# On the origin of the stellar halo and multiple stellar populations in the globular cluster NGC 1851

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# ABSTRACT

We propose that the observed stellar halo around the globular cluster (GC) NGC 1851 is evidence of its formation in the central region of its defunct host dwarf galaxy. We numerically investigate the long-term dynamical evolution of a nucleated dwarf galaxy embedded in a massive dark matter halo under the strong tidal field of the Galaxy. The dwarf galaxy is assumed to have a stellar nucleus (or a nuclear star cluster) that could be the progenitor for NGC 1851. We find that although the dark matter halo and the stellar envelope of the host dwarf of NGC 1851 can be almost completely stripped during its orbital evolution around the Galaxy, a minor fraction of stars in the dwarf can remain trapped by the gravitational field of the nucleus. The stripped nucleus can be observed as NGC 1851 with no/little dark matter, whereas stars around the nucleus can be observed as a diffuse stellar halo around NGC 1851. The simulated stellar halo has a symmetric distribution with a power-law density slope of  $\sim$ -2 and shows no tidal tails within  $\sim$ 200 pc from NGC 1851. We show that two GCs can merge with each other to form a new nuclear GC embedded in field stars owing to the low stellar velocity dispersion of the host dwarf. This result makes no assumption on the ages and/or chemical abundances of the two merging GCs. Thus, the observed stellar halo and characteristic multiple stellar populations in NGC 1851 suggest that NGC 1851 could have formed initially in the central region of an ancient dwarf galaxy. We predict that the stellar halo of NGC 1851 may have at least three different stellar populations. We also suggest some Galactic GCs with diffuse haloes, such as NGC 1904 and 5694, could be formed in a similar way to NGC 1851. We discuss the importance of GC merging within dwarfs in the formation of multiple stellar populations with abundance spreads in heavy elements in some Galactic GCs, such as M22 and NGC 2419. We also discuss other possible scenarios for the formation of the stellar halo around NGC 1851.

**Key words:** stars: formation – globular clusters: general – galaxies: star clusters: general – galaxies: stellar content.

### **1 INTRODUCTION**

The Milky Way hosts about 150 globular clusters (GCs; Harris 1996–2010 edition ) and these objects have been regarded by many as the best examples of a simple stellar population, that is, single age, helium abundance, metallicity and initial mass function (IMF) (Renzini & Buzzoni 1986). However, many studies have revealed that these simple stellar populations display extremely large chemical abundance variations for the light elements (e.g. see reviews by Smith 1987; Kraft 1994; Gratton, Sneden & Carretta 2004). Although the exact origin(s) of these light-element variations remains

unclear, it has become clear that every well-studied GC shows lightelement-abundance variations.

The massive GC  $\omega$  Cen possesses a large spread in lightelement, Fe-peak-element and neutron-capture-element abundances (e.g. Freeman & Rodgers 1975; Cohen 1981; Norris & Da Costa 1995; Smith et al. 2000), in contrast to the vast majority of GCs, and as such  $\omega$  Cen is regarded as an exception. Indeed, it has been strongly argued that  $\omega$  Cen is the remnant nucleus of an accreted dwarf galaxy (e.g. Freeman 1993). Photometric (Bedin et al. 2004) and spectroscopic (Johnson & Pilachowski 2010) studies now demonstrate the true complexity of this system.

Additionally, photometric and spectroscopic studies of other GCs have revealed complex structure in colour–magnitude diagrams (M22: Piotto 2008; NGC 1851: Milone et al. 2008; 47 tuc: Anderson

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et al. 2009) as well as perhaps unexpected dispersions in heavyelement abundances (M22: Marino et al. 2009; NGC 1851: Yong & Grundahl 2008; Yong et al. 2009; Carretta et al. 2010, 2011; Villanova, Geisler & Piotto 2010). At present, there are a number of GCs which clearly display multiple populations. Of these clusters, NGC 1851 may hold particular importance. NGC 1851 has a bimodal horizontal branch, a double subgiant branch, a large dispersion in s-process element abundances and a dispersion in metallicity (Yong & Grundahl 2008; Carretta et al. 2010, 2011; Villanova et al. 2010). Milone et al. (2011) have recently shown that two stellar populations with different s-element abundances are associated with two distinct populations in subgiant and red-giant branches in NGC 1851. An intriguing, but tentative, speculation is that NGC 1851 may be the product of the merger of two individual clusters (Carretta et al. 2010, 2011). Although recent observations have revealed two distinct populations in the horizontal-branch stars (Salaris, Cassisi & Pietrinferni 2008) and red-giant-branch ones (Han et al. 2009), and a possible bimodal [Fe/H] distribution (Lee et al. 2009) within NGC 1851, it remains unclear how these observations can be explained in the context of GC merging.

