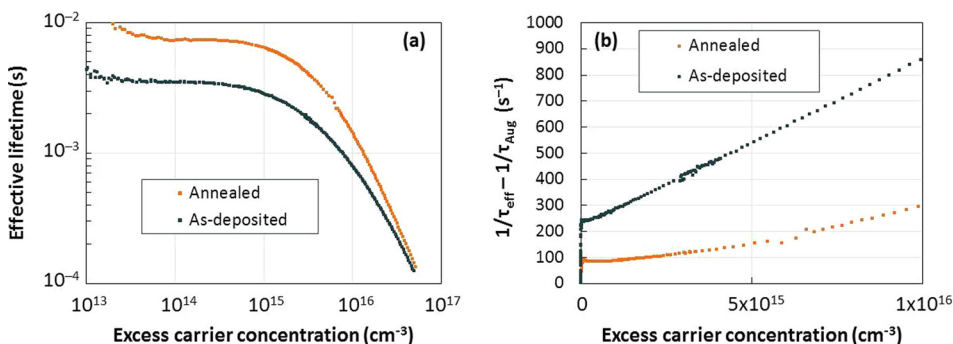


FIG. 5. Photoconductance lifetime measurements on undiffused n-type silicon passivated with Al₂O₃ before and after an anneal, plotting (a) effective lifetime against Δn_d , and (b) the same data presented as the inverse effective lifetime and where Auger recombination in the bulk has been extracted.

be reliably extracted without additional information about the sample. The most likely cause for this feature is that the bulk recombination is neither negligible nor constant with Δn_d .

From this example—and several others in the literature [e.g., Refs. 22 and 23]—it is evident that J_{0s} can be directly determined from lifetime measurements on non-diffused samples that have a high surface charge (provided that bulk recombination is either negligible or constant with Δn_d).

VIII. EXPERIMENTAL—DIFFUSED SILICON

Lifetime measurements are routinely employed to determine the recombination current of heavily doped layers J_{0e} (e.g., an emitter or a back-surface field). The J_{0e} depends on the SRH recombination at the surface, and on the SRH and Auger recombination within the layer. The contributions to the J_{0e} made by these mechanisms,

$$J_{0e} = J_{0e, \text{surface SRH}} + J_{0e, \text{SRH}} + J_{0e, \text{Auger}}, \quad (20)$$

can be determined by a careful simulation of the heavily doped layer.^{15,29–31} This requires consideration of carrier mobility, band-gap narrowing, Fermi–dirac statistics, interface properties, and the Auger coefficients. The parameters in Eq. (20) can be determined directly with EDNA 2 (Refs. 31 and 32) or construed from the outputs of device simulators such as PCID³³ and Sentaurus,³⁴ or from various analytical approaches.²⁹

In Figure 6(a), we re-plot the recent results of Ref. 12 to show J_{0e} , $J_{0e, \text{surface SRH}}$ and $J_{0e, \text{Auger}}$ for 21 samples, where the x-axis label states the boron surface concentration N_s . $J_{0e, \text{SRH}}$ is assumed negligible.¹² These results were derived from planar c-Si wafers diffused with boron and coated with Al_2O_3 . The figure shows that the contribution to J_{0e} from surface recombination is relatively constant with surface concentration; by contrast, the contribution from Auger recombination increases substantially and this is the reason that J_{0e} increases with N_s .

In Figure 6(b), we plot S_{eff} and J_{0s} against N_s , where the simulation with EDNA 2 is used to determine S_{eff} via Eq. (1) and J_{0s} via Eq. (2). The symbols represent the experimental diffused (circles) and undiffused (squares) *p*-type samples. The lines in Figure 6(b) are simulated from the interface parameters determined by CV measurements on undiffused samples, as described in detail in Ref. 12.

