

## MINERAL SOLUBILITY AND HYDROUS MELTING RELATIONS IN THE DEEP EARTH: ANALYSIS OF SOME BINARY A–H<sub>2</sub>O SYSTEM PRESSURE-TEMPERATURE-COMPOSITION TOPOLOGIES

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**ABSTRACT.** Phase relations involving hydrous melting, volatile and mineral solubility and supercritical fluid phenomena at high pressure for mineral–H<sub>2</sub>O systems are generally not completely constrained by experimental data or adequately treated in thermodynamic models. Here we examine geometric relations in pressure (*P*)-temperature (*T*)-composition (*X*) topologies of simple hydrous A–H<sub>2</sub>O binaries, thus avoiding some of the pitfalls associated with other approaches. The relations between mineral solubility surfaces, wet melting and critical L=V behavior are shown explicitly in a series of *PT*, *TX* and isopleth contoured *PT* projections. Our analysis highlights the significance of Clapeyron slopes of melt- and fluid-solubility isopleths for L+V coexistence, supercritical-fluid phenomena and the geometry of phase-equilibrium boundaries. The results are useful for understanding wet melting, magma degassing and fluid behavior in high-pressure metamorphic and subduction-zone environments. The diagrams illustrate the general pattern of mineral solubility in aqueous fluids and volatile solubility in silicate melts. We discuss the significance of the critical-curve geometry for phase relations and fluid/melt densities. We examine a continuum of phase relation topologies for A–H<sub>2</sub>O, and show that these can result from subtle but important differences in the compositional behavior of melt coexisting with H<sub>2</sub>O-rich fluid. The systems SiO<sub>2</sub>(quartz)–H<sub>2</sub>O and NaAlSi<sub>3</sub>O<sub>8</sub>(albite)–H<sub>2</sub>O are taken as examples for which there is experimental data available to calibrate a complete phase relation topology.

### INTRODUCTION

Recently there has been renewed interest in the nature and occurrence of supercritical fluids with hydrous-melt-like properties in geological processes. This renaissance is due mostly to the recognition that pressure, temperature conditions in subduction zones might be suitable to form supercritical fluids (for example, Massonne, 1992; Sharp and others, 1993; Scambelluri and Philippot, 2001; Hermann, 2003; Audétat and Keppler, 2004; Kessel and others, 2005a, 2005b; Hermann and others, 2006).

Considerable uncertainty attends discussion of the role and nature of fluids in deep-seated geological processes. In part this is because natural fluids are ephemeral, so that the details of fluid–rock interactions must be inferred indirectly, for example from major and trace element depletions or enrichments (Ague, 1994a, 1994b, 1997). Although fluid inclusions are occasionally identified in high-temperature, high-pressure rocks, their provenance is usually equivocal and/or they have decrepitated during exhumation (Invernizzi and others, 1998; Scambelluri and others, 2001; Ferrando and others, 2005).

Experimental studies and thermodynamic models of phase equilibria and solubility relations in rock–H<sub>2</sub>O systems provide independent constraints on the behavior and composition of minerals, fluids and melts at high-pressure and -temperature conditions. However, large regions of pressure-temperature-composition (*PTX*) space

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remain experimentally unexplored even for simple systems like  $\text{SiO}_2\text{-H}_2\text{O}$  and  $\text{NaAlSi}_3\text{O}_8\text{(albite)-H}_2\text{O}$ , with fluid compositions being probably the least known. Similarly, thermodynamic models (for example, Holland and Powell, 1998, 2001) typically do not treat all experimentally observed phenomena, such as complete fluid–melt miscibility (for example, Kennedy and others, 1962; Shen and Keppeler, 1997; Kessel and others, 2005a, 2005b), reflecting the paucity of data to calibrate thermochemical models.

Theoretical descriptions of the general *PTX* phase relation topology for various types of simple two component ( $A\text{-H}_2\text{O}$ ) systems have been available for a long time (for example, Morey and Niggli, 1913). However, these are seldom used except schematically in the geological literature. This is because, until recently, experimental constraints for real systems were insufficient to construct calibrated topologies. These kinds of topological frameworks can be integrated with fragmentary experimental data to circumvent limitations imposed by incomplete thermodynamic models and experimental data, to provide both conceptual insights and predictive constraints on the compositional behavior of each phase (for example, fluid and melt) over the entire *PT* space.

In this paper we examine a topological framework for a generic two-component silicate–water system ( $A\text{-H}_2\text{O}$ ), with a minimum of schematic distortion and explicitly show the systematics of how fluid and melt compositions relate to the phase relations, for example, the wet solidus and critical phenomena. Using this framework, we construct a semi-quantitative model of the system  $\text{SiO}_2\text{-H}_2\text{O}$ , which predicts the composition of the buffered fluid at any *P* and *T*. We discuss the general implications of the results, highlight the constraints imposed by experimental data and the phase relations that remain possible, yet rarely considered. The aim of this contribution is to clarify the links between changes in *PT*, fluid and melt compositions, and phase relations for simple systems.

#### BACKGROUND

The topological configuration of simple two-component systems ( $A\text{-H}_2\text{O}$ ) in which one component is highly volatile ( $\text{H}_2\text{O}$ ) has been known since at least Morey and Niggli (1913). Numerous detailed discussions of these ideal relations are available (for example, Ricci, 1951; Morey, 1957; Wyllie and Tuttle, 1960; Fyfe and others, 1978; Paillat and others, 1992; Manning, 2004; Veksler, 2004). Accordingly, only a brief summary is given here. In this paper we broadly follow the nomenclature given in Boettcher and Wyllie (1969a). A brief glossary of the terms and abbreviations is given in table 1.

One-component systems, like  $\text{H}_2\text{O}$  or *A*, have a liquid+vapor coexistence curve that at high-temperature terminates at a critical point (fig. 1, for  $\text{H}_2\text{O}$ :  $T_{\text{crit}} = 374\text{ }^\circ\text{C}$ ,  $P_{\text{crit}} = 22.1\text{ MPa}$ , critical density =  $0.32\text{ g/cm}^3$ , Haar and others, 1984). With increasing temperature along this curve, the properties of the liquid and vapor converge to the extent that liquid and vapor become indistinguishable at the critical point (analogous to the closing of a miscibility gap or solvus). At *T* and *P* above the critical point, a single supercritical fluid is stable. In the two-component system  $A\text{-H}_2\text{O}$ , a  $L=V$  critical curve connects the critical points in the end-member systems. Along the  $L=V$  critical curve liquid and vapor are indistinguishable, the curve represents the maximum *P*, *T* and *X* extent of the liquid–vapor miscibility gap (that is, the *PT* loci of the  $L\text{-V}$  solvus crest). At *T*, *P* above the critical curve one, supercritical, fluid is stable. Though not obvious from figure 1, the critical composition along the critical curve varies continuously from  $\text{H}_2\text{O}$  to *A* between the respective critical points. A second curve defined by the coexistence of three phases, solid-*A*+liquid+vapor, extends from the low-temperature  $A\text{-H}_2\text{O}$  eutectic point to the triple point for *A* (solid+liquid+vapor) where it terminates, is termed the solubility curve (fig. 1).

TABLE 1  
*Symbols used*

$P$	Pressure 1 bar = $10^5$ Pa, 1 GPa = $10^4$ bar = 10 kbar
$T$	Temperature usually as celsius, otherwise kelvin
$X$	Composition (usually by weight, otherwise molar)
$A$	silicate, the non-volatile component, in the solid state at room conditions
$S_A$	pure $A$ in the solid state*
$L_A$	pure $A$ in the liquid state
$G_A$	pure $A$ in the vapor state
$\text{H}_2\text{O}$	water, in the liquid state at ambient $T,P$ , the volatile component
ice	pure $\text{H}_2\text{O}$ in the solid state
steam	pure $\text{H}_2\text{O}$ in the vapor state
$A\text{-H}_2\text{O}$	simple binary system of interest
$V$	aqueous Vapor (= $\text{H}_2\text{O}$ with dissolved $A$ )
$L$	hydrous Liquid/melt (= $L_A$ with dissolved $\text{H}_2\text{O}$ )
Eut( $\text{H}_2\text{O}\text{-}S_A$ )	$\text{H}_2\text{O}\text{-}S_A$ eutectic point, where ice+ $S_A$ + $L$ + $V$ are in equilibrium
Trip.pt $\text{H}_2\text{O}$	triple point of pure $\text{H}_2\text{O}$ ( $L+V+S$ )
Trip.pt $A$	triple point of pure $A$ ( $L+V+S$ )
$k_{\text{H}_2\text{O}}$	$L=V$ critical point on the boiling curve of $\text{H}_2\text{O}$
$k_A$	$L=V$ critical point on boiling curve of pure $A$
$k_1(L=V)A$	lower $L=V$ critical endpoint on the vapor+liquid coexistence curve where $A$ is stable as a solid in the binary $A\text{-H}_2\text{O}$
$k_2(L=V)A$	upper $L=V$ critical endpoint in the binary $A\text{-H}_2\text{O}$ wet solidus ( $A$ is stable as a solid at this point)
$L=V$	the condition where $L$ and $V$ become indistinguishable at the closure of the $L+V$ solvus
SCF	SuperCritical Fluid, a completely miscible continuous solution. Where SCF is stable $L$ and $V$ do not coexist as immiscible phases

\* $A$  is refractory (or has low-volatility) as it is solid ( $S_A$ ) under most of the  $PT$  conditions considered (unless specified)

Morey and Niggli (1913) recognized two basic types of  $A\text{-H}_2\text{O}$  topology based on whether the critical and solubility curves remain separated (fig. 1A) or intersect in  $PTX$  (fig. 1B). The first type of behavior is characteristic of systems in which solid  $A$  is highly soluble in  $\text{H}_2\text{O}$ , a geological example is  $\text{NaCl}\text{-H}_2\text{O}$  (Sourirajan and Kennedy, 1962). The second type, where the critical and solubility curves intersect, is characteristic of systems in which solid  $A$  is sparingly soluble in  $\text{H}_2\text{O}$  (for example,  $\text{SiO}_2\text{-H}_2\text{O}$ , Kennedy and others, 1962). In this study we are concerned only with the second type, as it is appropriate generally to silicate- $\text{H}_2\text{O}$  systems.