Recently, Olszewski et al. (2009) revealed that NGC 1851 is surrounded by a diffuse stellar halo with a size of more than 500 pc and a mass of about 0.1 per cent of the dynamical mass of NGC 1851. The halo has an symmetric distribution with no elongated tidal tails and a power-law radial density profile that can fit to  $r^{-1.24}$ . Diffuse stellar haloes surrounding GCs have also been discovered in Whiting 1 (Carraro, Zinn & Moni Bidin 2007), AM 4 (Carraro 2009), NGC 5694 (Correnti et al. 2011) and NGC 1904 (Carballo-Bello & Martínez-Delgado 2010), which implies that stellar haloes around GCs are not very rare objects. Olszewski et al. (2009) suggested that the observed diffuse stellar halo can be formed from destruction of a dwarf galaxy that previously contained NGC 1851. Given the presence of stellar streams associated with GCs in the Galaxy and M31 (e.g. Bellazzini et al. 2003; Mackey et al. 2010), the above suggestion seems to be quite reasonable.

Our previous numerical studies showed that nucleated dwarfs can be transformed into very massive GCs such as  $\omega$  Cen in the Galaxy (Bekki & Freeman 2003) and G1 in M31 (Bekki & Chiba 2004) or ultracompact dwarf galaxies (UCDs) in clusters of galaxies (Bekki et al. 2003). These studies demonstrated that if the orbits of nucleated dwarfs are highly radial, then strong tidal fields of galaxies and clusters of galaxies can strip almost all of the dark matter and field stars from nucleated dwarfs while the nuclei remain intact owing to their compactness. They thus claimed that the stripped nuclei of nucleated dwarfs can be observed as massive GCs or UCDs. Bekki et al. (2003) already showed that the stripped nuclei can be surrounded by diffuse stellar haloes that are composed of field stars left behind from the tidal destruction processes of the dwarfs (see their figs 2 and 3). However, they did not investigate the physical properties of the haloes around stripped nuclei, and their models for the formation of UCDs are unreasonable for the formation of NGC 1851, a system much less massive than UCDs. Numerical simulations on dwarf destruction process (e.g. Goerdt et al. 2008; Lokas et al. 2010) and nucleus formation from GC merging (e.g. Capuzzo-Dolcetta & Miocchi 2008a,b) did not discuss the origin of NGC 1851 either. Thus, it is unclear whether the observed stellar halo around NGC 1851 can be really formed from disruption of a nucleated dwarf interacting with the Galaxy.

The purpose of this paper is to explore whether the stellar halo around NGC 1851 can be formed as a result of the transformation of a nucleated dwarf into a GC by using numerical simulations on the long-term dynamical evolution of nucleated dwarfs around the Galaxy. We also investigate whether GC merging, which is suggested to be responsible for the formation of NGC 1851 (e.g. Carretta et al. 2010), can really occur in the central region of the host dwarf. In this paper, we adopt a scenario in which NGC 1851 was previously a stellar nucleus (or nuclear star cluster) that was formed *in situ* or through merging of two GCs with different chemical abundances. We mainly discuss (i) physical conditions for a nucleated dwarf to become NGC 1851; and (ii) time-scales of GC merging in NGC 1851's host dwarf . We also discuss how GC merging is important for the formation of GCs with abundance spreads in heavy elements, such as NGC 2419 and M22.

It should be stressed here that the present scenario is only one of possible ones. For example, Küpper et al. (2010) have recently showed that extra-tidal stellar populations can be formed as a result of tidal interaction of star clusters with their parent host galaxies. Although the present models are idealized and less realistic in some aspects (e.g. fixed Galactic potential and point-mass representation of GCs in dwarfs), we consider that the models enable us to grasp some essential ingredients of the formation of NGC 1851. Furthermore, none of the results presented makes any assumption on the ages and/or chemical compositions of the merging GCs. This study represents an important first step towards a fully self-consistent model for the formation of NGC 1851: a considerably more sophisticated theoretical model for both dynamical and chemical properties of NGC 1851 will be constructed in our future papers.

The plan of this paper is as follows. In the next section, we describe our numerical model for dynamical evolution of nucleated dwarfs around the Galaxy and for GC merging in dwarfs. In Section 3, we present the numerical results on the transformation of nucleated dwarfs into GCs during disruption of dwarfs by the Galaxy. In this section, we also discuss the time-scales of GC merging for different models. In Section 4, we provide important implications of the present results in terms of the origin of multiple stellar populations in GCs. We summarize our conclusions in Section 5. Note that we do not intend to discuss chemical properties of multiple stellar populations in NGC 1851 using some theoretical models: Ventura et al. (2009) have recently discussed C+N+O abundances of NGC 1851 using their models for asymptotic giant branch (AGB) stars. We do not discuss the possible connection between the formation of NGC 1851 and the evolution of Canis Major dwarf galaxy (e.g., Forbes & Bridge 2010) in the present paper.

# **2 THE MODEL**

### 2.1 A scenario

We consider that a nucleated dwarf galaxy is a host for NGC 1851 and was accreted on to the Galaxy at least several Gyr ago. Accordingly, the dwarf has been strongly influenced by the strong tidal field of the Galaxy so that it has been almost completely destroyed. The stripped nucleus (or nuclear star cluster) is now observed as one of the Galactic GCs, NGC 1851. The stellar nucleus of NGC 1851's host dwarf was formed by merging two GCs each of which has stellar populations with almost identical chemical abundances in  $\alpha$  and Fe-peak elements yet different ones in light elements (e.g. C, N and O) and *s*-process elements. The two clusters were formed in different regions of the dwarf such that they could have slightly different abundances in *s*-process (and heavier) elements. After the creation of a new GC by merging of the two GCs, the new GC could quickly sink into the nuclear region owing to its larger original mass (>5 × 10<sup>5</sup> M<sub>☉</sub>). The nucleus (NGC 1851) had two distinct populations with different abundances in *s*-process elements and slightly different ages, which reflects differences in formation epochs of the two GCs.