Figure 6(b) shows that S_{eff} increases with N_s , as has often been observed in studies on heavily doped silicon.^{5–12} (Exceptions to this trend also exist^{35,36}). It would be wrong to conclude, however, that the reason that S_{eff} increases with N_s is necessarily because Q decreases or S_{n0} increases (e.g., by an increase in interface defects). It was shown in Ref. 12 that the dependence of J_{0e} on N_s presented in Figure 6(b) is entirely consistent with a constant S_{n0} of 1.1×10^4 cm/s and a constant Q/q of -1.7×10^{12} cm⁻². Thus, the increase in S_{eff} observed in Figure 6(b) is an artefact of its derivation, as explained in Sec. V. In short, the surface charge is too large for Case 1 to be satisfied, and thus S_{eff} necessarily depends on N_s . Put otherwise, N_s and Q do not fall within the yellow region of Figure 3.

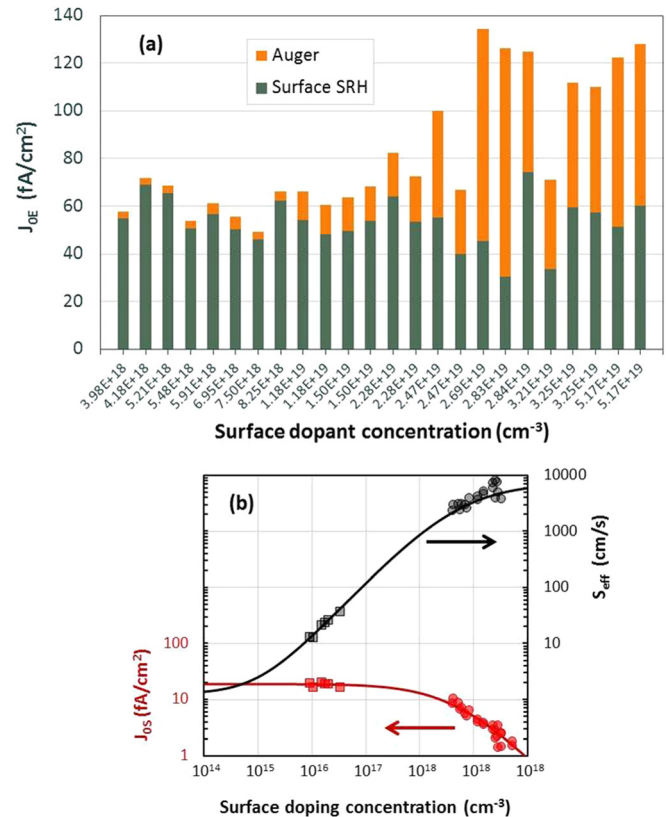


FIG. 6. Photoconductance lifetime measurements of Al_2O_3 -coated Si wafers presented in Ref. 12 replotted to show (a) experimental J_{0e} and calculated $J_{0e, \text{surface SRH}}$ and $J_{0e, \text{layer Auger}}$, and (b) S_{eff} and J_{0s} against the boron surface concentration.

In summary, plots of S_{eff} against N_s are easily misconstrued. Here, the example illustrates how S_{eff} can increase with N_s when all interface parameters are constant with N_s . We do not discount the possibility that in some structures, interface parameters could change with N_s , as has been concluded by other experimental techniques,^{18–20} but it is clear that changes in interface parameters cannot be determined from $S_{\text{eff}}(N_s)$ without accounting for the influence of Q , N_s , Δn_d , and the assumptions entailed in Eq. (7). Moreover, when N_s is high, analyses need also account for uncertainties in the physical models for band-gap narrowing and Auger recombination (which are currently rather large), as well as variations in n_{ie} between $x=s$ and $x=d$ as outlined in Appendix A.

Finally, Figure 6(b) plots J_{0s} vs N_s , as determined by Eq. (2). At $N_s < 10^{17}$ cm⁻³, J_{0s} is approximately constant with N_s , indicative of Q being sufficiently large relative to N_s that Case 3 is satisfied (i.e., the samples are within the blue region of Figure 3). In this range, J_{0s} is a particularly useful parameter because it provides a single value to quantify the surface passivation and is independent of the substrate properties (N_s and Δn_d).

