Observation of two elastic thresholds in Ge$_x$As$_y$Se$_{1-x-y}$ glasses

R. P. Wang,$^{1,a}$ A. Smith,$^1$ B. Luther-Davies,$^1$ H. Kokkonen,$^2$ and I. Jackson$^2$

$^1$Centre for Ultrahigh Bandwidth Devices for Optical Systems (CUDOS), Laser Physics Centre, Research School of Physics and Engineering, Australian National University, Canberra, ACT 0200, Australia

$^2$Research School of Earth Sciences, Australian National University, Canberra, ACT 0200, Australia

(Received 20 October 2008; accepted 8 January 2009; published online 12 March 2009)

We have prepared Ge$_x$As$_y$Se$_{1-x-y}$ glasses with mean coordination numbers (MCNs) from 2.2 to 2.86. $T_g$ was found to generally increase with increasing MCN while the glass density showed a maximum at MCN $\approx$ 2.45 and a minimum at MCN $\approx$ 2.65. The elastic moduli of the glasses were estimated from the shear and compressional wave velocities measured by ultrasonic pulse interferometry. For the first time we simultaneously observed two elastic transition thresholds, the first at MCN $\approx$ 2.45 and the second at MCN $\approx$ 2.65, which appear closely correlated with changes in the glass microstructure. The elastic moduli of two groups of samples with the same MCN = 2.4 and 2.64 but different compositions suggest that the chemical compositions also have an influence on the elastic properties. © 2009 American Institute of Physics. [DOI: 10.1063/1.3079806]

The purpose of measuring the elastic properties of Ge$_x$As$_y$Se$_{1-x-y}$ glasses is twofold. From a practical point of view, chalcogenide glasses are promising for both acousto-optic devices and acoustic delay lines due to their very high acousto-optic figure of merit, low acoustic attenuation, and low optical absorption in the near infrared region.$^1,2$ However, there has been no systematic investigation of the acousto-optic properties of the Ge–As–Se glass system, and their dependence on the chemical composition of the glass is unknown. On the other hand, many physical properties of chalcogenide glasses have been found to correlate with the mean coordination number (MCN, defined as a sum of the respective elemental concentrations times their covalent coordination number), which is a measure of the network connectivity. By mean field theory using a counting constraint algorithm, Phillips and Thorpe$^3$ first identified a floppy-to-rigid transition at MCN $\approx$ 2.4. By considering self-organization of a random network, Boolchand and co-workers$^4-6$ further found a rigid but stress-free intermediate phase (IP) from Raman scattering data and temperature-modulated differential scanning calorimetry. A thermally reversing compositional window was reported in the IP, where the glasses are generally nonaging. This behavior makes IP Ge–As–Se glasses very interesting for photonics applications since structural relaxation observed in most amorphous materials is detrimental to the stability of all photonic devices.$^7$ The Boolchand IP in As$_x$Se$_{1-x}$ has been found to occur for MCN between 2.29 and 2.37, while in Ge$_x$As$_y$Se$_{1-x-y}$ glasses containing the same concentrations of Ge and As it appears for MCN between 2.27 and 2.46.$^8$ Recently, however, it was reported that the absence of aging within the so-called reversibility windows was not found in As$_x$Se$_{1-x}$ glasses that had been subjected to long-term physical aging.$^9$ Therefore, further experiments for a wide compositional range are necessary to elucidate the correlation between the network structure, the physical properties, and MCN. Obviously, a starting point to understand the IP is to examine the elastic response of the glassy network.