In this scenario, it is inevitable that NGC 1851 can currently contain field stars that were initially in the nuclear region of its host. It is, however, unclear how many stars can finally surround NGC 1851 after the destruction of its dwarf. It is highly likely that GC merging occurs in the host dwarf owing to a small velocity dispersion of the dwarf,  $\sim 10 \text{ km s}^{-1}$ . However, it is unclear whether the merged GCs can become a stellar nucleus or whether the merged GCs can be stripped from the host before it can sink into the nuclear region. We thus quantitatively estimate physical properties of the stellar halo around NGC 1851 and the time-scale of GCs, in this study.

# 2.2 Nucleated dwarf

A nucleated dwarf is modelled as a fully self-gravitating system and assumed to consist of a dark matter halo, a stellar component and a nucleus. The dark matter halo and the main stellar component of the dwarf are represented by collisionless *N*-body particles. In the present *N*-body simulations, the nucleus is represented by a single point-mass particle, because the inner structure of NGC 1851 (R < 10 pc) cannot be numerically resolved. Gas dynamics and star formation including new GC formation are not included in this study. For convenience, the stellar component (i.e. the main baryonic component) is referred to as either the 'envelope' or the 'stellar envelope' so that we can distinguish this component from the stellar nucleus.

The density profile of the dark matter halo with the total mass of  $M_{dm,dw}$  is represented by that proposed by Salucci & Burkert (2000):

$$\rho_{\rm dm}(r) = \frac{\rho_{\rm dm,0}}{(r+a_{\rm dm})(r^2+a_{\rm dm}^2)},\tag{1}$$

where  $\rho_{dm,0}$  and  $a_{dm}$  are the central dark matter density and the core (scale) radius, respectively. For convenience, we hereafter call this profile the 'SB' profile (or model). Recent observational and numerical studies have shown that the adopted 'cored dark matter' haloes are reasonable for describing dark matter distributions in low-mass galaxies (e.g. Governato et al. 2010; Oh et al. 2011). Therefore, the above SB profile rather than the 'NFW' one (Navarro, Frenk & White 1996) with a central cusp predicted by the cold dark matter model is better for the present model for low-mass nucleated dwarfs. For the SB profile, the dark matter core parameters,  $\rho_{dm,0}$ ,  $a_{dm}$  and  $M_0$  (where  $M_0$  is the total dark matter mass within  $a_{dm}$ ), are not free parameters, and clear correlations are observed between them (Burkert 1994):

$$M_0 = 4.3 \times 10^7 \left(\frac{a_{\rm dm}}{\rm kpc}\right)^{7/3} M_{\odot}.$$
 (2)

All dark matter particles are distributed within  $5a_{dm}$ , which can roughly correspond to the tidal radii of dwarfs ( $\sim$ 7 kpc) at the apocentre distance (=35 kpc) for the total masses of  $\sim$ 10<sup>9</sup> M<sub> $\odot$ </sub>.

The stellar component of the dwarf is modelled as a bulge-less stellar disc with the total mass of  $M_{s,dw}$  and the size of  $R_{s,dw}$ . The radial (*R*) and vertical (*Z*) density profiles of the stellar disc are assumed to be proportional to  $\exp(-R/R_0)$  with scalelength  $R_0 = 0.2R_{s,dw}$  and to  $\operatorname{sech}^2(Z/Z_0)$  with scalelength  $Z_0 = 0.04R_{s,dw}$ , respectively. In addition to the rotational velocity caused by the gravitational field of disc and dark halo components, the initial radial and

azimuthal velocity dispersions are assigned to the disc component according to the epicyclic theory with Toomre's parameter Q = 1.5. The vertical velocity dispersion at a given radius is set to be 0.5 times as large as the radial velocity dispersion at that point.

We investigate models with different  $M_{s,dw}$  and adopt Freeman's law (Freeman 1970) to determine  $R_0$  of a disc galaxy according to its disc mass:

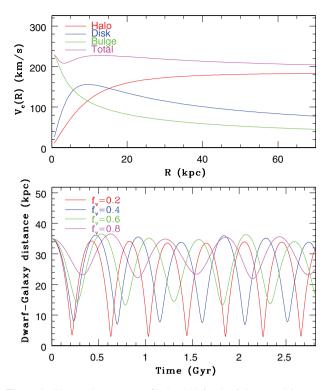
$$R_0 = C_{\rm d} \left( \frac{M_{\rm d}}{6 \times 10^{10} \,\rm M_{\odot}} \right)^{0.5} \,\rm kpc, \tag{3}$$