Intersection of the solubility and critical curves produces two separate  $P, T$  regions where a liquid-vapor miscibility gap is stable and there is a discontinuity in the solubility curve (fig. 1B). In the geological literature, the high-temperature and low-temperature segments of the solubility curve are commonly called the wet solidus and the vapor-saturation curve, respectively. The ability to predict regions of immiscibility is of obvious geochemical interest, as immiscible phases have different chemistries and physical properties (viscosity and density). Hence  $L+V$  immiscibility can lead to a spatial fractionation of the dissolved mass (for example, Hedenquist and Lowenstern, 1994; Heinrich and others, 1999; Sun and others, 2003).

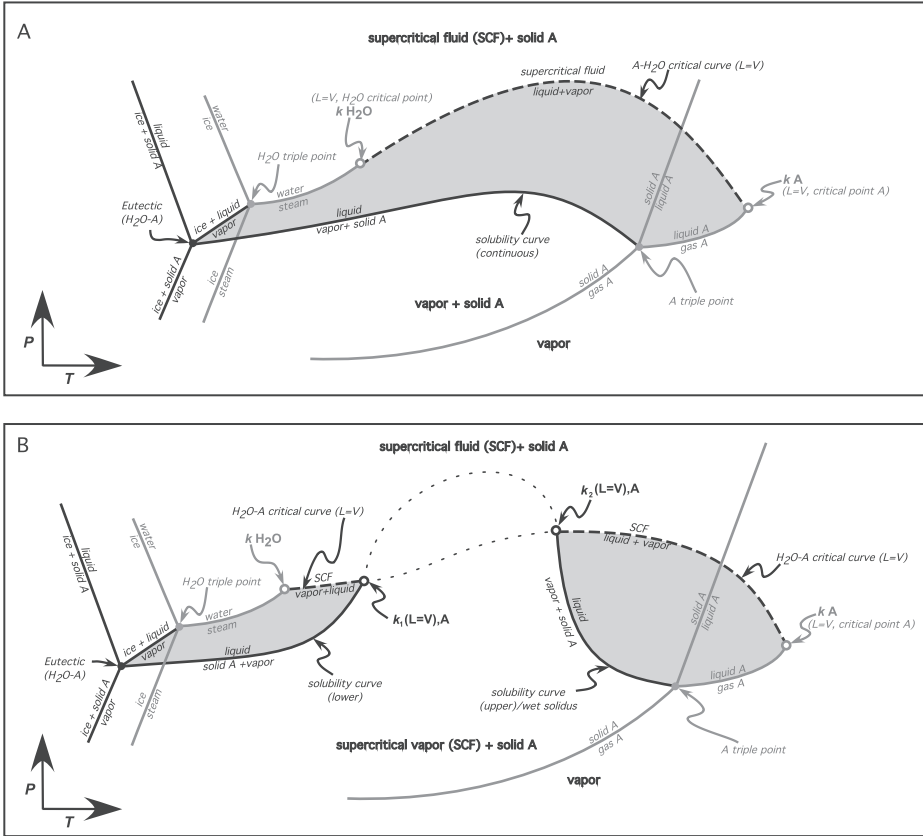


Fig. 1. Schematic  $PT$  projections illustrating two contrasting binary eutectic  $A-H_2O$  topologies where, (A) solubility curve ( $S+V=L$ ; solid) and critical curve ( $L=V$ ; dashed) do not intersect, an example is  $NaCl-H_2O$ ; and, (B) solubility curve (solid) and critical curve (dashed) intersect, examples include  $SiO_2-H_2O$  and  $NaAlSi_3O_8-H_2O$ . Gray fields indicate where a liquid+vapor miscibility gap is stable. Gray curves = end-member equilibria; black curves = binary system equilibria. Curves (dotted) between critical endpoints  $k_1(L=V)A$  and  $k_2(L=V)A$  are imaginary/metastable (after Morey and Niggli, 1913).

Two-dimensional, isobaric  $TX$  sections reveal the manner in which phase stability and composition are related to the phase-equilibrium boundaries projected in  $PT$  (fig. 2).

VAPOR, MELT AND SUPERCRITICAL FLUID COMPOSITIONS ON  $PT$  PROJECTIONS

*General Construction and Discussion of Some Important Aspects*

To overcome the shortcomings of schematic diagrams, we present for the first time  $PT$  projections in which liquid, vapor and supercritical fluid compositions are completely shown. Changes in fluid and liquid compositions on a  $PT$  projection can be expressed explicitly by using various continuous, composition iso-lines (isopleths) for each phase. Here we use this method to clarify the relations indicated on figures 1 and 2. We focus our discussion on the high-temperature melting relations involving melt and vapor and supercriticality.

Examination of figure 2 shows that there are four distinct saturation-surfaces involving liquid and vapor in the binary  $A-H_2O$  that need to be represented: 1) the subsolidus fluid ( $V$ ) composition at saturation with mineral- $A$ ; 2) the supersolidus

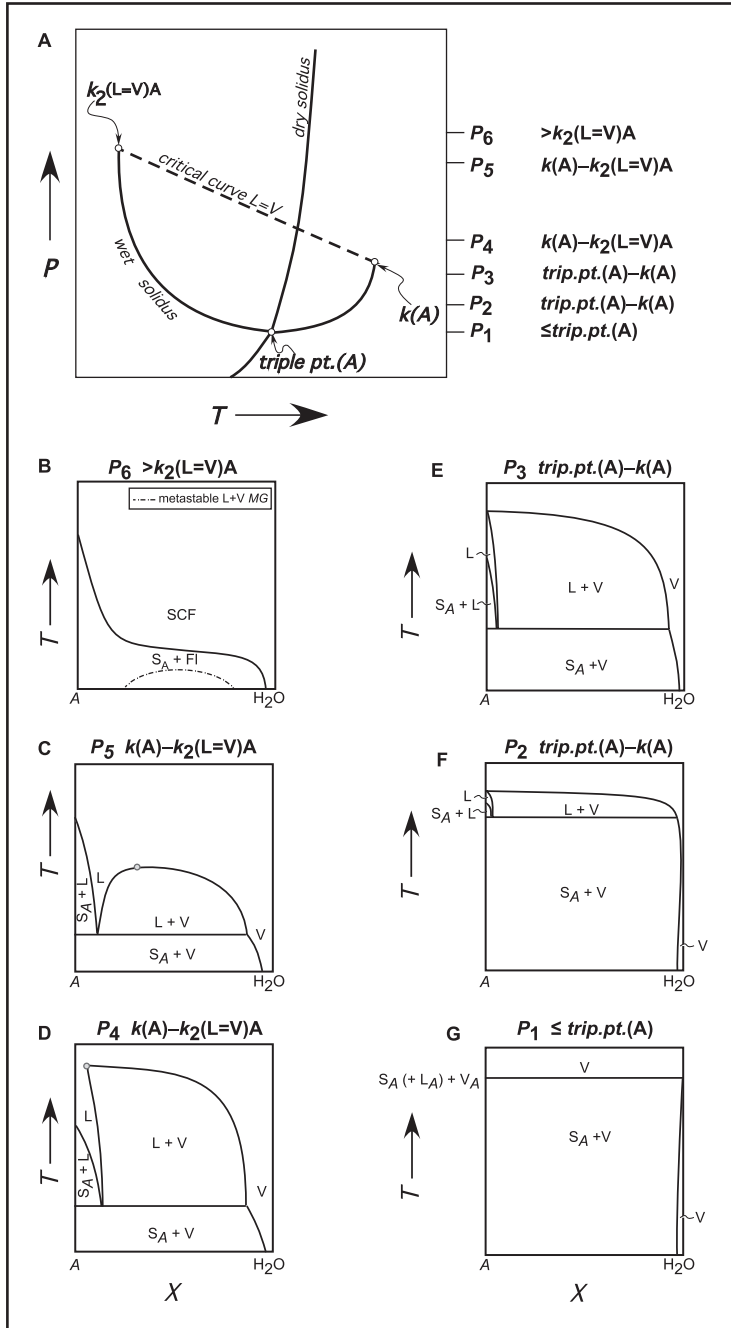


Fig. 2. Schematic showing relations between  $PT$  projection (A) and isobaric  $TX$  sections (B–G) for an A-H<sub>2</sub>O system where the solubility curve and critical curve intersect, analogous to a silicate-H<sub>2</sub>O system ('type-2', fig. 1B). The L+V miscibility gap ('MG', dashed curve, B) is shown as metastable below the solubility curve at pressures higher than the critical endpoint of the wet solidus, implying that the metastable projection of the critical curve also has a negative  $dP/dT$  slope.

liquid (melt) composition at saturation with mineral-A; 3) the supersolidus vapor composition in equilibrium with the coexisting melt; and 4) the supersolidus liquid composition at saturation with vapor. Some of these surfaces (represented by isopleths) are continuous, but inflected, across phase-equilibrium boundaries. For example, at  $P$  below the wet solidus endpoint, vapor is stable on both the high- and low-temperature sides of the wet solidus. While vapor isopleths are inflected at the wet solidus they are continuous to higher temperature. At the wet solidus, the other phase with which vapor coexists changes from crystalline-A at lower  $T$  to hydrous liquid (L) at higher temperature (fig. 2C). A two-phase L+V field terminates along a critical curve (fig. 2B). At the critical curve coexisting L and V isopleths of the same composition intersect, hence  $L=V$ . L and V are immiscible at  $P$  and  $T$  below the critical endpoint on the wet solidus, here denoted as  $k_2(L=V)A$ . Mineral-A is a stable phase at the critical endpoint on the wet solidus. At higher  $P$  and  $T$  than the critical endpoint, the wet solidus has vanished and crystalline-A-saturated vapor and liquid fields are continuous.