We, therefore, prepared 17 glasses with different compositions covering all the glass-forming regions including floppy, intermediate, and stressed rigid phases of the phase diagram.$^5$ A detailed description about sample preparation can be found in our previous work.$^9$ The glass transition temperature $T_g$ was measured using a differential scanning calorimeter (DSC) (Shimadzu DSC-50) with 10 K/min scanning rate. The density $\rho$ of the samples was measured using a Mettler H20 balance (Mettler-Toledo Ltd., Switzerland) with a MgO crystal used as a reference. Samples from each glass composition were weighed five times and the average density was recorded. Ultrasonic pulse interferometry was employed to measure both shear and compressional wave velocities at room temperature within the transducer response envelope centered at a resonant frequency of 20 MHz. The ultrasonic travel times were systematically corrected to reduce the effect of the bonding layer between the sample and the transducer.$^{10}$ The shear $C_s$ and compressional $C_c$ elastic moduli were calculated using the formulas $C_s = \rho V_s^2$ and $C_c = \rho V_c^2$, where $V_s$ and $V_c$ are, respectively, the shear and compressional wave velocities. The errors in the measurements of both shear and compressional elastic moduli were estimated to be less than 0.5%.

Figure 1 shows the density of the Ge$_x$As$_y$Se$_{1-x-y}$ glasses as a function of MCN. For comparison, the data from Ref. 11 have also been included. The samples from two different sources exhibit similar behavior. For example, the density first increases with increasing MCN exhibiting a maximum at MCN $\approx$ 2.45 before decreasing to a minimum at MCN around 2.65. For MCN < 2.4 corresponding, for example, to glass samples such as Ge$_{10}$As$_{55}$Se$_{35}$, Ge$_{25}$As$_{60}$Se$_{15}$, and Ge$_{30}$As$_{30}$Se$_{40}$, if there were no changes in the arrangement of the atoms in the glass, progressively replacing Se by As atoms should reduce the glass density because Se is heavier than As. Therefore, the observed opposite trend of increasing density with increasing MCN for MCN < 2.4 suggests that

$^a$Electronic mail: rpw111@rsphysse.anu.edu.au.
creases with increasing MCN except for the samples with higher T_g. The appearance of phase separation can, however, destroy the backbone of the network and consequently cause a drop in T_g, emphasizing that this is due to a medium-range structural order. Between 2.4 and 2.65, several experimental results have confirmed that chalcogenide glasses have a layer-type structure which contain flexible segments. Therefore increasing the concentration of Ge and As will result in a vitreous matrix with higher T_g. The appearance of phase separation can, however, destroy the backbone of the network and consequently cause a drop in T_g. Noteworthy is that in Table I, the glasses with the same MCN of 2.4 exhibit almost the same T_g, emphasizing that T_g does depend on the network connectivity and hence MCN, rather than the particular chemical composition.

The acoustic velocities in Table I are in good agreement with the published values for samples with similar compositions. For example, Krause et al. reported that T_g and V_c for Ge_{24}As_{24}Se_{52} glasses were 1.037 and 2.518 km/s, respectively, about 4.5% higher than our results. Ohmachi and Uchida reported that T_g and V_c were 1.227 ± 0.002 and 2.250 ± 0.003 km/s, respectively, in As_{2}Se_{3}, which are very close to the values we obtained for Ge_{5}As_{30}Se_{75}. Yun et al. reported that in Ge_{8}Se_{95}, T_g and V_c were 1.03 ± 0.02 and 1.88 ± 0.02 km/s, very close to our results for Ge_{5}As_{10}Se_{85} where the values were 1.037 and 1.982 km/s, respectively.

The evolution of elastic moduli C_s and C_c as a function of MCN is plotted in Figs. 2(a) and 2(b). The key result is the simultaneous appearance of two transition thresholds at MCN = 2.45 and 2.65, respectively. Unlike the results reported in Refs. 16 and 17 where the elastic moduli below MCN = 2.4 were almost constant, we observed increasing moduli with increasing MCN for Se-rich samples such as Ge_{5}As_{10}Se_{85}, Ge_{5}As_{20}Se_{75}, and Ge_{5}As_{30}Se_{65} glasses. The differences could be caused by the complete neglect of van der Waals interactions and dihedral angle forces in the theoretical treatment presented in Ref. 16, which are certainly needed to stabilize the structure in the floppy phase which exists for MCN < 2.4 and the inaccurate representation of MCN values in Ref. 17 due to the presence of 6%–8% oxygen impurity in their samples. Since the van der Waals interaction decreases with decreasing Se concentration in the three Se-rich samples, an increase in the elastic moduli becomes a natural result of introducing Ge and As.