where  $C_d$  is a normalization constant. Although  $C_d = 3.5$  is a reasonable value for a luminous disc galaxy like the Galaxy, lowluminosity disc galaxies have low surface stellar densities and thus  $R_0$  determined by the above equation would not be so appropriate (i.e. significantly smaller than the observed), as shown in Kauffmann et al. (2003). We thus adopt  $C_d = 8.75$  for low-mass nucleated dwarfs for most models in this study. For the adopted mass–size scaling relation, a dwarf with  $M_{s,dw} = 10^8 \text{ M}_{\odot}$  has  $R_{s,dw} = 1.8 \text{ kpc}$  (stellar disc size) and  $R_0 = 0.36 \text{ kpc}$  (scalelength). We also investigate low surface brightness ('LSB') models in which  $C_d = 13.8$  and therefore dwarfs are classified as very low surface brightness galaxies. These LSB models are used for discussing the origin of the observed small mass (~ $10^3 \text{ M}_{\odot}$ ) of the stellar halo around NGC 1851. The ratio of  $M_{dm,dw}$  to  $M_{s,dw}$  is a free parameter represented by  $f_{dm}$ , though  $f_{dm} = 9$  for most models.

The spin of a stellar disc of the dwarf is specified by two angles  $\theta_d$  and  $\phi_d$  (degrees).  $\theta_d$  is the angle between the *z*-axis and the vector of the angular momentum of the disc.  $\phi_d$  is the azimuthal angle measured from the *x*-axis to the projection of the angular momentum vector of the disc on to the *x*-*y* plane, where the *x*-*y* plane is coincident with the Galactic plane. We have investigated models with different  $\theta_d$  and  $\phi_d$  for the orbits of the host dwarf of NGC 1851 adopted in the standard model (M1). We found that the present results on the formation processes of stellar haloes around stripped nuclei are essentially the same between the models. Thus, we describe the results of the models with  $\theta_d = 45^\circ$  and  $\phi_d = 30^\circ$ .

The stellar nucleus with a mass  $M_{n,dw}$  is represented by a pointmass particle that has a Plummer potential with a scaling length of  $a_{n,dw}$ . The value of  $a_{n,dw}$  is set to be the same as the gravitational softening length of the stellar nucleus particle, as described later. The ratio of  $M_{n,dw}$  to  $M_{s,dw}$  in a dwarf is a free parameter which is represented by  $f_n$  and ranges from  $10^{-4}$  to  $10^{-1}$ . We investigate models with vastly different  $f_n$ , because we need to clearly demonstrate how the formation processes of the stellar halo around NGC 1851 depend on  $f_n$ . Recent observations have shown that the typical ratio of  $M_{n,dw}$  to  $M_{s,dw}$  in brighter nucleated galaxies ( $M_B <$ -15 mag) is  $\sim 0.3$  per cent and there is a dispersion of 3.2 in  $f_n$  (Côté et al. 2006). Possibly,  $M_{s,dw}$  of nucleated dwarfs at high redshifts were significantly lower than those at present, because gas had not been completely converted into stars. Therefore, it is likely that  $f_n$ of ancient nucleated dwarfs that were accreted on to the Galaxy long time ago were significantly larger than 0.003. We therefore mainly investigate the models with  $f_n = 0.01$ . It should be noted that Georgiev et al. (2009) found bright ( $M_V \sim -9 \text{ mag}$ ) nuclear GCs in dwarf irregular galaxies, which could be progenitors of old Galactic GCs like NGC 1851.

In this paper, we do not discuss how the destruction processes of dwarfs depend on initial dark matter profiles of the dwarfs. This is because our previous simulations (Bekki et al. 2003) have already investigated dynamical evolution of dwarfs with cored (SB) and cuspy (NFW) dark matter haloes. They clearly demonstrated that if the NFW models are adopted, then the transformation of nucleated



**Figure 1.** The rotation curve profile  $[V_c(R)]$  for the Galaxy model (upper panel) and the time-evolution of the distance between a nucleated dwarf and the Galaxy for four representative models. The contributions from halo (red), disc (blue), bulge (green) and all components (magenta) are shown separately in the upper panel. The time-evolution dwarf–Galaxy distances for T < 2.8 Gyr are shown for models with  $f_v = 0.2$  (red), 0.2 (red), 0.4 (blue), 0.6 (green) and 0.8 (magenta) in the lower panel.

dwarfs into UCDs or massive GCs becomes much less likely. We thus consider that this previous result can be true for the formation of NGC 1851 from a nucleated dwarf.

#### 2.3 The Galaxy

The orbit of the dwarf is assumed to be influenced only by the *fixed* gravitational potential of the Galaxy having three components: a dark matter halo, a disc and a bulge. We assume the following logarithmic dark matter halo potential for the Galaxy:

$$\Phi_{\text{halo}} = v_{\text{halo}}^2 \ln(r^2 + d^2), \tag{4}$$

where d = 12 kpc,  $v_{halo} = 131.5$  km s<sup>-1</sup> and *r* is the distance from the centre of the Galaxy. The gravitational potential of the Galactic disc is represented by a Miyamoto & Nagai (1975) potential:

$$\Phi_{\rm disc} = -\frac{GM_{\rm disc}}{\sqrt{R^2 + (a + \sqrt{z^2 + b^2})^2}},$$
(5)