At $N_s > 10^{17}$ cm⁻³, J_{0s} decreases with N_s . Over this range, J_{0s} is as flawed as S_{eff} in quantifying the surface passivation, because neither parameter defines the quality of the surface passivation independently of the substrate properties.

IX. CONCLUSION

This paper described two effective surface recombination parameters, S_{eff} and J_{0s} . Their dependence on interface parameters and dopant surface concentration N_s was derived. It was found that for c-Si at 300 K in low-injection, S_{eff} is independent of N_s only when $Q^2/N_s < 1900$ cm for accumulation and < 1600 cm for depletion; otherwise S_{eff} increases with N_s . This condition would be rarely satisfied in undiffused wafers but sometimes satisfied in heavily diffused wafers (provided they are coated with lowly charged films). Also for c-Si at 300 K in low-injection, J_{0s} is independent of N_s when $Q^2/N_s > 1.5 \times 10^7$ cm for accumulation and $Q^{1.85}/N_s > 1.5 \times 10^6$ cm for inversion. These conditions are commonly satisfied in undiffused wafers but rarely in diffused wafers. Thus, J_{0s} is a superior metric for comparing surface passivation of undiffused samples than the current convention of comparing S_{eff} ; nevertheless, the derivation and limitations of J_{0s} should be understood before its widespread application.

APPENDIX A: EQUATIONS WHEN $p_{0s}n_{0s}$ DOES NOT EQUAL $p_{0d}n_{0d}$

The equations in the main body of this paper were derived under the assumption that $p_{0s}n_{0s} = p_{0d}n_{0d}$; that is, that the effects of BGN and degeneracy are identical at s and d . This appendix states how the equations would be re-expressed without this assumption. We now use n_{is}^2 to represent $p_{0s}n_{0s}$ and n_{id}^2 to represent $p_{0d}n_{0d}$.

In Eqs. (4)–(6) and (11), as well as all equations for J_{0e} in Table I, n_{ie} should be replaced with n_{is} .

Equations for S_{eff} in Table I (except Case 1) should be multiplied by the factor n_{is}^2/n_{id}^2 .

Equations (13)–(15) should be rewritten

$$n_s = \frac{n_{is}}{n_{id}} n_d \exp\left(\frac{\psi_s}{V_T}\right), \quad (\text{A1})$$

$$p_s = \frac{p_{is}}{p_{id}} p_d \exp\left(-\frac{\psi_s}{V_T}\right), \text{ and} \quad (\text{A2})$$

$$\frac{p_s n_s}{n_{is}^2} = \frac{p_d n_d}{n_{id}^2}. \quad (\text{A3})$$

APPENDIX B: THE DEPENDENCE OF S_{p0} AND S_{n0} ON ENERGY-DEPENDENT DEFECTS

Defect states at a semiconductor surface do not have the same energy at all spatial locations. Instead, there is a distribution of defect energies introduced by variable bond strain. The capture cross sections are also often assumed to vary with the energy of the defect.¹ To account for these energy dependences when determining U_s , an approach that integrates the SRH equation as a function of energy is often applied, for which the energy-dependent variables are n_1 , p_1 , D_{it} , σ_p , and σ_n . When this is the case, the SRH equation is¹

$$U_s = (p_s n_s - n_{is}^2) \int_{E_v}^{E_c} \frac{dE}{\frac{p_s + p_1(E)}{S_{n0}(E)} + \frac{n_s + n_1(E)}{S_{p0}(E)}}, \quad (\text{B1})$$

where $S_{n0}(E) = v_{thn} D_{it}(E) \sigma_n(E)$ and $S_{p0}(E) = v_{thp} D_{it}(E) \sigma_p(E)$.

The principle problem with solving Eq. (B1) is that it requires an intimate knowledge of the interface. That is, for any given passivation scheme and sample, researchers must determine many energy-dependent values in order to determine U_s from its interface parameters.