For MCN between 2.45 and 2.65, C_s and C_c are almost constant at ~68 and ~230 kbar, respectively. Tanaka commented that this is due to a medium-range structural order. Between 2.4 and 2.65, several experimental results have confirmed that chalcogenide glasses have a layer-type structure which contain flexible segments. Thus, when compressing the samples, the van der Waals forces between the segments are mainly responsible for the moduli, while the covalent bonds within an individual segment are almost unperturbed by pressure. Therefore all the glasses have

---

**TABLE I.** A list of the prepared samples ordered by compositions, MCN, shear acoustic velocity V_c, compressional acoustic velocity V_p, shear elastic module C_s, and compressional module C_c.

<table>
<thead>
<tr>
<th>Composition</th>
<th>MCN</th>
<th>T_g (°C)</th>
<th>(\rho) (g/cm³)</th>
<th>V_p (km/s)</th>
<th>V_c (km/s)</th>
<th>C_s (kbar)</th>
<th>C_c (kbar)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ge_{5}As_{10}Se_{85}</td>
<td>2.2</td>
<td>133.5</td>
<td>4.391 ± 0.002</td>
<td>1.037</td>
<td>1.982</td>
<td>47.19</td>
<td>172.49</td>
</tr>
<tr>
<td>Ge_{5}As_{20}Se_{75}</td>
<td>2.3</td>
<td>145.2</td>
<td>4.475 ± 0.003</td>
<td>1.117</td>
<td>2.098</td>
<td>55.88</td>
<td>197.15</td>
</tr>
<tr>
<td>Ge_{9}As_{24}Se_{66}</td>
<td>2.4</td>
<td>179.5</td>
<td>4.538 ± 0.001</td>
<td>1.222</td>
<td>2.248</td>
<td>67.62</td>
<td>229.00</td>
</tr>
<tr>
<td>Ge_{15}As_{10}Se_{85}</td>
<td>2.4</td>
<td>179.3</td>
<td>4.427 ± 0.001</td>
<td>1.172</td>
<td>2.158</td>
<td>60.87</td>
<td>206.23</td>
</tr>
<tr>
<td>Ge_{11}As_{32}Se_{64.5}</td>
<td>2.44</td>
<td>210.5</td>
<td>4.488 ± 0.006</td>
<td>1.240</td>
<td>2.240</td>
<td>69.08</td>
<td>225.29</td>
</tr>
<tr>
<td>Ge_{11}As_{32}Se_{64.5}</td>
<td>2.47</td>
<td>236.7</td>
<td>4.495 ± 0.001</td>
<td>1.250</td>
<td>2.212</td>
<td>70.16</td>
<td>219.66</td>
</tr>
<tr>
<td>Ge_{11}As_{32}Se_{64.5}</td>
<td>2.48</td>
<td>204.9</td>
<td>4.498 ± 0.001</td>
<td>1.193</td>
<td>2.212</td>
<td>64.10</td>
<td>220.15</td>
</tr>
<tr>
<td>Ge_{12.5}As_{32}Se_{62.5}</td>
<td>2.5</td>
<td>247.9</td>
<td>4.493 ± 0.006</td>
<td>1.249</td>
<td>2.276</td>
<td>70.02</td>
<td>232.61</td>
</tr>
<tr>
<td>Ge_{12.5}As_{32}Se_{62.5}</td>
<td>2.55</td>
<td>280.4</td>
<td>4.448 ± 0.001</td>
<td>1.242</td>
<td>2.261</td>
<td>68.65</td>
<td>227.46</td>
</tr>
<tr>
<td>Ge_{13}As_{32}Se_{61}</td>
<td>2.59</td>
<td>293.4</td>
<td>4.434 ± 0.005</td>
<td>1.244</td>
<td>2.290</td>
<td>68.53</td>
<td>232.41</td>
</tr>
<tr>
<td>Ge_{22}As_{32}Se_{58}</td>
<td>2.64</td>
<td>323.7</td>
<td>4.435 ± 0.001</td>
<td>1.254</td>
<td>2.284</td>
<td>69.68</td>
<td>231.02</td>
</tr>
<tr>
<td>Ge_{13}As_{32}Se_{51}</td>
<td>2.64</td>
<td>285.9</td>
<td>4.384 ± 0.002</td>
<td>1.212</td>
<td>2.223</td>
<td>65.10</td>
<td>218.90</td>
</tr>
<tr>
<td>Ge_{22}As_{32}Se_{54}</td>
<td>2.68</td>
<td>335.9</td>
<td>4.449 ± 0.002</td>
<td>1.274</td>
<td>2.306</td>
<td>72.01</td>
<td>236.12</td>
</tr>
<tr>
<td>Ge_{24}As_{32}Se_{52}</td>
<td>2.72</td>
<td>353.1</td>
<td>4.437 ± 0.002</td>
<td>1.309</td>
<td>2.361</td>
<td>76.26</td>
<td>248.09</td>
</tr>
<tr>
<td>Ge_{25}As_{32}Se_{55}</td>
<td>2.78</td>
<td>383.3</td>
<td>4.431 ± 0.001</td>
<td>1.369</td>
<td>2.435</td>
<td>82.43</td>
<td>260.85</td>
</tr>
<tr>
<td>Ge_{15}As_{10}Se_{70}</td>
<td>2.85</td>
<td>404.3</td>
<td>4.441 ± 0.001</td>
<td>1.457</td>
<td>2.552</td>
<td>94.22</td>
<td>289.17</td>
</tr>
<tr>
<td>Ge_{13}As_{32}Se_{47}</td>
<td>2.86</td>
<td>405.2</td>
<td>4.452 ± 0.001</td>
<td>1.506</td>
<td>2.648</td>
<td>100.9</td>
<td>311.2</td>
</tr>
</tbody>
</table>