where  $M_{\text{disc}} = 1.0 \times 10^{11} \,\text{M}_{\odot}$ , and  $a = 6.5 \,\text{kpc}$ ,  $b = 0.26 \,\text{kpc}$  and  $R = \sqrt{x^2 + y^2}$ . The following spherical Hernquist (1990) model is adopted for the potential of the Galactic bulge:

$$\Phi_{\text{bulge}} = -\frac{GM_{\text{bulge}}}{r+c},\tag{6}$$

where  $M_{\text{bulge}} = 3.4 \times 10^{10} \,\text{M}_{\odot}$  and  $c = 0.7 \,\text{kpc}$ . These reasonable sets of parameters give a realistic rotation curve for the Galaxy with a maximum rotation speed of 224 km s<sup>-1</sup> at  $R = 8.5 \,\text{kpc}$ . Fig. 1 shows the rotation curve profile  $[V_c(R)]$  for the adopted model.

The centre of the Galaxy is always set to be (x, y, z) = (0,0,0), whereas the initial location and velocity of the dwarf are free parameters that can control the orbital evolution of the dwarf. The initial distance of the dwarf from the Galactic Centre and the velocity are represented by  $R_i$  and  $f_v v_c$ , respectively, where  $v_c$  is the circular velocity at  $R_i$ . The inclination angle between the initial orbital plane and the *x*–*z* plane (=Galactic disc plane) is denoted by  $\theta$ . Guided by previous studies of the orbital evolution of the Galactic GCs (Dinescu et al. 1997; Dinescu, Girard & van Altena 1999), we consider that  $R_i$ , which corresponds to the apocentre distance, equal to  $2R_{d,mw}$  (where  $R_{d,mw}$  is the stellar disc size of the Galaxy and is 17.5 kpc in this study),  $f_v = 0.4$  and  $\theta = 46.6^\circ$  are reasonable for the orbit of the dwarf. We, however, investigate models with different  $R_i$ ,  $f_v$  and  $\theta$  owing to some observational uncertainties in the proper motion of NGC 1851.

Therefore, the initial 3D position and velocity of the dwarf are set to be  $(x, y, z) = (R_i \cos \theta, 0, R_i \sin \theta)$  and  $(V_x, V_y, V_z) = (0, f_v v_c, 0)$ , respectively. Although we have investigated models with a variety of different  $R_i$ ,  $f_v$  and  $\theta$  for a given  $M_{s,dw}$  (and  $R_{s,dw}$ ), we mainly describe here the results of the 'standard model' with  $R_i = 35$  kpc and  $f_v = 0.4$ , and  $\theta = 46.6^\circ$ . Fig. 1 shows the orbit with respect to the Galaxy for four representative models with  $R_i = 35$  kpc,  $\theta =$  $46.6^\circ$ , and  $f_v = 0.2$ , 0.4, 0.6 and 0.8.

# 2.4 GC merging

Previous numerical simulations on GC evolution in *isolated* lowmass disc galaxies showed that GC merging in the central regions of the galaxies is possible (Bekki 2010a). GC-merging processes, however, have not been extensively investigated for NGC 1851's host dwarf *interacting with the Galaxy*. Therefore, we investigate whether GC merging can occur in dwarfs before the complete destruction of the dwarfs by the Galaxy using the models with GCs, though we focus mainly on the transformation processes of nucleated dwarfs into GCs in the models with no GCs described in Section 2.1. Two GCs are represented by point-mass particles with masses of  $m_{gc}$  and are referred to as GC1 and GC2. The initial distances of GC1 and GC2 from the centre of the host are denoted by  $r_1$  and  $r_2$ , respectively. The initial velocities of the GCs are chosen such that they are the same as those of disc-field stars that are closest to the GC particles.

We follow the orbital evolution of the GCs and investigate whether the GCs can satisfy the following two physical conditions of GC merging at each time-step: (i) the distance of the two GCs  $(R_{gc})$  is less than 10 pc; and (ii) the total energy  $(E_t)$  is less than 0. Here  $E_t = E_p + E_k$ , where  $E_p$  and  $E_k$  are the total potential energy and kinetic energy of a system composed *only* of the two GCs represented by point-mass particles, respectively. We estimate  $E_p$  and  $E_k$  based on  $m_{gc}$ , the distance between the two GCs  $(R_{gc})$ , and the velocity difference between GC1 and GC2  $(V_r)$  at each time-step. We consider that if the above two conditions are satisfied, then the two GCs are regarded as 'merged' and we thereby investigate the time-scale of the GC merging  $(t_m)$ . The initial locations of the two GCs are randomly chosen and the GCs are assumed to rotate around the host-dwarf-like disc-field stars.