Figure 3 schematically illustrates the manner in which liquid and vapor compositional isopleths relate to various phase equilibrium boundaries, especially at the wet solidus,  $L=V$  critical curve and their terminations. Other notable points include: 1) the isopleth location within the liquid+vapor field above the wet solidus is arbitrary. That is the compositions derived from the figure at a fixed  $P$  and  $T$  are not quantitatively constrained, they are schematic; 2) the relative isopleth positions and slope are constrained because the isopleth geometry determines the shape of the solvus in this field. The isopleth geometry corresponds to the general behavior shown in figure 2; and, 3) the broad framework of mineral-A solubility isopleths in the supercritical field is based on data for  $\text{SiO}_2\text{-H}_2\text{O}$  (for example, Manning, 1994). The solubility relations near the lower critical endpoint ( $k_1$ ) and the implications of various modifications of figure 3 are considered in more detail below.

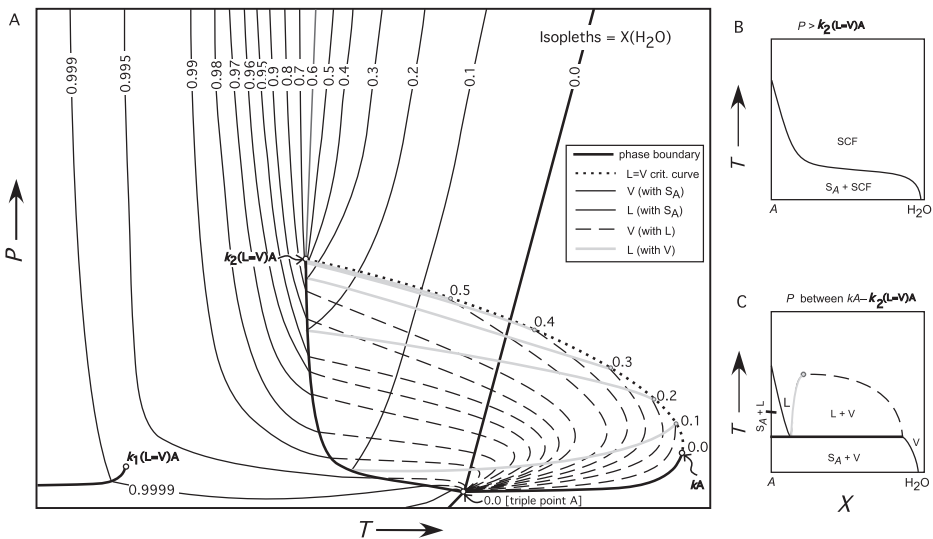


Fig. 3. (A) Composition projected as isopleths (thin curves) onto the  $PT$  surface for a 'type-2' system, mineral  $A\text{-H}_2\text{O}$ , in which the critical curve intersects the solubility curve (figs. 1B and 2). Equilibrium phase boundaries (bold curves), V-saturated L composition (thin dashed) intersects the coexisting V composition (thin unbroken curves) at the  $L=V$  critical curve (bold dashed line). A single upper critical isopleth, here  $X(\text{H}_2\text{O}) = 0.6$ , extends from  $k_2(L=V)A$ , a different lower critical isopleth extends from  $k_1(L=V)A$  occurring between  $0.999\text{-}0.9999\text{ }X(\text{H}_2\text{O})$  (not shown). (B) and (C) are isobaric  $TX$  sections through the  $PT$  phase relations.

Figure 3 shows that the wet solidus terminates into a divariant field at the intersection with a critical ( $L=V$ ) curve, at which vapor and liquid converge in composition. At the critical endpoint on the wet solidus, mineral- $A$  coexists with a supercritical fluid of fixed composition. In the divariant field, mineral- $A$  may coexist with a supercritical-fluid, the fluid composition depends on both  $T$  and  $P$ . The critical composition at the wet solidus endpoint extends as a line in  $PT$ . The composition of supercritical fluid coexisting with mineral- $A$  may vary continuously, but will be more liquid-like or vapor-like depending on the  $P$  and  $T$ , relative to the  $PT$  location of the critical composition. At  $T$  above the triple point of  $A$ , the liquid+vapor curve for  $A$  is also the zero- $\text{H}_2\text{O}$  isopleth for liquid+vapor and it terminates at  $kA$ . All other  $A\text{-H}_2\text{O}$  liquid and vapor isopleths of the same composition are separated in the liquid+vapor field, except where they intersect at the critical curve. The range of fluid compositions occurring along the  $L=V$  critical curve fall between the critical composition at  $k_2(L=V)A$  and pure  $A$  at  $kA$  (and *trip.pt.A*, fig. 3).

Ideal simple binary system topologies have certain limitations. An example is the requirement that all hydrous vapor originate at the triple point for a single anhydrous end-member ( $A$ ), whereas more complex systems will contain more than one end-member anhydrous triple point. For more complex solutions, it is not usually obvious which parts of the equilibria in a  $PT$  projection will be seen by a particular bulk composition, given that the compositions of the phases, here  $L$  and  $V$ , vary along the univariant lines.

Paillat and others (1992) presented a three-dimensional  $PTX$  model of solid-liquid-vapor phase relations for  $\text{NaAlSi}_3\text{O}_8(\text{albite})\text{-H}_2\text{O}$ . The topology they describe is analogous to the  $A\text{-H}_2\text{O}$  system shown in figure 3 but does not extend up to  $P$  of the wet solidus critical endpoint,  $k_2(L=V)\text{Alb}$  (their diagram may be of assistance in visualizing our contoured version). In the following section, we discuss the significance of the  $dP/dT$  geometry of liquid and vapor compositional isopleths, critical curves and relative  $P, T$  positions of points  $k_2(L=V)A$ ,  $kA$ , and *trip.pt.A*.

#### *Critical Points and $L=V$ Curve Geometries, Isopleth Slopes and Their Relation to Mineral Solubility and the Fluid-Melt Solvus*

Here we focus on  $L+V$  immiscibility and the geometry of the critical curve (fig. 4). The  $dP/dT$  slopes of fluid and melt isopleths directly reflect the  $PTX$  behavior of the  $L+V$  solvus. For clarity, these lines are not shown on figure 4. The key aspect of figure 4 is the illustration of how critical curve geometries relate to immiscibility and govern solubility behavior. Different topological configurations arise from contrasting  $dP/dT$  and  $dT/dX$  (or  $dP/dX$ ) behavior of hydrous liquid and aqueous vapor compositions. Curvature and fanning of coexisting immiscible  $L$  and  $V$  isopleths in  $PT$  relates directly to the solvus geometry. Isopleths have additional chemical meaning, as they indicate the  $P$  and  $T$  dependence of solubility (in  $L$  or  $V$ ), which reflects the underlying dissolution mechanisms.

From a geometric perspective, it is principally the  $PT$  location of the invariant and critical points in  $A\text{-H}_2\text{O}$  that determines the average  $dP/dT$  slope of the equilibrium phase boundaries, and hence also that of the various isopleths. In figure 4A, the critical endpoint on the solidus  $k_2(L=V)A$  occurs at a lower pressure than  $kA$ . As a result, the critical curve requires an overall positive  $dP/dT$ . The  $L+V$  miscibility gap in this system is encountered at pressures above the end of the wet solidus for appropriate compositions, but not in the presence of a mineral.

Figure 4B shows a critical ( $L=V$ ) curve that develops a  $P$  maximum above the critical endpoint of the wet solidus. The accompanying isobaric  $TX$  section shows how the  $L+V$  solvus is isolated at higher  $T$  than the solubility surface, rather than at lower  $T$ . The isobar intersects the critical curve at two temperatures, producing an island of  $L+V$  immiscibility above the second critical endpoint in the absence of a wet solidus.