When four particular requirements are satisfied, however, a far simpler relationship between U_s and the interface parameters can be derived. The first requirement is that n_1 and p_1 be negligible, as occurs when there is negligible recombination through defects with energies near the band edge. This requirement is met by Si–SiO₂ (Ref. 37) and Si–Al₂O₃.³⁸ The second requirement is that $\sigma_p(E)$ and $\sigma_n(E)$ exhibit a negligible dependence on E for each defect. Careful experimentation suggests that this is a reasonable approximation for Si–SiO₂ (Refs. 39–43) and Si–Al₂O₃.^{38,12} The third requirement is that the energy distribution of the defect can be represented by a Gaussian distribution

$$D_{it}(E) = D_{itmax} \exp\left[-\left(\frac{E - E_{max}}{\sqrt{2}\mu}\right)^2\right], \quad (\text{B2})$$

where D_{itmax} and E_{max} are the D_{it} and energy at the peak of the distribution, and μ is the standard deviation of the distribution. (In fact, any distribution whose integral between E_v and E_c is approximately the same as the integral between $-\infty$ and $+\infty$ will do.) The fourth and final requirement—as was imposed in the main body of the paper—is that only one of the denominator terms in the SRH equation is significant.

When satisfied, these four simplifications modify Eq. (B1) to give

$$U_s = p_s S_{p0}, \quad (\text{B3})$$

where

$$S_{p0} = v_{th} \sigma_p D_{itmax} \int_{E_v}^{E_c} \exp\left[-\left(\frac{E - E_{max}}{\sqrt{2}\mu}\right)^2\right] dE, \quad (\text{B4})$$

which for a strongly peaked distribution, solves to give

$$S_{p0} = \sqrt{2\pi} v_{th} \sigma_p D_{itmax} \mu. \quad (\text{B5})$$

An analogous equation can be derived for S_{n0} .

The principle value of Eq. (B5) lies in its simplicity. It states that the recombination is independent of defect energy E and can be computed without numerical integration. Moreover, for a given defect type, where one might expect σ_p and μ to vary little from sample to sample, one could state that

$$S_{p0} = c_{defect} D_{itmax}, \quad (\text{B6})$$

where c_{defect} is a constant that represents a type of defect, such as the P_b bond at the Si–SiO₂ interface,⁴⁴ or the principle donor-like bond at the Si–Al₂O₃ interface.³⁸ If this proves viable, then it enables a simpler comparison between passivation schemes, deposition technologies, and annealing conditions. For a given interface, once c_{defect} is determined

for one passivation scheme, one need only determine $D_{it\ max}$ to calculate the recombination velocity of any other substrate passivated by the same scheme.

We emphasise that Eq. (B6) entails several assumptions and should only be applied after they have been appropriately assessed.

APPENDIX C: EXPLICIT SOLUTIONS TO EQUATION (12) WHEN THE SURFACE IS IN WEAK DEPLETION OR ACCUMULATION

We can find explicit solutions to Eq. (12) for the condition where the majority carrier concentration is far greater than the minority carrier concentration at both s and d . This is valid from weak depletion to strong accumulation. In the case of an n -type semiconductor, this requires $n_s, n_d \gg p_s, p_d$, simplifying Eq. (12) to give

$$\exp\left(\frac{\psi_s}{V_T}\right) - 1 - \frac{N_D \psi_s}{n_d V_T} = \frac{Q^2}{2q\epsilon_s V_T n_d}. \quad (\text{C1})$$

In low injection, when $n_d \sim N_D$, it can be further simplified by noting that the LHS is a partial Maclaurin series

$$\sum_{k=2}^{\infty} \frac{(\psi_s/V_T)^k}{k!} = \frac{Q^2}{2q\epsilon_s V_T N_D}. \quad (\text{C2})$$

In Case 1, Q is sufficiently small that ψ_s is negligible; in Case 2, Q is sufficiently small that only the $k=2$ term is significant and the LHS of Eq. (C1) equals $(\psi_s/V_T)^2/2$; in Cases 3 and 4, the LHS of Eq. (C1) is assumed equal to $\exp(\psi_s/V_T)$.

For p -type, N_D in Eq. (C2) is replaced by N_A .

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