Fig. 1. Density of the Ge_{x}As_{1-x}Se_{85} glasses from our results (solid squares and error bars) and from Ref. 11 (open circles).
moduli of similar magnitude, irrespective of their detailed microscopic structure.

For MCN values above 2.65, the segments will be cross linked by increasing Ge and As concentrations forming a stressed-rigid phase. A line fit to the data above MCN = 2.65 in Fig. 2(b) when projected to MCN = 4 gives $C_v = 788.5$ kbar, which is comparable with crystalline Ge at 880 kbar where no van der Waals interaction exists. Tanaka reported that the constraint-counting formalism yields a value of MCN $\approx 2.67$ for transition to a rigid state if a two-dimensional layer structure is embedded in a 3-dimensional space. The transition we observed at 2.65 is, therefore, very close to that threshold.

All previous attempts to search for elastic transitions in chalcogenide glasses failed to identify the existence of two transition thresholds. We cannot be absolutely certain as to whether these two transitions are specifically related to the IP threshold at 2.65. However, our results clearly demonstrate the existence of two transition thresholds at MCN 2.45 and 2.65, which correlate with the stress-strain transitions predicted for this ternary glass system.

In summary, we prepared Ge$_x$As$_{1-x}$Se$_{1−y}$ glasses spanning a MCN from 2.2 and 2.86. $T_g$ was found to increase with increasing MCN, except those glasses located within the nanoscale phase-separated regions of the phase diagram. The density of the glasses shows a maximum at 2.45 and a minimum at 2.65. The elastic moduli of the glasses were estimated from the shear and compressional wave velocities measured by the ultrasonic pulse interferometry. At the first time we simultaneously observed two elastic transition thresholds at MCN 2.45 and 2.65, which correlate with the structural transitions predicted for this ternary glass system.

This research is supported by the Australian Research Council through its Centres of Excellence and Federation Fellow Programs.


![Shear Wave](image1.png)

**FIG. 2.** (Color online) (a) The shear and (b) compressional elastic moduli and their error bars as a function of MCN. The solid lines correspond to least-squares fitting results.