We first run models in which dynamical evolution of dwarfs with two GCs is followed until the two GCs merge. For these models, we estimate the time-scale of GC merging for a given set of model parameters. We then run models in which merging of two GCs results in the formation of a new GC and the subsequent evolution of the GC in the dwarf is followed. For these models, the new GC just after the GC merging has the total mass of GC1 and GC2,

Model <sup>a</sup>	$M_{\rm s,dw}^{\ b}$	$R_{\rm s,dw}^{c}$	$f_{\rm dm}{}^d$	$f_n^{e}$	$R_i^f$	$f_v{}^g$	$m_{\rm gc}{}^h$	$r_1^{i}$	$r_2^{j}$	Comments
M1	1.0	1.8	9	$10^{-2}$	35.0	0.4	_	_	_	Standard model
M2	1.0	1.8	9	$10^{-2}$	35.0	0.2	-	-	-	More radial orbit
M3	1.0	1.8	9	$10^{-2}$	35.0	0.6	-	_	_	
M4	1.0	1.8	9	$10^{-2}$	35.0	0.8	-	-	-	
M5	1.0	1.8	9	$10^{-2}$	8.8	0.4	-	_	_	Smaller apocentre
M6	1.0	1.8	9	$10^{-2}$	17.5	0.4	-	-	-	
M7	1.0	1.8	9	$10^{-2}$	70.0	0.4	-	_	_	
M8	0.1	0.6	9	$10^{-2}$	35.0	0.4	-	_	_	Smaller dwarf mass
M9	0.5	1.3	9	$10^{-2}$	35.0	0.4	-	_	_	
M10	2.0	2.5	9	$10^{-2}$	35.0	0.4	_	_	_	
M11	1.0	1.8	9	$10^{-4}$	35.0	0.4	_	_	_	Less massive nucleus
M12	1.0	1.8	9	$10^{-3}$	35.0	0.4	_	_	_	
M13	1.0	1.8	9	$10^{-1}$	35.0	0.4	-	_	_	
M14	0.1	2.8	90	$5 \times 10^{-2}$	35.0	0.4	-	_	_	LSB
M15	0.1	2.8	90	$5 \times 10^{-2}$	35.0	0.2	_	_	_	
M16	0.1	0.6	9	$5 \times 10^{-2}$	35.0	0.4	-	_	_	
M17	0.1	0.6	9	$5 \times 10^{-2}$	35.0	0.2	_	_	_	
MG1	1.0	1.8	9	_	35.0	0.4	5.0	0.2	0.2	With two GCs
MG2	1.0	1.8	9	_	35.0	0.4	5.0	0.4	0.4	
MG3	1.0	1.8	9	_	35.0	0.4	5.0	0.8	0.8	
MG4	1.0	1.8	9	_	35.0	0.4	5.0	0.1	0.3	
MG5	1.0	1.8	9	_	35.0	0.4	5.0	0.1	0.5	
MG6	1.0	1.8	9	_	35.0	0.4	5.0	0.3	0.5	
MG7	1.0	1.8	9	_	35.0	0.4	0.2	0.2	0.2	
MG8	1.0	1.8	9	_	35.0	0.4	0.5	0.2	0.2	
MG9	1.0	1.8	9	_	35.0	0.4	2.0	0.2	0.2	
MGM1	1.0	1.8	9	_	35.0	0.4	5.0	0.2	0.2	GC merging
MGM2	1.0	1.8	9	_	35.0	0.4	5.0	0.1	0.4	
MGM3	1.0	1.8	9	_	35.0	0.4	5.0	0.4	0.4	
MGM4	1.0	1.8	9	_	35.0	0.4	0.2	0.2	0.2	
MGM5	1.0	1.8	9	-	35.0	0.4	0.5	0.2	0.2	
MGM6	1.0	1.8	9	_	35.0	0.4	2.0	0.2	0.2	
MGM7	0.1	2.8	90	-	35.0	0.4	5.0	0.2	0.2	LSB

 Table 1. Description of the model parameters for the representative models.

<sup>*a*</sup>GCs are not included in models M1–M17, whereas they are included in models MG1–MG9 and MGM1–MGM7. Merging of two GCs and the resultant formation of a new single GC are included only in models MGM1–MGM7.

<sup>b</sup>The total mass of a stellar envelope in a dwarf in units of  $10^8 \text{ M}_{\odot}$ .

<sup>c</sup>The initial size of a stellar disc in a dwarf in units of kpc.

<sup>*d*</sup>The ratio of  $M_{dm,dw}$  (dark matter mass) to  $M_{s,dw}$  in a dwarf.

<sup>*e*</sup> The ratio of  $M_{n,dw}$  (stellar nucleus mass) to  $M_{s,dw}$  in a dwarf.

<sup>*f*</sup>The initial distance of a dwarf from the centre of the Galaxy in units of kpc.

<sup>g</sup>The initial velocity of a dwarf is given by  $f_v v_c$ , where  $v_c$  is the circular velocity of the Galaxy at  $R = R_i$ .

<sup>*h*</sup>The mass of a GC in units of  $10^5 M_{\odot}$ .

<sup>*i*</sup>The initial distance of GC1 from the centre of its host dwarf in units of  $R_{s,dw}$ .

<sup>*j*</sup>The initial distance of GC2 from the centre of its host dwarf in units of  $R_{s,dw}$ .

and the position and velocity are exactly the same as those for the centre of mass of the original two GCs. Table 1 summarizes the parameters for 33 representative models for which the results are discussed in this paper. Models M1–M17 with no GCs are for investigating the dynamical evolution of nucleated dwarfs, whereas models MG1–MG9 are for estimating  $t_m$ . We investigate whether the merged GCs can sink into the nuclear region of their host dwarf and finally become stellar nuclei (or nuclear star clusters) by using models MG1–MGM7.

