The M 4 Core Project with HST – II. Multiple stellar populations at the bottom of the main sequence

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Accepted 2014 January 6. Received 2013 December 29; in original form 2013 November 21

ABSTRACT

The M 4 Core Project with HST is designed to exploit the Hubble Space Telescope (HST) to investigate the central regions of M 4, the Globular Cluster closest to the Sun. In this paper we combine optical and near-infrared photometry to study multiple stellar populations in M 4. We detected two sequences of M-dwarfs containing ~38 per cent (MS1) and ~62 per cent (MS2) of MS stars below the main-sequence (MS) knee. We compare our observations with those of NGC 2808, which is the only other GCs where multiple MSs of very low-mass stars have been studied to date. We calculate synthetic spectra for M-dwarfs, assuming the chemical composition mixture inferred from spectroscopic studies of stellar populations along the red giant branch, and different helium abundances, and we compare predicted and observed colours. Observations are consistent with two populations, one with primordial abundance and another with enhanced nitrogen and depleted oxygen.

Key words: stars: Population II – globular clusters: individual: NGC 6121.

1 INTRODUCTION

The M 4 Core Project with HST is a Hubble Space Telescope (HST) large program (GO-12911, PI: Bedin) designed to provide high-accuracy astrometry and photometry for stars in the core of the closest Globular Cluster (GC) M 4 (d⊙ = 2.2 kpc, Harris 1996, updated as in 2010). The observations are designed to detect binary dark companions (such as a black hole, a white dwarf, or a neutron star) of bright main-sequence (MS) stars by measuring the ‘wobble’ of the luminous star around the centre of mass of the binary system.

The exquisite photometry and astrometry provided by HST make this data set ideal for several other astrophysical applications including the search for variable stars or transiting exoplanets, the measure of absolute proper motions and annual parallax, the study of internal dynamics and of photometric binaries, and the search for intermediate-mass central black hole (see Bedin et al. 2013, hereafter Paper I, for an overview of the project). One of the main goals of the project is the investigation of multiple stellar populations in this cluster.

Several papers have been dedicated to the study of the different stellar generations host by M 4. Spectroscopy has revealed that M 4 stars have inhomogeneous content of C, N, O, Al and Na (e.g. Gratton, Quarta & Ortolani 1986; Brown & Wallerstein 1992; Drake, Smith & Suntzeff 1992; Smith et al. 2005) and exhibit Na–O, Al–O, C2014 The Authors
Published by Oxford University Press on behalf of the Royal Astronomical Society

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and C–N anticorrelations (e.g. Ivans et al. 1999; Marino et al. 2008; Carretta et al. 2009; Villanova & Geisler 2011). The distribution of [Na/Fe] and [O/Fe] is bimodal, and the two groups of Na-poor/ O-rich and Na-rich/O-poor stars, which are commonly associated with a first and a second stellar generation, populate two distinct red giant branches (RGBs; Marino et al. 2008). The colour distribution of horizontal-branch (HB) stars is also bimodal and is strictly related to the stellar populations: blue-HB stars share the same chemical composition as second-generation stars, while the red-HB stars are consistent with being first generation (Marino et al. 2011). Photometric evidence of multiple populations in M 4 (Marino et al. 2008; Lee et al. 2009; Monelli et al. 2013) is based on the analysis of the RGB, while, so far, no evidence of multiple or extended MS has been found.

In a recent study of the massive GC NGC 2808, Milone et al. (2012a, hereafter M12a) have demonstrated that the F110W and F160W filters of the Infrared Channel of the Wide Field Camera 3 (WFC3/IR) on the HST are powerful tools to identify multiple sequences along the MS of very-low mass (VLM) stars. The near-infrared (NIR) portion of the spectrum of cold M-dwarfs is very sensitive to the effects of molecules, in particular H$_2$O. For this reason, NIR photometry can provide unique information on multiple populations among VLM stars. In this paper we extend the study by M12a on NGC 2808 to the less-massive GC M 4. We exploit the data set available from GO-12911 and from the HST archive to detect, for the first time, multiple stellar populations at the bottom of the MS of this GC.

2 DATA AND DATA ANALYSIS

The data set used in this paper consists in images obtained with the IR and Ultraviolet and visual camera (UVIS) of WFC3 and the Wide Field Channel of the Advanced Camera for Surveys (WFC/ACS) of HST. In addition, we used the photometric catalogues in F606W and F775W compiled by Bedin et al. (2009) in their study of the M 4 white-dwarf cooling sequence (GO-10146, PI. L. Bedin), and the photometric catalogue in F467M described in Paper I.