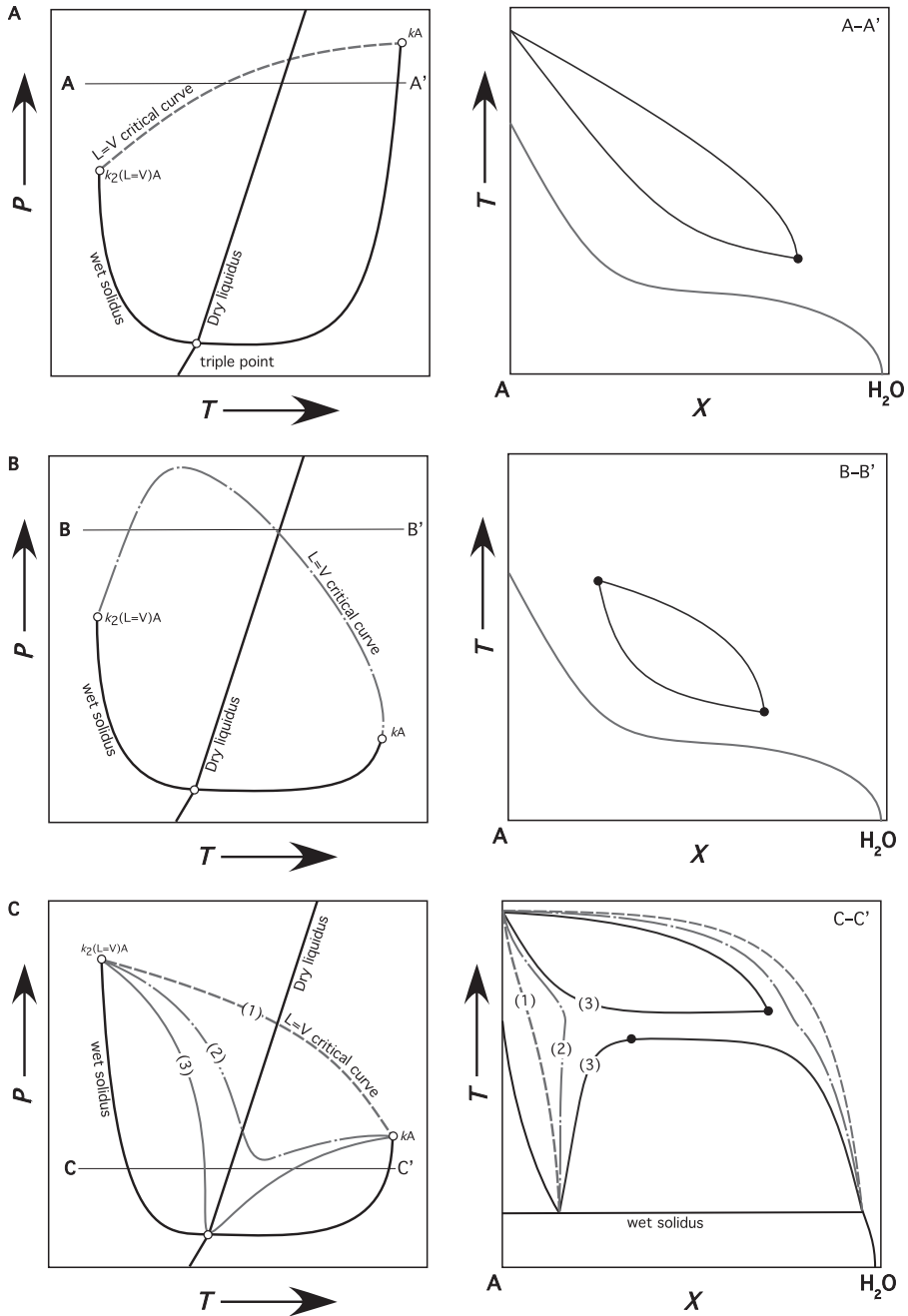


Fig. 4. Illustration of relations between critical curve geometry and fluid-melt solvus behavior. (A) Positive  $dP/dT$  critical curve where  $P_{k_2(L=V)A} < P_{kA}$ . (B) Critical curve with  $P$  maximum above  $k_2(L=V)A$  and  $kA$ . (C) Where critical points  $P_{k_2(L=V)A} > P_{kA}$  and comparing critical curves: (1) having entirely negative  $dP/dT$ ; (2) with  $P$  minimum between  $k_2(L=V)A$  and  $kA$ ; and (3) intersecting with the triple point for pure  $A$  from higher and lower  $T$ . Open circles represent critical endpoints; filled circles indicate where the  $TX$  sections cut the critical curve.

Figure 4C, shows three different critical L=V curve arrangements and accompanying isobaric *TX* sections (c-c') showing the L+V solvi which produce these curves. An important observation is that reversals isopleth  $dP/dT$  correspond to a  $dT/dX$  slope reversal in the L+V solvus limb(s). These inflections suggest that the L+V miscibility gap is characterized by two solvi components. Isopleth slope reversals, where no phase transitions are involved in the coexisting minerals, could be associated with chemical coordination changes in either the V or L phases. The case where the 'low' and 'high' L+V solvi are completely separated is shown by curve '3' (fig. 4C). Here, solubility isopleths do not reverse  $dP/dT$ , but maintain positive or negative slope within each L+V field. Relations associated with critical L+V curve '3' are discussed further below.

#### *Clapeyron Slope of Critical L=V Curves*

Unfortunately, the physical properties of silicate-bearing aqueous fluids are poorly known (for example, density). Nonetheless, the fundamental systematics for volumetric properties of supercritical and immiscible fluid mixtures are known from simple thermodynamic relations (for example, Rowlinson, 1983; Levelt Sengers, 2000). The latter allow us to make some simple statements regarding the relative physical properties of miscible and immiscible fluids.

The geometry of critical phase boundaries contains information about the physical properties of the phases involved. For example, at constant temperature, if a mixture of L+V becomes completely miscible with increasing pressure, it is because the homogeneous phase has a higher density than the coexisting immiscible L+V. The slope of an equilibrium boundary, such as the L=V critical curve, is defined by the Clapeyron relation:  $dP/dT = \Delta S / \Delta V$ . If the boundary is a straight line, then the values of  $\Delta S$  (entropy of reaction) and  $\Delta V$  (volume of reaction) are not dependent upon *T* and *P*. A negative  $dP/dT$  slope implies that  $\Delta S$  and  $\Delta V$  have opposite signs, while for positive  $dP/dT$ ,  $\Delta S$  and  $\Delta V$  have the same sign. Thus, the slope (and curvature) of critical curves has a simple thermodynamic significance and provides information on the nature of the relative compressibilities of L+V and supercritical fluids.

So far, L=V critical curves reported in hydrous silicate systems (NaAlSi<sub>3</sub>O<sub>8</sub>-H<sub>2</sub>O, Shen and Keppler, 1997; NaAlSiO<sub>4</sub>-H<sub>2</sub>O, NaAlSi<sub>2</sub>O<sub>6</sub>-H<sub>2</sub>O, 'haplogranite'-H<sub>2</sub>O, Bureau and Keppler, 1999; NaAlSi<sub>3</sub>O<sub>8</sub>-H<sub>2</sub>O±Na<sub>2</sub>O±B<sub>2</sub>O<sub>3</sub>±F<sub>2</sub>O<sub>-1</sub>, Sowerby and Keppler, 2002) show negative  $dP/dT$  slopes and are nearly linear, within the experimental uncertainty. In these cases the supercritical region lies on the high-pressure side of the critical curve. Accordingly, we expect high-pressure critical fluids to be more compressible than equivalent immiscible L+V mixtures. A negative  $dP/dT$  also implies that cooling of a supercritical solution results in L+V unmixing. However, note that there is evidence that some silicate-H<sub>2</sub>O critical curves possess positive  $dP/dT$ ; for example, parts of the system Na<sub>2</sub>SiO<sub>3</sub>-SiO<sub>2</sub>-H<sub>2</sub>O (Urusova and Valyashko, 2001). Critical (L=V) curves with positive  $dP/dT$  allow immiscible L+V mixtures to evolve into supercritical solutions on cooling.

Additionally, it is possible that some L=V critical lines may be curved to the extent that *T* minima (or maxima) occur. The theoretical analysis by Boettcher and Wyllie (1969a) of wet melting relations and critical curves in a ternary MO-SiO<sub>2</sub>-H<sub>2</sub>O system suggests that the occurrence of *P*, *T* minima (and maxima) on critical curves is practically unavoidable in non-binary, higher-order systems. Significantly, a *T* minimum (or maximum) on a critical curve implies  $\Delta V=0$  and requires a density inversion amongst the phases at the critical curve. A density inversion need not accompany a significant change in the coexisting fluid compositions. Thus, with increasing pressure the hydrous silicate liquid would become relatively less dense and eventually more buoyant than the H<sub>2</sub>O-rich fluid at high *P*. An example of L-V density inversion occurs in the binary CO<sub>2</sub>-H<sub>2</sub>O system close to 0.23 GPa (Tödheide and Franck, 1963; Takenouchi and Kennedy, 1964).

GEOMETRICALLY CONSISTENT *PTX* RELATIONS FOR AN INCOMPLETELY DETERMINED SYSTEM:  
SiO<sub>2</sub>–H<sub>2</sub>O AS AN EXAMPLE

Mineral solubility and wet melting relations in the SiO<sub>2</sub>–H<sub>2</sub>O system have been the subject of numerous investigations (table 2). Figure 5 shows a representative compilation of experimental knowledge of SiO<sub>2</sub>–H<sub>2</sub>O. Respectively, the two critical endpoints,  $k_1(L=V)Qtz$  and  $k_2(L=V)Qtz$ , are located near  $kH_2O$  (374 °C, 22.1 MPa; Haar, and others, 1984) and at 1100 °C, 0.97 GPa,  $\sim 0.47 X(SiO_2)$  (Kennedy and others, 1962). Guissani and Guillot (1996) calculated that the critical point for pure silica,  $kSiO_2$ , occurs at 11,700 °C,  $\sim 0.2$  GPa and critical density = 0.58 g cm<sup>-3</sup>. In the binary system SiO<sub>2</sub>–H<sub>2</sub>O, the upper *PT* region in which L+V immiscibility occurs is less well constrained. The location of the critical curve (L=V) (dashed curve, fig. 5B) is not presently known – except in the vicinity of the quartz wet solidus ( $Qtz+V=L$ ) where it terminates by intersection with the L=V critical curve (Kennedy, and others, 1962). At higher temperature, the binary critical (L=V) curve intersects the critical point ( $L_{SiO_2}=V_{SiO_2}$ ) of pure silica  $kSiO_2$  (fig. 3). The location of critical endpoints  $k_2(L=V)Qtz$  and  $kSiO_2$  indicates that the L=V critical curve has an average negative  $dP/dT$  slope (approximately,  $-0.073$  MPa K<sup>-1</sup>, for linear  $dP/dT$ ). The available data for SiO<sub>2</sub>–H<sub>2</sub>O can thus be described by a type-2 topology as described above (see fig. 1B and fig. 3).