We primarily consider 'equal-mass' GC mergers, because this is consistent with some observations (e.g. Milone et al. 2008) which showed that the mass ratio of two subpopulations in NGC 1851 is 45:55. Han et al. (2009), however, suggested that the mass ratio is 75:25. The latest results by Milone et al. (2009) are slightly different from those by Milone et al. (2008) and more consistent with those by Han et al. (2009). Given these possibly different mass ratios derived from different observations, it would be important to investigate models in which two GCs have different initial masses. We consider that equal-mass GC merger models enable us to grasp essential ingredients of GC-merging processes in dwarfs interacting with the Galaxy. Thus, we briefly describe and discuss the results of the different initial GC mass models in Appendix A.

# 2.5 Simulation setup

In order to simulate the long-term dynamical evolution of nucleated dwarfs with and without GCs for  $\sim 11$  Gyr, we use the latest version of GRAPE (GRavity PipE, GRAPE-7), which is a special-purpose reconfigurable add-in card (attached to the PCI-X I/O slot of a computer) for gravitational dynamics (Sugimoto et al. 1990). We use our original GRAPE code (Bekki 2010a) which enables us to investigate both global dynamical evolution of galaxies and orbital evolution of GCs within them. The time-integration of the equation of motion is performed by using the second-order leap-frog method with a

time-step interval of ~0.01 $t_{dyn}$ , where  $t_{dyn}$  is the dynamical timescale of a host dwarf. The total number of particles for the dark matter ( $N_{dm}$ ) and the stellar envelope ( $N_s$ ) used in the standard model is 200 000 and 200 000, respectively. It takes about 86 CPU hours for us to run the above standard model using GRAPE-7 (model 300E). We have a limited amount of computation time for this study and we need to run at least ~100 models with different model parameters in the present investigation. We therefore consider that the total number of particles of 400 000 is reasonable (not numerically costly) that we can adopt for each model. We confirm that the results do not depend on *N* for  $N \ge 400 000$ .

The gravitational softening lengths ( $\epsilon$ ) for the dark matter particles and the stellar ones are denoted by  $\epsilon_{dm,dw}$  and  $\epsilon_{s,dw}$ , respectively. We determine  $\epsilon$  for each of these components based on the halfnumber radius of the particles. The softening lengths for GCs and nucleus particles are assumed to be the same as  $\epsilon_{s,dw}$ . We consider that when two different components interact gravitationally, the mean softening length for the two components is applied for the gravitational calculation. For example,  $\epsilon = (\epsilon_{dm,dw} + \epsilon_{s,dw})/2$ is used for gravitational interaction between dark matter particles and stellar ones in a dwarf. In the standard model,  $\epsilon_{dm,dw}$  and  $\epsilon_{s,dw}$ are set to be 128 and 20 pc, respectively. In the following, *T* in a simulation represents the time that has elapsed since the simulation started.

# **3 RESULTS**

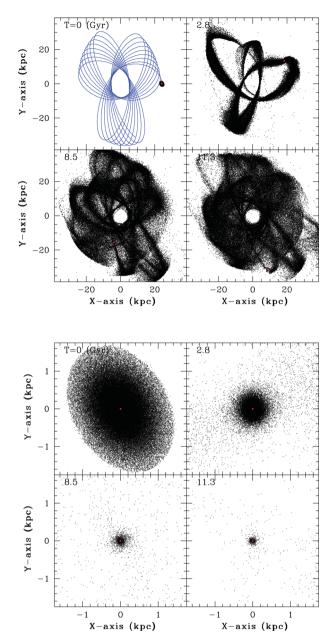
We first describe the formation processes of the stellar halo around NGC 1851 based on the results of the models (M1–M18) in which two GCs are not included, in Section 3.1. We then describe the results of the models with GCs (MG1–MG9), and those in which two GCs are allowed to merge with each other and thereby form new GCs (MGM1–MGM5), in Section 3.2.

#### 3.1 Stellar halo formation

#### 3.1.1 The standard model

Fig. 2 summarizes the orbital evolution of the nucleated dwarf around the Galaxy and the transformation processes of the dwarf to a naked nucleus (i.e. GC NGC 1851). As the dwarf passes by the pericentre distance, the stellar envelope of the dwarf is strongly influenced by the tidal field of the Galaxy so that stars in the dwarf can be efficiently stripped. As a result of this, the dwarf gradually loses its dark matter halo and stars, and the size of the stellar disc becomes significantly smaller (T = 2.8 Gyr). Although almost all of the dark matter has been tidally stripped from the dwarf by T =8.5 Gyr, a minor fraction of the disc-field stars may remain trapped by the gravitational potential of the stellar nucleus and thus surround the nucleus. Finally, the total mass of the dark matter halo and the stellar envelope within 200 pc from the nucleus becomes  $4.5 \times 10^3$ and  $3.3 \times 10^5 \,\mathrm{M_{\odot}}$ , respectively ( $T = 11.3 \,\mathrm{Gyr}$ ). The stars around the stripped stellar nucleus can be observed as a stellar halo around NGC 1851. The stripped stars can finally form numerous long tidal streams that follow the orbit of the dwarf.