WFC3/IR data are archival HST images from program GO-12602 (PI. A. Dieball). This data set consists of 16 × 652 s exposures through F110W and 8 × 652 s through F160W of a ∼2 × 2 arcmin field located at about 1.5 arcmin North-East from the cluster centre. Since the original goals of GO-12602 project were the search for brown dwarfs in GCs and the study of the hydrogen-burning limit and the stellar/sub-stellar border of the MS, this data set is optimized to get high-accuracy photometry of faint M-dwarfs. We also used WFC3/UVIS 3 × 911 s and 3 × 922 s exposures in F390W from GO-12602 (PI. A. Dieball) and 4 × 50 s exposures in F814W from GO-12311 (PI. G. Piotto). We corrected the poor charge-transfer efficiency (CTE) in the WFC3/UVIS data by using the procedure by Anderson & Bedin (2010).

Photometry and astrometry of WFC3/IR images have been carried out by using a software package that is based largely on the tools presented in Anderson & King (2006). We corrected stellar positions for geometric distortion by using the solution developed by one of us (JA). Photometry has been calibrated as in Bedin et al. (2005) by using online estimates for zero-points and encircled energies.1 Both the software package and geometric distortion correction tool will be presented in a forthcoming paper. Photometry and astrometry of WFC3/UVIS have been determined as in Paper I.

The colour–magnitude diagrams (CMDs) have been corrected for differential reddening as in Milone et al. (2012b). First, we selected a subsample of stars by including only those cluster members that lie on the MS and are brighter than the knee. We extracted the MS ridge line and for each star, we estimated how the 35 neighbouring stars in the subsample systematically lie to the red or the blue of the fiducial sequence. This systematic colour and magnitude offset, measured along the reddening line, is indicative of the differential reddening. We found that the reddening variation, within the field of view analysed in this paper, is smaller than $\Delta E(B − V) < 0.025$ mag, and is consistent with the degree of differential reddening measured by Hendricks et al. (2012) and Monelli et al. (2013) in the same region.

Stellar proper motions are determined by comparing the positions of stars measured at two different epochs from GO-10146 ACS/WFC data (epoch: 2004.6) and GO-12602 IR/WFC3 data (epoch: 2012.3), and by following a method that has been comprehensively described in other papers (e.g. Bedin et al. 2003, 2008; Anderson & van der Marel 2010).

3 MULTIPLE SEQUENCES OF M-DWARFS

The $m_{\text{F160W}}$ versus $m_{\text{F110W}}$ CMD (hereafter NIR CMD), corrected for differential reddening, is shown in Fig. 1 for all the stars in the field of view. The inset shows the vector-point diagram (VPD) of proper motions in WFC3/IR pixel units. The fact that the absolute proper motion of M 4 differs significantly from that of background/foreground stars makes proper motions measurements the tool of choice for separating field stars from cluster members (see Bedin et al. 2003).

In Fig. 1 we represent with black circles the stars that, according to their proper motion, are probable cluster members, while red crosses indicate field stars. A visual inspection of the cluster CMD

1 http://www.stsci.edu/hst/wfc3/phot_zp_lbn

Figure 1. $m_{\text{F160W}}$ versus $m_{\text{F110W}}$ CMD of stars in the WFC3/IR field of view. Stars that are M 4 members according to their proper motion are plotted as black points, while field stars are represented with red crosses. The inset shows the VPD (in WFC3/IR pixel units) of the proper motions for the same stars as shown in the CMD. The red circle is adopted to separate cluster members from field stars.
reveals that below the turn off, over a range of $\sim 2.5$ F160W magnitudes ($\sim 14.0 < m_{F160W} < 17.5$), the MS is narrow and there are no evident signs of any large colour spread or split. At fainter luminosities, below the MS knee, there is a dramatic change in the colour distribution of MS stars, and the MS splits into two sequences. This section is dedicated to the analysis of these sequences of VLM stars, and we start by demonstrating that the bimodal colour distribution is not entirely due to photometric errors.