Figure 5B schematically shows the phase relations for SiO<sub>2</sub>–H<sub>2</sub>O near the upper three-phase ( $Qtz+V=L$ ) curve, along with *PT* stability of the different SiO<sub>2</sub> polymorphs. Figure 5C shows the composition of V-saturated liquid at different temperatures for a series of pressures, expressed as mole fraction water  $X(H_2O)$ . Below 0.4 GPa there is little or no temperature dependence of H<sub>2</sub>O solubility in the liquid. Above 0.5 GPa, as  $k_2(L=V)Qtz$  is approached, H<sub>2</sub>O solubility strongly increases with increasing temperature. L and V compositions converge to one critical composition (or supercritical fluid, SCF) at the upper or second critical endpoint on the wet solidus. Figure 5E shows an isobaric *TX* section through figure 5A at 0.4 GPa. Figures 5D and 5F show measured SiO<sub>2</sub> solubility in H<sub>2</sub>O at 1.5 GPa as a function of temperature, expressed in weight percent (H<sub>2</sub>O) and mole fraction  $X(H_2O)$ , respectively. The L+V miscibility gap is gone at this pressure,  $P > k_2(L=V)Qtz$  (solvus is shown metastable at a lower temperature than the solubility curve). There is a continuous transition from dry SiO<sub>2</sub> liquid ( $L_{SiO_2}$ ) to almost pure H<sub>2</sub>O liquid, without passing through a wet melting reaction. L and V are completely miscible and a single fluid phase stably coexists with solid-SiO<sub>2</sub> at these conditions; the fluid is supercritical.

Observations by Nakamura (1974) that show quartz solubility is continuous with increasing temperature (up to the melting point) appear to leave little doubt that in SiO<sub>2</sub>–H<sub>2</sub>O the quartz wet solidus is no longer defined at 1.5 GPa. Moreover, it is worth recognizing that the different quartz solubility data sets are in good general agreement and support the melting relations and critical endpoint on the wet solidus observed by Kennedy and others (1962). Similar agreement is observed between Anderson and Burnham (1965), Kennedy and others (1962) and Holtz and others (2000) at pressures where the wet solidus is still present (figs. 5C and 5E), and also on the *T* dependence of quartz solubility in H<sub>2</sub>O at 1.5 GPa (above the end of the wet solidus) determined by Nakamura (1974) and Manning (1994; figs. 5D and 5F).

*Insights from Water Solubility and Supercriticality in the System NaAlSi<sub>3</sub>O<sub>8</sub>(albite)–H<sub>2</sub>O*

Like SiO<sub>2</sub>–H<sub>2</sub>O, NaAlSi<sub>3</sub>O<sub>8</sub>–H<sub>2</sub>O appears to be a type-2 system topology albeit with additional complexities, for example with increasing pressure albite breaks down to jadeite + quartz (Holland, 1980; Liu and Bohlen, 1995).

Figure 6A indicates experimentally investigated *P, T* conditions in the albite–water (NaAlSi<sub>3</sub>O<sub>8</sub>–H<sub>2</sub>O) system (a representative selection from table 2). Figure 6B shows a schematic *PT* projection of albite–H<sub>2</sub>O phase relations.

TABLE 2  
*Experimental investigations in SiO<sub>2</sub> (quartz)—H<sub>2</sub>O and NaAlSi<sub>3</sub>O<sub>8</sub> (albite)—H<sub>2</sub>O systems*

System	Mineral solubility along the H <sub>2</sub> O liquid + vapor coexistence curve	Mineral solubility in supercritical H <sub>2</sub> O (V)	Position of the wet solidus and phase compositions	Critical L=V miscibility phenomena	Dry melting curve	Solubility of H <sub>2</sub> O in vapor-saturated melt	Position of liquid + gas coexistence curve and critical point of pure dry system
SiO <sub>2</sub> -H <sub>2</sub> O	Kennedy (1950)	Kennedy (1944, 1950)	Tuttle and England (1955)	Kennedy and others (1962)	Jackson (1976)	Kennedy and others (1962)	Guissami and Guilfoit (1996)
	Fournier (1960)	Mory and Hesselgesser (1951)	Kennedy and others (1962)	Stewart (1967)	Kanzaki (1980)	Holtz and others (2000)	
	Kitahara (1960)	Wasserburg (1958)	Stewart (1967)	Nakamura (1974)	Hudson and others (2002)		
	van Lier and others (1960)	Wood (1958)	Boettcher (1984)				
	Morey and others (1962)	Weill and Fyfe (1964)	Luth and Boettcher (1986)				
	Stever (1962)	Anderson and Burnham (1965)					
	Crerar and Anderson (1971)	Sommerfeld (1967)					
	Mackenzie and Gees (1971)	Semenova and Tsiklis (1970)					
	Volosov and others (1972)	Crerar and Anderson (1971)					
	Hemley and others (1980)	Nakamura (1974)					
	Fleming and Crerar (1982)	Fournier and Potter (1982)					
	Fournier and Potter (1982)	Ragnarsdóttir and Walther (1983)					
	Rimstidt (1997)	Walther and Orville (1983)					
		Manning (1994)					
		Manning and Boettcher (1994)					
	Wang and others (2004)						
NaAlSi <sub>3</sub> O <sub>8</sub> (albite)-H <sub>2</sub> O		Currie (1968)*	Yoder (1958)	Boettcher and Wyllie (1969a)	Scharrer and Bowen (1956)	Goranson (1938)	Not determined
		Davis (1972)*	Bohlen and others (1982)	Paillet and others (1992)	Birch and LeComie (1960)	Burnham and Jahns (1962)	
		Woodland and Walther (1987)*	Goldsmith and Jenkins (1985)	Shen and Keppler (1997)	Boyd and England (1963)	Orieva (1962)	
		Vidale (1983)*	Luth and Boettcher (1986)		Boettcher and others (1982)	Khitrov and others (1963)	
		Stalder and others (2000)*	Stalder and others (2000)		Boettcher and Carroll (1996)	Luth and others (1964)	
		Shmulovich and others (2001)				Kadik and Lebedev (1968)	
		Hauzenberger and others (2001)*				Boettcher and Wyllie (1969a)	
		Pak and others (2003)*				Morse (1970)	
		Shmulovich and others (2006)				Burnham and Davis (1971 & 1974; PVT studies)	
						Eggler and Kadik (1979)	
						Voight and others (1981)	
						Day and Fenn (1982)	
						Hamilton and Oxtoby (1986)	
						Richet and others (1986)	
						Paillet and others (1992)	
					Behrens (1995)		

Notes: Studies of amorphous silica, SiO<sub>2</sub> polymorph stabilities and phase relations in the general Na<sub>2</sub>O—Al<sub>2</sub>O<sub>3</sub>—SiO<sub>2</sub>±H<sub>2</sub>O and related systems are not tabulated. \*Solid albite (NaAlSi<sub>3</sub>O<sub>8</sub>) dissolves incongruently/non-stoichiometrically in H<sub>2</sub>O.