To do this, an effective test consists of subdividing the available F110W, F160W, F606W and F775W images of the same field into two independent groups (NIR and visual) and compare their CMDs. If the colour broadening is entirely due to photometric errors, a star that has bluer (or redder) colours in one CMD will have an equal probability of being red or blue in the second one. However, if the two sequences identified in the first data set have systematically different magnitudes and colours in the second one, the colour broadening of the MS is more likely to be intrinsic. This procedure was introduced by Anderson et al. (2009) in their analysis of the colour spread among MS stars in 47 Tuc and is applied in the following to the case of M 4.

In Fig. 2, we compare two CMDs of the faint MS stars obtained from two independent data sets. The NIR CMD is plotted in the upper-left panel and the $m_{F775W}$ versus $m_{F606W} - m_{F775W}$ CMD (hereafter visual CMD) is shown in the upper-right panel. Reddening direction is indicated in each CMD by grey arrows. The length of each arrow corresponds to a reddening variation of $\Delta E(B - V) = 0.17$ mag that is about seven times larger than the maximum reddening variation observed in the M 4 field studied in this paper.

In the NIR CMD we have defined, by eye, two groups of $MS_I$ and $MS_{II}$ stars with $m_{F160W} > 17.2$ that we have coloured green and magenta, respectively. In the visual CMD, we kept for each star the same colour as defined in NIR: it is quite clear that the two groups of stars remain well separated. Moreover, the evidence that $MS_I$ stars...
have, on average redder $m_{F606W} - m_{F775W}$ colour than MS$_{I}$ stars but bluer $m_{F110W} - m_{F160W}$ colour demonstrates that the colour spread cannot be due to residual differential reddening.

In order to strengthen this result, in each CMD we have derived a fiducial line of MS$_{II}$ stars, which is represented as a continuous magenta line in Fig. 2. We then calculated the differences between the $m_{F606W} - m_{F775W}$ (and $m_{F110W} - m_{F160W}$) colours of each star and the colour of the fiducial at the same $m_{F775W}$ (or $m_{F160W}$) magnitude. These colour residuals are designated $\Delta_{\text{VIS}} = \Delta (m_{F606W} - m_{F775W})$ and $\Delta_{\text{NIR}} = \Delta (m_{F110W} - m_{F160W})$.

The verticalized $m_{F160W}$ versus $\Delta_{\text{NIR}}$ and $m_{F775W}$ versus $\Delta_{\text{VIS}}$ CMDs are plotted in the panels (c$_{1}$) and (d$_{1}$), respectively. Panels (c$_{2}$) and (d$_{2}$) show the corresponding histogram of the colour–residual distribution for the straightened MS$_{I}$ and MS$_{II}$ in three luminosity intervals. In addition, in panel (e) we show the anti-correlation between $\Delta_{\text{VIS}}$ and $\Delta_{\text{NIR}}$ colour residuals. MS$_{II}$ stars have on average bluer $m_{F606W} - m_{F775W}$ colours than MS$_{I}$ stars with the same F775W magnitude. The colour order is reversed in the NIR CMD. This behaviour further confirms that the colour broadening is an intrinsic feature of the faint MS of M 4.

Having excluded the possibility that the colour spread of VLM MS stars is due to photometric errors, we can now estimate the fraction of stars in each of the two sequences. To do this we applied a procedure that has been widely used by our group (e.g. Piotto et al. 2007) and is illustrated in Fig. 3 for M 4. We restrict our study to MS stars in the luminosity interval where the split MS is more clearly visible ($18.5 < m_{F160W} < 20.1$). The left panel of Fig. 3 shows the NIR CMD of these stars while the $m_{F160W}$ versus $\Delta_{\text{NIR}}$ diagram is shown in the middle panel. The histogram distribution of $\Delta(m_{F110W} - m_{F160W})$, which is plotted in the right panel for stars in three F160W intervals 18.50 < $m_{F160W}$ < 19.03, 19.03 < $m_{F160W}$ < 19.57, 19.57 < $m_{F160W}$ < 20.10, is clearly bimodal and has been fitted with the sum of two Gaussians. The fraction of stars in each sequence was estimated by comparing the area under the two Gaussians. From the upper, the middle and the fainter histogram, we found that the less populated MS contains 36 per cent, 44 per cent and 35 per cent of stars, respectively. We infer that, on average, 38 ± 4 per cent of stars belong to the less populated MS$_{I}$, while the most populated MS$_{II}$ is made of the 62 ± 4 per cent of stars. The error is estimated as the rms of the three independent estimates divided by the square root of two.

Marino et al. (2008), in their spectroscopic study of stellar populations along the RGB of M 4, concluded that 64 ± 10 per cent of the RGB stars are sodium rich and oxygen poor, while the remaining 36 ± 10 per cent ones have Na and O abundance similar to those of halo-field stars with the same metallicity. We note that the fractions of MS$_{I}$ and MS$_{II}$ stars are identical, at one-sigma level, to the fractions of Na-rich/O-poor and Na-poor/O-rich stars, respectively. In the next section, we further investigate the connection between the observed sequences of M-dwarfs and the multiple stellar populations in M 4.

### 4 COMPARISON WITH NGC 2808

The IR channel of the WFC3 camera on HST revealed multiple sequences of VLM stars in two other massive GCs, namely NGC 2808 and NGC 5139 (M12a; Milone 2012). The case of NGC 2808 has been studied in particularly large details and therefore it can provide us with useful information for our study on M 4.

The similarity in metallicity between NGC 2808 and M 4 justifies the comparison between the two.² NGC 2808 has been widely studied in the context of multiple stellar populations. The upper part of its CMD, from the turn-off down to the MS knee, is split in three sequences (Piotto et al. 2007), where the middle and the blue MS are highly helium enhanced (up to $Y \sim 0.39$ for the bluest MS), while the red MS has primordial helium (D’Antona & Caloi 2004; D’Antona et al. 2005; Piotto et al. 2007; Milone et al. 2012b). Furthermore, spectroscopic studies have revealed significant star-to-star variations in the light-element abundances (e.g. Norris & Smith 1983; Bragaglia et al. 2010; Pasquini et al. 2011; Marino et al. 2014) with the presence of an extreme Na–O anticorrelation (Carretta et al. 2006, Carretta et al. 2009).

In the NIR CMD, the three MSs merge together at the luminosity of the MS knee, while at fainter magnitudes, at least two MSs can be identified. A bluer, more populated MS$_{I}$ that contains ~65 per cent of MS stars, and a MS$_{II}$ with ~35 per cent of stars. The fractions of stars along MS$_{II}$, and MS$_{I}$ are very similar to the fraction of red-MS stars (~62 per cent) and the total fraction of middle-MS and blue-MS stars (~24 + 14 = 38 per cent; Milone et al. 2012b), respectively.

The observed CMD of NGC 2808 has been compared with appropriate evolutionary models for VLM stars and synthetic spectra that account for the chemical composition of the three stellar populations of this cluster (see M12a for details). It turns out that MS$_{II}$ is associated with the first stellar generation, which has primordial He, and O-C-rich/N-poor stars, while MS$_{I}$ corresponds to a second-generation stellar population that is enriched in He and N and depleted in C and O. The MS$_{I}$ is the faint counterpart of the red MS identified by Piotto et al. (2007), whereas

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² Metallicity estimates of M4 derived from high-resolution spectroscopy include: [Fe/H] = −1.18 ± 0.01 (Ivans et al. 1999), [Fe/H] = −1.07 ± 0.01 (Marino et al. 2008), [Fe/H] = −1.20 ± 0.01 (Carretta et al. 2009), [Fe/H] = −1.06 ± 0.02 (Villanova et al. 2012), [Fe/H] = −1.12 ± 0.02 (Marino et al. 2011), [Fe/H] = −1.07 ± 0.01 (Malavolta et al. 2013). In the case of NGC 2808 measurements of [Fe/H] from high-resolution spectra provide: [Fe/H] = −1.15 ± 0.01 (Carretta et al. 2006), [Fe/H] = −1.15 ± 0.07 (Pasquini et al. 2011), [Fe/H] = −1.22 ± 0.01 (Marino et al. 2014).
the MS\textsubscript{I} corresponds to the lower-mass counterpart of the middle MS and blue MS discussed in the Piotto et al. paper.

The left panel of Fig. 4 reproduces the $m_{\text{F160W}}$ versus $m_{\text{F110W}}$ CMD of NGC 2808 from M12a with overlaid fiducial lines of MS\textsubscript{I} and MS\textsubscript{II}. The vertical and horizontal dotted lines mark the colour and the magnitude of the redest point of MS\textsubscript{II} fiducial. The middle panel shows the same NIR CMD of M 4 as in Fig. 1 with the fiducials of the two MSs superimposed. The fiducial lines of NGC 2808 and M 4 MSs are compared in the right panel where we subtracted from the colour and the magnitude of each point, the colour and the magnitude of the redest point of the corresponding fiducial [$\Delta(m_{\text{F110W}} - m_{\text{F160W}})$ and $\Delta m_{\text{F160W}}$].