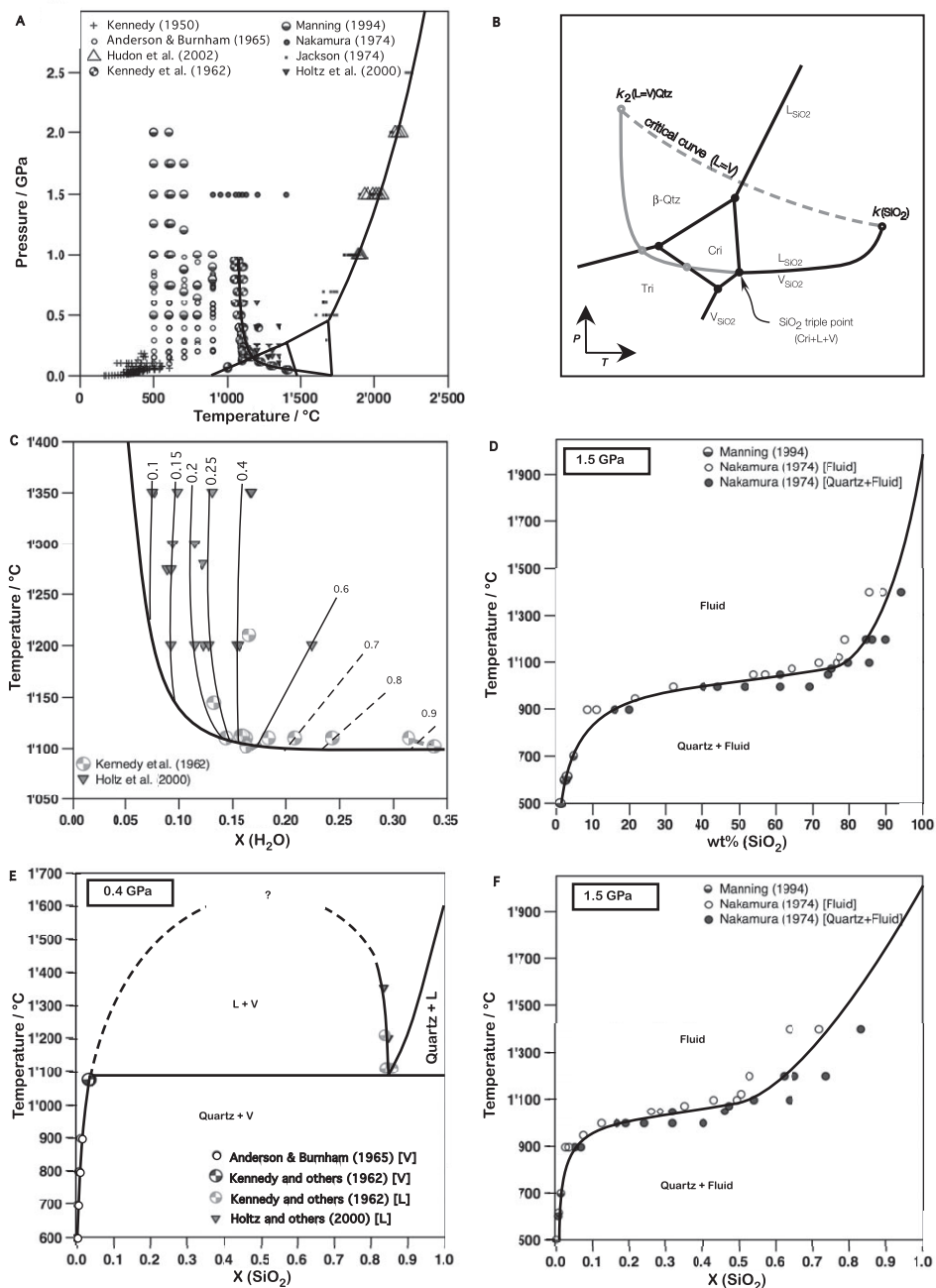


Fig. 5. The  $SiO_2$ – $H_2O$  system. (A) Experimental  $PT$  locations (a selection, table 2). (B)  $PT$  phase relations near the wet solidus.  $SiO_2$  polymorphs:  $Tri$  = tridymite;  $Cri$  = cristobalite;  $\beta\text{-Qtz}$  = beta-quartz;  $L$  = liquid;  $V$  = vapor. (C)  $H_2O$  solubility (as wt%  $H_2O$ ) in liquid silica ( $L$ ) as a function of  $T$  for various isobars (GPa at ends of steep solid curves). (D) 1.5 GPa quartz solubility/phase equilibria data plotted as weight percent. (E)  $TX$  section at 0.4 GPa. (F) Figure D replotted as mol fraction  $X(SiO_2)$ ;  $mw H_2O=18.02$ ,  $mw SiO_2=60.09$ .

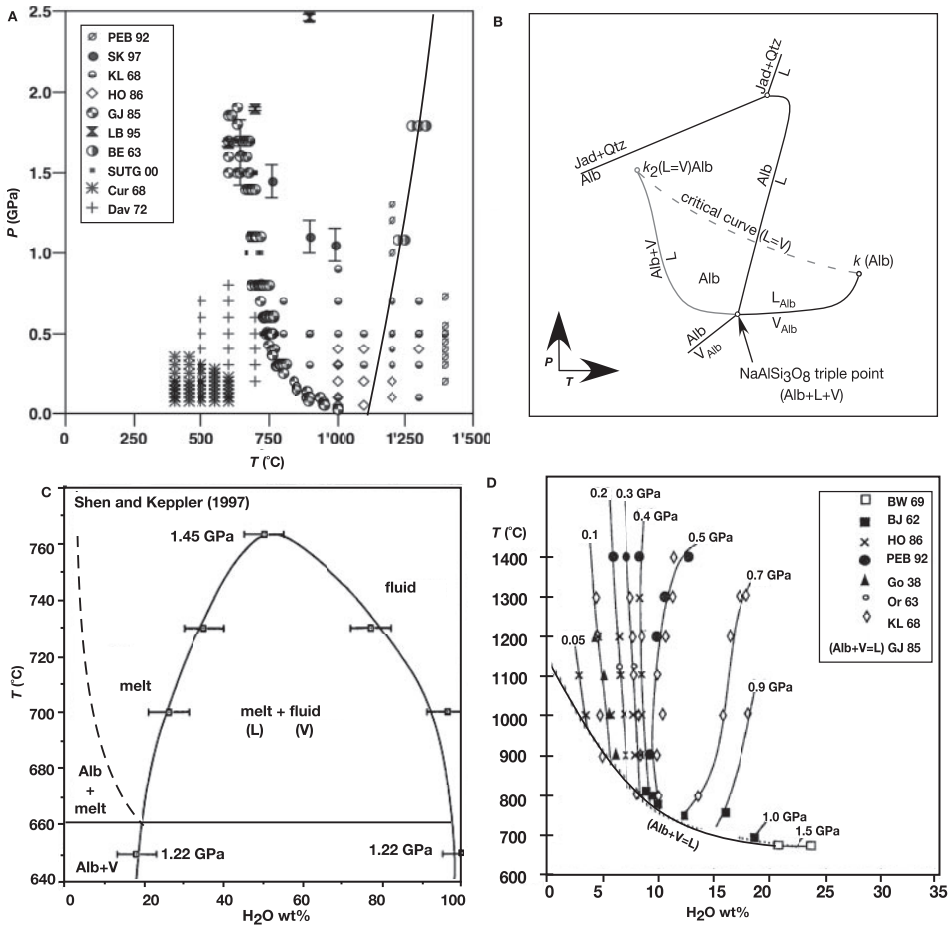


Fig. 6. NaAlSi<sub>3</sub>O<sub>8</sub>(albite)–H<sub>2</sub>O phase relations. (A) Experimental data  $P$ ,  $T$  locations (representative selection, table 1). Dry liquidus (solid line, Alb=L<sub>Alb</sub>) is shown for reference. (B) Inferred  $PT$  phase relations for NaAlSi<sub>3</sub>O<sub>8</sub>–H<sub>2</sub>O. (C) L+V solvus from Shen and Keppler (1997). Note the data are polybaric, L+V data at 1.22 GPa occur at a  $T$  below the wet solidus (660 °C) and are metastable. (D) H<sub>2</sub>O solubility (as weight percent water) in liquid albite (L) as a function of  $T$  for various isobars (GPa given at ends of steep solid curves) from 0.05 to 1.5 GPa (after Paillat and others, 1992). Data sources, BW: Boettcher and Wyllie (1969b); BJ: Burnham and Jahns (1962); HO: Hamilton and Oxtoby (1986); PEB: Paillat and others (1992, data at 0.35, 0.45 and 0.55 GPa are not plotted in D); Go: Goranson (1938); Or: Orlova (1963); KL: Kadik and Lebedev (1968); GJ 85: Goldsmith and Jenkins (1985); SK 97: Shen and Keppler (1997); LB 95: Liu and Bohlen (1995); BE 63: Boyd and England (1963); SUTG 00: Stalder and others (2000); Cur 68: Currie (1968); Dav 72: Davis (ms, 1972).

Figure 6D shows H<sub>2</sub>O solubility in albite-liquid (L) as a function of temperature for a series of pressures (Paillat and others, 1992). Up to 0.4 GPa, H<sub>2</sub>O solubility in L decreases with increasing  $T$  or is neutral, and all data agree well. Above 0.5 GPa, H<sub>2</sub>O solubility becomes increasingly prograde with increasing pressure; at 0.7 and 0.9 GPa only the highest values are plotted and these represent a minimum H<sub>2</sub>O concentration in L, since exsolution of the dissolved vapor upon quenching made accurate measurements on the glasses difficult (Paillat and others, 1992). The values reported by Paillat and others (1992) at and above 1.0 GPa were inferred by chemographic methods.

Shen and Keppler (1997) located the NaAlSi<sub>3</sub>O<sub>8</sub>–H<sub>2</sub>O critical curve (L=V) between 1.0 and 1.5 GPa (fig. 6A) and determined the geometry of the solvus (fig. 6C).

This curve has an overall negative  $dP/dT$  slope ( $\sim -0.55$  MPa  $K^{-1}$ , assuming linear  $dP/dT$ ). The intersection of this critical curve with the three-phase curve (Alb+V=L) occurs at 700 °C, 1.6 GPa (Stalder and others, 2000). These observations support the overall topology (type-2, fig. 1B) inferred by Paillat and others (1992).

Several aspects of the NaAlSi<sub>3</sub>O<sub>8</sub>-H<sub>2</sub>O system are currently poorly constrained. They include a paucity of information on subsolidus albite solubility in aqueous fluid. Experimentally, albite solubility is complicated by incongruent dissolution. Solubility studies include Currie (1968, reviewed by Fyfe and others, 1978), Anderson and Burnham (1983, a source of data from an unpublished thesis, Davis, ms, 1972), Shmulovich and others (2001), and Antignano and Manning (2003). The composition of vapors coexisting with hydrous albite liquids are also poorly known (although see Clark, 1966, p. 415–436; Boettcher and Wyllie, 1969b).

Although fewer data are available, similar vapor-saturated melt behavior is observed in the system SiO<sub>2</sub>-H<sub>2</sub>O (fig. 5C). One of the weaknesses in the SiO<sub>2</sub>-H<sub>2</sub>O data set is limited information on the L+V solvus above the wet solidus. However, a semi-quantitative *PTX* diagram for SiO<sub>2</sub>-H<sub>2</sub>O can be constructed if it is assumed that L and V isopleths have the same general configuration in this system as in the system NaAlSi<sub>3</sub>O<sub>8</sub>-H<sub>2</sub>O.