The MS\textsubscript{I} fiducials of M 4 and NGC 2808 overlap for almost the entire analysed $\Delta m_{\text{F160W}} - \Delta(m_{\text{F110W}} - m_{\text{F160W}})$ interval. On the contrary, the MS\textsubscript{II} fiducials exhibit significant differences. Above the MS knee, MS\textsubscript{I} is significantly redder than MS\textsubscript{II} in NGC 2808, while any colour difference of the two MSs of M 4 is small, and MS\textsubscript{II} is almost superimposed to MS\textsubscript{I} in our NIR CMD. Below the MS knee, MS\textsubscript{II} is redder than MS\textsubscript{I} in both clusters but the colour difference is about 2.5 times larger in the case of NGC 2808.

5 INTERPRETING THE SPLIT MS

In an attempt to explain the behaviour of MS\textsubscript{I} and MS\textsubscript{II} in the CMDs of Fig. 5 and to understand the origin of the double MS, we have followed a procedure similar to the one adopted by M12a in their analysis of multiple MSs of VLM stars in NGC 2808.

While for NGC 2808 only NIR photometry was available for VLM stars, we can combine visual and IR photometry for M 4 to get information of the two MSs of M-dwarfs by comparing their relative position in different CMDs. Since we have photometry in seven filters, we can derive six CMDs $m_{\text{F160W}}$ versus $m_{\text{F110W}}$ ($X = \text{F390W, F467M, F606W, F775W, F814W, F110W}$) that are shown in Fig. 5 where we have used for MS\textsubscript{I} and MS\textsubscript{II} the same colour codes introduced in Fig. 2.

In all the cases, MS\textsubscript{I} is bluer than MS\textsubscript{II} but the separation changes slightly from one colour to another. To quantify the separation of the two sequences we have calculated the colour distance between MS\textsubscript{I} and MS\textsubscript{II} at $m_{\text{F110W}} = 18.75$, which is the magnitude corresponding to the horizontal lines in Fig. 5. These colour differences, $\delta(m_{\text{x}} - m_{\text{F160W}})$, are listed in Table 1.

5.1 The possible effect of binaries

A broadening of the MS could be the result of binaries which are observed in GCs as a spread of the MS. At the distance of M 4, a binary system will appear as a single point-like source, whose luminosity is equal to the sum of the luminosity of its components. Equal-mass MS binaries (MS–MS binary) form a sequence that runs almost parallel to the MS, ~0.75 magnitudes brighter. When the masses of the two components are different, the binary will appear brighter than each component and populate a CMD region between the fiducial line and the equal-mass binary line. In Fig. 5 we have superimposed to each CMD the fiducial lines of MS\textsubscript{I} and MS\textsubscript{II} (green and magenta on continuous lines) as well as the fiducial lines of equal-mass MS\textsubscript{I} – MS\textsubscript{I} and MS\textsubscript{II} – MS\textsubscript{II} binaries (green and magenta dash–dotted lines). The fact that in the $m_{\text{F160W}}$ versus $m_{\text{F110W}}$ CMD all MS\textsubscript{II} stars lie outside the region between the two green lines demonstrate that MS\textsubscript{II} cannot be explained with MS\textsubscript{I} – MS\textsubscript{I} binaries. Similarly, the evidence, that in several CMDs of Fig. 5 (like $m_{\text{F110W}}$ versus $m_{\text{F160W}}$ and $m_{\text{F775W}}$ versus $m_{\text{F160W}}$) most of MS\textsubscript{I} stars are located outside the region populated by MS\textsubscript{I} – MS\textsubscript{I} binaries, demonstrates that MS\textsubscript{I} is inconsistent with a population of MS\textsubscript{II} – MS\textsubscript{II} binaries.

5.2 The effect of multiple populations

In the previous section, we have demonstrated that binaries are not responsible of the splitting of the MS. Here, we investigate the possibility that MS bimodality is due to the presence of multiple generations of stars. In order to interpret our observations we need to compare the observed colours of MS\textsubscript{I} and MS\textsubscript{II} M-dwarfs with predictions from theoretical models as done by M12a for NGC 2808. Since NGC 2808 and M 4 have similar metallicities, for M 4, we used the grid of evolutionary models for low- and VLM stars adopted by M12a for NGC 2808.

These theoretical models have been calculated by using the same physical inputs described by Cassisi et al. (2000) and Pietrinferni.
Figure 5. $m_{F160W}$ versus $m_X - m_{F160W}$ ($X = F110W, F814W, F775W, F606W, F467M$ and $F390W$) CMDs of M 4. We coloured green and magenta the groups of $MS_I$ and $MS_{II}$ stars defined in Fig. 2. Green and magenta continuous lines are the fiducials of $MS_I$ and $MS_{II}$, respectively, while dash–dotted lines mark the locus of equal-mass $MS_I$ − $MS_I$ and $MS_{II}$ − $MS_{II}$ binaries. Grey lines at $m_{F160W} = 18.75$ mark the magnitude level where the colour separation between $MS_I$ and $MS_{II}$ has been calculated (see text for details).

Table 1. Colour difference between $MS_I$ and $MS_{II}$ at $m_{F160W} = 18.75$.

<table>
<thead>
<tr>
<th>$\delta (m_{F390W} - m_{F160W})$</th>
<th>$\delta (m_{F467M} - m_{F160W})$</th>
<th>$\delta (m_{F606W} - m_{F160W})$</th>
<th>$\delta (m_{F775W} - m_{F160W})$</th>
<th>$\delta (m_{F814W} - m_{F160W})$</th>
<th>$\delta (m_{F110W} - m_{F160W})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-0.126 \pm 0.023$</td>
<td>$-0.069 \pm 0.018$</td>
<td>$-0.047 \pm 0.010$</td>
<td>$-0.054 \pm 0.008$</td>
<td>$-0.054 \pm 0.005$</td>
<td>$-0.042 \pm 0.008$</td>
</tr>
</tbody>
</table>

et al. (2006) and have been converted into the observational domain by integrating the synthetic spectra of the BT-Settl AGSS model atmosphere grid\(^3\) (Allard, Homeier & Freytag 2012) over the IR WFC3 bandpasses.

As already discussed in Section 1, M 4 exhibits star-to-star variations in the abundance of several light elements like (C, N, O, Mg, Al, Na), which affect the colour of the RGB, the SGB and MS (Marino et al. 2008; Sbordone et al. 2011; Milone et al. 2012c, Cassisi et al. 2013). Since the literature model atmospheres used to calculate colour–$T_{eff}$ transformation do not account for the light-element abundances of the two stellar populations of M 4, we have computed synthetic spectra with the appropriate chemical composition. Specifically we assumed for $MS_I$ and $MS_{II}$ the abundances of C, N, O, Mg, Al, and Na as measured for first- and second-generation RGB stars by Marino et al. (2008, see their table 6).

We also assumed that $MS_{II}$ is slightly helium enhanced ($Y = 0.27$) with respect to $MS_I$ which has primordial helium content ($Y = 0.248$) as inferred by D’Ercole et al. (2010) on the basis of their comparison of chemical-evolution models and measurements of sodium and oxygen in RGB stars.

We have used the ATLAS9 and SYNTH programs (Kurucz 2005; Sbordone, Bonifacio & Castelli 2007) to calculate synthetic spectra of a $MS_I$ and $MS_{II}$ star at $m_{F160W} = 18.75$. We assumed $T_{eff} = 3700$ K, log $g = 5.3$ and microturbulence 1.0, that are the values derived for a M-dwarf with $m_{F160W} = 18.75$ from the best-fitting BaSTI isochrones (Pietrinferni et al. 2004, 2006). We accounted for CO, C$_2$, CN, OH, MgH, SiH, H$_2$O, TiO, VO and ZrO.

\(^3\) http://phoenix.ens-lyon.fr/simulator.
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Figure 6. Left: synthetic spectra for a \( M_{\text{SI}} \) (green) and \( M_{\text{SII}} \) (magenta) star at \( m_{\text{F160W}} = 18.75 \) (upper panel). Flux ratio (middle panel). Transmission curves of the filters used in this work (lower panel). Right: \( m_X - m_{\text{F160W}} \) colour distance between \( M_{\text{SI}} \) and \( M_{\text{SII}} \) at \( m_{\text{F160W}} = 18.75 \) (X = F390W, F467M, F606W, F775W, F814W, F110W and F160W). Observations are represented with black circles, while red asterisks indicate results from synthetic spectra.