#### *A Semi-Quantitative Model for the SiO<sub>2</sub>-H<sub>2</sub>O System*

Figure 7 shows the quartz-, melt-, and vapor-saturation isopleth framework for the SiO<sub>2</sub>-H<sub>2</sub>O system. Figure 7B shows quartz solubility near  $k_1(L=V)Qtz$ . Liquid and vapor compositions coexisting with quartz are given by mole fraction H<sub>2</sub>O along the isoplethal contours. The experimental data of Kennedy and others (1962) for L and V compositions on the quartz-wet solidus and the quartz solubility data of Anderson and Burnham (1965), Nakamura (1974), and Manning (1994) at 1.5 GPa provide the constraints on the isopleth geometry at  $P$  and  $T$  above the termination of the wet solidus at  $k_2(L=V)Qtz$ . The isopleths for  $X(H_2O)^3 = 0.97$ , at  $T < 900$  °C were calculated using the quartz solubility equation of Manning (1994). Elsewhere, the isopleths are fit by hand to the data indicated on figure 5A. The quartz solubility isopleths near the lower S+L+V curve segment (up to 500 °C, 0.1 GPa) are given by mole fraction SiO<sub>2</sub>,  $X(SiO_2)$ , in figure 7B and are fit by hand to the data of Kennedy (1950). No quartz solubility data appear to be available for vapor compositions on the 'lower' S+L+V curve or in the 'gaseous' supercritical region.

The  $T$ -dependence of H<sub>2</sub>O solubility in vapor-saturated liquid changes as a function of  $P$  (fig. 5C). On a contoured *PT* projection (as in fig. 7), this corresponds to a change in the slope of the respective isopleths from  $dP/dT$  near positive or neutral to negative with increasing pressure. This behavior is also present in albite-H<sub>2</sub>O (fig. 6D).

SiO<sub>2</sub>-H<sub>2</sub>O may not be directly relevant to most natural rocks but it does serve to illustrate that topological approaches can be useful for understanding S-L-V phase equilibria that may involve critical behavior.

#### DISCUSSION

##### *Isopleth $dP/dT$ Slopes, L+V Solvi and Invariant Points*

In a pioneering study, Burnham and Davis (1974) used thermodynamic data derived from *PVT* measurements to calculate two divariant equilibria, H<sub>2</sub>O solubility in albite liquid at V saturation and the melt composition in equilibrium with albite over a wide range of *PT* conditions, and also the univariant wet solidus equilibrium (Alb+V=L). They predicted that melt isopleths at vapor-saturation would have increasingly positive  $dP/dT$  slope with increasing  $P$  (see their fig. 18). Such behavior is inconsistent with the L-V solvus found by Shen and Keppler (1997; fig. 6C) and inferred by Paillat and others (1992) which require coexisting L and V isopleths to both have negative  $dP/dT$  slope as the L=V curve is approached isobarically with

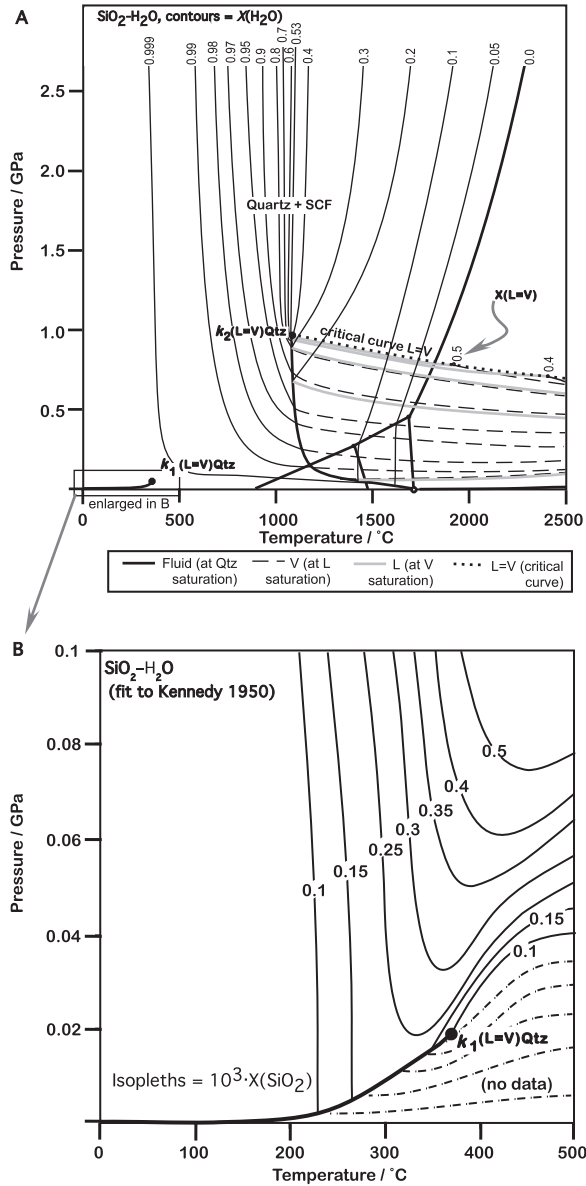


Fig. 7. (A) Semi-quantitative *PTX* projection of solubility and phase relations in the SiO<sub>2</sub>-H<sub>2</sub>O system consistent with available experimental observations (fig. 5) and assuming the L+V solvus behaves similarly to that observed for NaAlSi<sub>3</sub>O<sub>8</sub>-H<sub>2</sub>O. The figure is truncated at 2500 °C for clarity as  $kSiO_2$  lies at 11,700 °C, ~ 0.2 GPa. The critical isopleth extending from  $k_2(L=V)Qtz$  is X(H<sub>2</sub>O) = 0.53. The high-temperature part is expected to resemble that shown in fig. 3. (B) Shows quartz solubility isopleths near the lower critical endpoint. At this scale the lower Qtz+V=L curve (due to low solubility) is not distinguished from the L+V coexistence curve for pure H<sub>2</sub>O.

increasing *T*. Although their general method was sound, Burnham and Davis (1974) did not correctly predict the L+V solvus behavior with increasing *P*. This highlights the importance of having adequate experimental data to calibrate thermodynamic models, or for our purposes identifying the correct topology.

Geologically, the location of the silicate liquid+vapor coexistence curve and triple point may be of significance for the understanding of condensation of planetary materials from primitive solar nebula (for example, Mysen and Kushiro, 1988). These features are, however, poorly known owing to the extreme conditions where they are likely to occur for refractory geological compounds. If the results of Guissani and Guillot (1996) provide some general guidance, they imply that  $kA$  occurs at a significantly lower pressure than  $k_2(L=V)A$  but also higher pressure than the triple point of pure A. This relative  $PT$  arrangement differs from previous speculations on the  $PT$  location of  $kA$  which place it at higher pressure than  $k_2(L=V)A$  (for example,  $NaAlSi_3O_8-H_2O$ , Wyllie and Tuttle, 1960;  $SiO_2-H_2O$ , Tuttle and Bowen, 1958; Krauskopf, 1979), or at equivalent (or lower) pressure than the triple point (for example,  $NaAlSi_3O_8-H_2O$ , Paillat and others, 1992, see their fig. 7). As noted above, this is significant because the positions of the anhydrous  $L=V$  critical point and  $k_2(L=V)A$  impose strong constraints on the critical curve, and hence also on the general structure of the fluid+melt solvus, as indicated in figure 4. As an interesting example, it is worth considering the isopleth geometry and critical curve geometry for a system in which  $H_2O$  solubility in vapor-saturated liquid increases with increasing  $T$  at all pressures. This situation implies that the solvus does not change its basic shape as a function of pressure, and hence that there is no  $dP/dT$  reversal in the  $H_2O$  solubility curves. Inspection of the topologies discussed indicates that such relations are possible if two distinct regions of  $L+V$  immiscibility are present above the wet solidus (fig. 4C).

#### *A Two L+V Solvus A-H<sub>2</sub>O Topology*

Figure 8 shows the shape of solubility surfaces and phase relations developed where the critical ( $L=V$ ) curve intersects the anhydrous triple point in a hypothetical system  $A-H_2O$ . An interesting aspect of this topology is that the high-pressure phase relations are identical to those shown in figure 3, whereas at lower pressure  $L+V$  immiscibility can occur in two distinct  $PT$  regions that are separated by a super-solvus or completely miscible region (fig. 8E). The geometry imposed by the invariant points and the intersecting lines requires that the isopleths for immiscible  $L+V$  compositions have a certain  $dP/dT$  slope in each of the separate fields of immiscibility. Thus, vapor- and liquid-isopleths, and the critical curve have negative  $dP/dT$  slopes at temperatures below the triple point, but at higher-temperature, all have positive  $dP/dT$  slopes. Despite the similarities at high pressure, systems like albite- $H_2O$  in which solubility isopleths show an inflection from negative to positive  $dP/dT$  are not part of this topological family because they do not have a temperature interval of complete miscibility between separate  $L+V$  solvi (for example, Paillat and others 1992). 'Two-solvi' systems of this type have not yet been described, but the example illustrates how limited solubility data could be used to discriminate between possible topologies and identify the location and geometry of phase equilibrium boundaries.

#### *Critical (L=V) Curve-Wet Solidi Intersections, Non-Intersections and 'Second' Critical Endpoints*

The formation of a critical endpoint only occurs where the wet solidus and the  $L=V$  critical curve intersect and have the same composition. It is not necessary that all critical ( $L=V$ ) lines intersect a wet solidus. For example, Boettcher and Wyllie (1969b) noted that wet nepheline melting is strongly incongruent. Hence,  $L$  and  $V$  compositions on the wet solidus do not lie on the nepheline- $H_2O$  join. This could explain why the nepheline- $H_2O$  critical ( $L=V$ ) curve (Bureau and Keppler, 1999) crosses the nepheline wet solidus (Boettcher and Wyllie, 1969b) in  $PT$  without generating a critical endpoint.