The synthetic spectra of a representative \( M_{\text{SI}} \) and \( M_{\text{SII}} \) star \( m_{\text{F160W}} = 18.75 \) are compared in the upper-left panel of Fig. 6, while the flux ratio is plotted on the middle-left. The strong absorption at \( \lambda > 13 \, 000 \, \text{Å} \), previously observed in the synthetic spectra of \( M_{\text{SI}} \) star of NGC 2808, is present in spectra of \( M_{\text{SII}} \) and \( M_{\text{SII}} \) and is mainly due to \( \text{H}_2\text{O} \) molecules. In the bottom-left panel we also show the transmission curve of the ACS/WFC and NIR/WFC3 filters used in the analysis.

In contrast with M 4 where the difference in [O/Fe] between the first and second stellar population is smaller than 0.2 dex (e.g. Marino et al. 2008), second-generation stars of NGC 2808 can be depleted in oxygen by up to \( \sim 1.3 \) dex (e.g. Carretta et al. 2006). The feature at \( \lambda > 13 \, 000 \, \text{Å} \) is less evident in the synthetic spectra of \( M_{\text{SII}} \) stars of NGC 2808 as a consequence of their extreme \( \text{O} \)-depletion (see fig. 4 of M12a).

The fact that the colour separation between \( M_{\text{SI}} \) and \( M_{\text{SII}} \) of M 4 is small when compared to NGC 2808 seems to be due to the small \( \text{O} \)-depletion of second-generation stars in M 4. As shown in the right panel of Fig. 6, the trend of the synthetic-colour differences is consistent with the observations. Fig. 6 supports the idea that \( M_{\text{SI}} \) stars represent a first stellar generation, having primordial helium and high oxygen, while \( M_{\text{SII}} \) can be associated with a second generation consisting of stars enhanced in He, N, Na and depleted in O.

6 SUMMARY

NIR infrared photometry obtained with the IR/WFC3 camera of \( \text{HST} \) has revealed a double sequence of M-dwarfs in the CMD of the GC M4 and allowed us to extend the study of its stellar populations to the VLM regime. The NIR CMD of M 4 shows that, below the knee, the MS splits into two distinct components that we designate \( M_{\text{SI}} \) and \( M_{\text{SII}} \). They contain 38 ± 4 per cent and 62 ± 4 per cent of the stars, respectively.

The comparison of observations and synthetic spectra of M-dwarf which accounts for the chemical composition of the two stellar populations in M 4 shows that the presence of the \( \text{H}_2\text{O} \) molecule on the atmosphere of these cold stars has a strong effect on their \( m_{\text{F110W}} - m_{\text{F160W}} \) colour. The fact that light-element variations are inferred also among fully convective M-dwarfs provides strong evidence of their primordial origin and demonstrates that they correspond to different stellar generations. We associate the \( M_{\text{SI}} \) with the first stellar generation, which share the same chemical composition as the Na-poor/O-rich stars observed by Marino et al. (2008) along the RGB. \( M_{\text{SII}} \) corresponds to a second stellar generation and is enriched in Na, N and Al and depleted in C, O and Mg.

We compare the NIR CMDs of M 4 and NGC 2808 where multiple sequences of M-dwarfs have been observed by M12a. We find that the colour separation between \( M_{\text{SI}} \) and \( M_{\text{SII}} \) of M 4 is significantly larger in NGC 2808, likely as a consequence of the extreme abundance pattern of its second generations. The detection of multiple sequences of VLM stars in M 4 suggests that this can be a common feature in GCs and not a peculiarity of massive clusters like NGC 2808 and \( \omega \) Centauri. NIR observations with WFC3 on board \( \text{HST} \) have proven to be a powerful and sensitive tool to study the effect of even small abundance differences on the faint, low-mass MS, and therefore an additional observational windows for the study of multiple stellar populations in GCs down to the lowest-mass MS stars.

ACKNOWLEDGEMENTS

APM and HJ acknowledge the financial support from the Australian Research Council through Discovery Project grant DP120100475.
SC is grateful for financial support from PRIN-INAF 2011 ‘Multiple Populations in Globular Clusters: their role in the Galaxy assembly’ (PI E. Carretta), and from PRIN MIUR 2010-2011, project ‘The Chemical and Dynamical Evolution of the Milky Way and Local Group Galaxies’, prot. 2010LY5N2T (PI F. Matteucci). LRB and GP acknowledge PRIN-INAF 2012 funding under the project entitled: ‘The M4 Core Project with Hubble Space Telescope’.

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