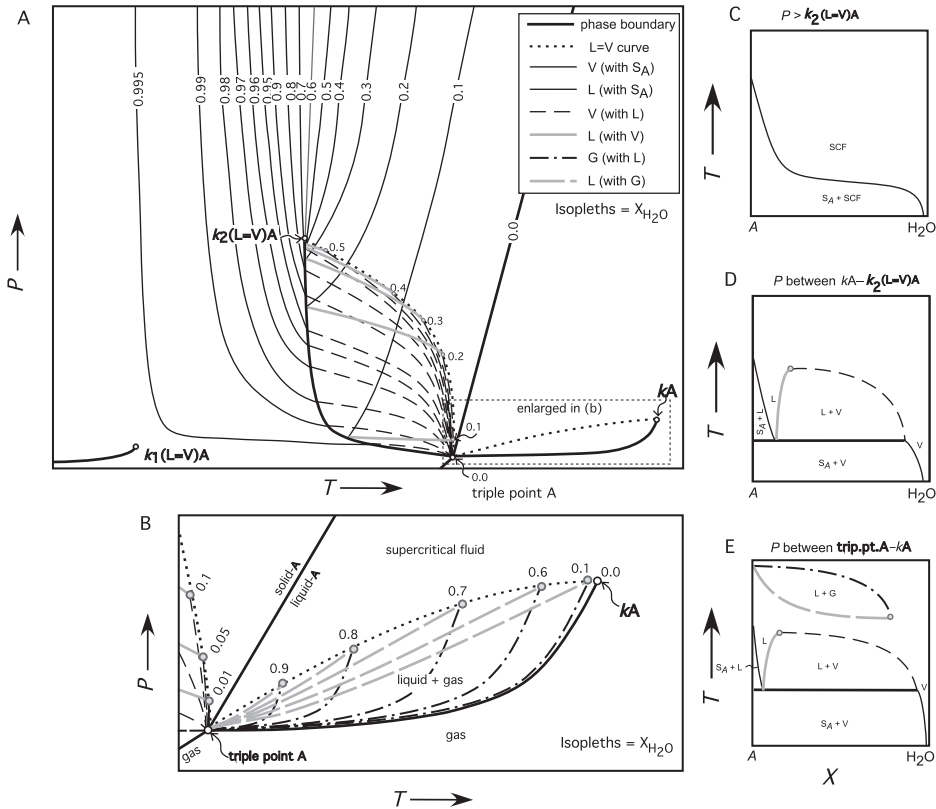


Fig. 8. (A) *PT* projection of binary system A-H<sub>2</sub>O with two L+V solvi. The two solvi result from the L=V critical curve intersecting the triple point between  $k_2(L=V)$  and  $kA$  from both higher and lower *T*. Isopleth values in *X*(H<sub>2</sub>O). (B) Enlargement of isopleth details for the L+G solvus above dry liquidus. (C–E) show iso-baric *TX* sections through the topology.

*Is a Critical (L=V) Endpoint on a Wet Solidus Significant?*

Recent attention has focused on the occurrence of critical endpoints terminating different wet solidi (for example, Stalder and others, 2000, 2001; Kessel and others, 2005a, 2005b) and the location of L=V critical curves in *PT* space (Shen and Keppler, 1997; Bureau and Keppler, 1999; Sowerby and Keppler, 2002). However, little attention has been given to the structure of the solubility surfaces that give rise to the phase relations being discussed.

Supercritical fluid (melt) compositions can vary continuously with changes in pressure and temperature in the supercritical region, via mineral precipitation and or dissolution. Supercritical phenomena allow fluids to attain hydrous melt-like compositions without passing through a classical melting reaction. Chemically it is not expected that supercritical melts should differ significantly from melts generated via a conventional melting relation at lower pressure on the wet solidus. This is true of the simple A-H<sub>2</sub>O systems (fig. 3, and SiO<sub>2</sub>-H<sub>2</sub>O, fig. 7) discussed, and is also supported by recent data on the composition of sub- and supercritical hydrous melts derived from a K-free eclogite (Kessel and others, 2005a, 2005b).

There is a single critical fluid isopleth, extending from the critical endpoint of a wet solidus. If SiO<sub>2</sub>-H<sub>2</sub>O is any indication, the *PT* trajectory of the critical isopleth

extends smoothly in the direction mimicking a metastable extension of the wet solidus. Supercriticality above a so-called second critical endpoint allows intermediate compositions (between aqueous fluid and silicate melt) to be realized. However, intermediate composition fluids probably only occur in a relatively narrow range of  $PT$  conditions, which may not be experienced (or only briefly so) in many rocks (Manning, 2004; Hermann and others, 2006).

#### *Fluid Composition, $H_2O$ Activity and Calculated Phase Diagrams*

Recognizing regions of low- and high  $a(H_2O)$  fluids is important, as calculated phase equilibria at high temperatures and pressures can be very sensitive to this parameter (for example, Powell and others, 2005; Yang and Powell, 2006). Other properties like viscosity and diffusivity are known to be strongly dependent on  $H_2O$  content and thus, pressure and temperature are also important. Figures 3, 7 and 8 show how the value of  $a(H_2O)$  can vary significantly in  $PT$  relative to the critical endpoint on a wet solidus when saturated with a solid. It may be justified to assume that  $X(H_2O)$  and  $a(H_2O)$  are proportional and fixed by the mineral solubility at any given  $PT$ . In contrast, in fields where two fluid phases are present the relationship between  $X(H_2O)$  and  $a(H_2O)$  is expected to be complex and non-linear, as is generally the case when a solvus exists.

An important observation from  $SiO_2$ – $H_2O$  is that the critical isopleth divides  $PT$  into a dilute, high- $a(H_2O)$  fluid region and at higher temperature, low- $a(H_2O)$  or solute-rich fluids or supercritical melts occur. The  $PT$  conditions where intermediate compositions near  $\sim 0.5 X(H_2O)$  occur, fall in a narrow band near the critical isopleth, and hence are comparatively rare in  $PT$  (Manning, 2004). On the other hand, the band of  $PT$  where intermediate fluids are stable is likely to vary its position depending on the bulk composition (or mineral+fluid assemblage) of interest, and hence may be more common (or impossible) in certain rocks on specific tectonic  $PT$  paths.

The relation between  $PT$  and  $a(H_2O)$  is further complicated by other factors that include the presence of soluble salts, like NaCl, that may contribute to enhanced mineral solubility and reduced  $a(H_2O)$  at a given  $PT$  (for example, Aranovich and Newton, 1996, 1997; Newton and Manning, 2002). Thus, although gaps remain, our understanding of fluids and  $a(H_2O)$  in high-pressure environments is evolving and should lead to improved calculated fluid-saturated phase diagrams, which may be turned to the task of interpreting natural hydrothermal and wet melting processes.

#### *Geological Applications: Explosive Volcanism, Porphyry Ore Genesis and Subduction Zone Processes*

Exsolution of volatiles from magmas is the primary mechanism by which volatile components are liberated from the Earth's interior to the atmosphere and oceans. Volatile saturation determines volcanic eruption styles (Burnham, 1985; Sparks and others, 1994) and is also a fundamental process in the formation of magmatic-hydrothermal ore deposits (Burnham 1979; Hedenquist and Lowenstern, 1994). Understanding  $PTX$  relations of hydrous magmas provides an insight into processes that drive magmas to exsolve (or resorb) volatile and crystalline components. Similarly, the ability to construct compositionally contoured  $PT$  surfaces allows fluid-mediated solute transport and melting in metamorphic environments (like dehydration and fluid flow in subduction zone environments), to be conceptually (in the absence of calibrated plots) understood more clearly (Hermann and others, 2006). Analysis of contoured  $PT$  plots illustrates how subtle differences in solubility surfaces (for example  $dP/dT$  slopes and phase relations) between systems are non-trivial as in natural environments they can result in strongly contrasting behavior along different  $PT$  paths.

## CONCLUSIONS

We have constructed a geometrically complete, semi-schematic, general  $PTX$  model of phase relations and solubility surfaces in silicate- $\text{H}_2\text{O}$  systems from a critical evaluation of theoretical topological relations and assimilation of published experimental data for the  $\text{SiO}_2\text{-H}_2\text{O}$  and  $\text{NaAlSi}_3\text{O}_8\text{-H}_2\text{O}$  systems. The model describes those aspects of basic phase relations for rock-water systems that are poorly known or even unconstrained, and can be used to predict phase stability and the shape of solubility surfaces for fluid phases in  $PT$  space with limited experimental data. Even if the absolute position of the phase composition isopleths on a  $PT$  projection is unknown, the isopleth slopes (positive or negative  $dP/dT$ ) on the  $PT$  projection and the compositional range and trends of the isopleths are determined for a given  $PTX$  topology. The relations between critical fluid compositions and the end of wet melting are made clear.

There is a simple and regular relation between  $PT$  conditions and the composition of a supercritical fluid where mineral-saturated. In the miscible or supercritical region, a continuum exists between  $\text{H}_2\text{O}$ -rich fluids and supercritical hydrous silicate melt compositions. However, distinct compositional ranges are confined to restricted and well-defined  $PT$  conditions. Fluid  $PTX$  domains are correlated with the position and  $dP/dT$  slope of the critical isopleth extending from the critical endpoint on the wet solidus of interest.

The simple approach and examples we describe are conceptually useful for relating solubility surfaces and phase boundary geometries, the design of future experimental studies and understanding large-scale behavior of  $\text{H}_2\text{O}$ -bearing fluid- and melt-interactions with minerals in high  $PT$  environments.

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