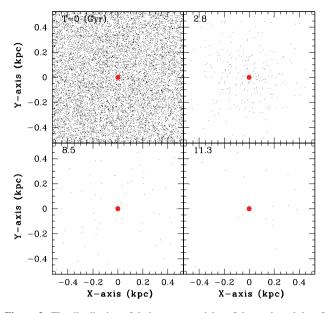
Fig. 3 clearly shows that the dark matter halo with the cored radial density profile can be efficiently stripped so that the total mass within the central 500 pc ( $M_{\rm dm,500\,pc}$ ) can decrease dramatically. As a result of this,  $M_{\rm dm,500\,pc}$  becomes 8.7 × 10<sup>5</sup>, 1.8 × 10<sup>4</sup> and 4.5 × 10<sup>3</sup> M<sub> $\odot$ </sub> at T = 2.8, 8.5 and 11.3 Gyr, respectively. The derived  $M_{\rm dm,500\,pc}$  means that the naked nucleus (=GC NGC 1851) is highly likely to be observed as a GC with no dark matter halo, though it



**Figure 2.** The time-evolution of the stellar distribution of a nucleated dwarf projected on to the x-y plane for a large scale (upper panel) and small scale (lower panel) in the standard model (M1). The centre of each frame is coincident with the Galactic Centre in the upper four plots and with the centre of the dwarf in the lower plots. The location of a nucleus particle is shown by a red big dot. The blue line in the upper left-hand plot of the upper panel describes the orbital evolution of the dwarf. The time *T* shown in the upper left-hand corner of each panel represents the elapsed time for this simulation.

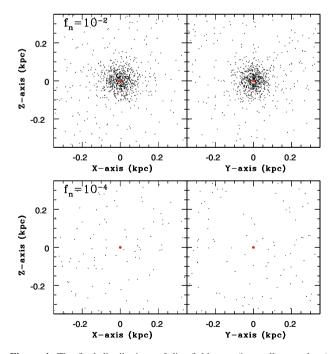
can have a tiny fraction of dark matter. Inspection of Figs 2 and 3 demonstrates that even if NGC 1851 is formed from the destruction of a nucleated dwarf embedded in a massive dark matter halo, it can have no/little dark matter within it. It should here be stressed that if the cuspy NFW dark matter halo is adopted for the model of a nucleated dwarf, then the dwarf is less likely to be destroyed by the tidal field of its host environment (see Bekki et al. 2003).

Fig. 4 shows the final distributions of the stellar haloes formed around the stripped nuclei for the standard model with  $f_n = 0.01$  and for the comparative model M5 with a less massive nucleus and

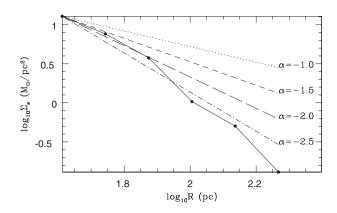


**Figure 3.** The distribution of dark matter particles of the nucleated dwarf projected on to the x-y plane at four representative time-steps for the standard model. The central big red particle represents the location of the stellar nucleus of the dwarf.

 $f_n = 10^{-4}$ . The stellar halo in the standard model shows a symmetric and spherical distribution with no tidal tails, whereas the stripped nucleus can hardly keep disc-field stars in model M5. This clear difference demonstrates that strong gravitational fields of stellar nuclei are important for the formation of stellar haloes around the nuclei during the destruction of nucleated dwarfs by the Galaxy. Fig. 5 shows that the projected density distribution of the stellar



**Figure 4.** The final distributions of disc-field stars (i.e. stellar envelope) around the stripped nuclei projected on to the *x*–*z* plane (left-hand panels) and the *y*–*z* one (right-hand panels) for the standard model (M1) with  $f_n = 10^{-2}$  (upper panels) and the comparative model (M5) with  $f_n = 10^{-4}$  (lower panels). The central big red particle represents the location of the stellar nuclei of the dwarfs.



**Figure 5.** The final projected radial density profile of the stellar halo around the stripped nucleus in the standard model (T = 11.3 Gyr). For comparison, the power-law density profiles with the slopes  $\alpha = -1.0$ , -1.5, -2.0 and -2.5 are shown by the dotted, short-dashed, long-dashed and dot-dashed lines, respectively. The best-fitting observational slope is -1.24 in the range 60–300 pc (Olszewski et al. 2009) and the observational data can also fit to the slopes of -0.58 and -1.9 within  $1\sigma$  errors.

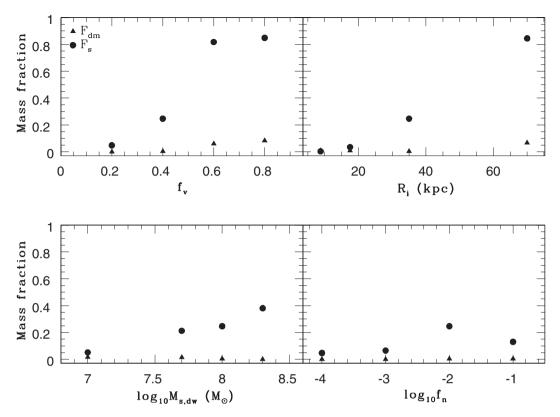
halo in the standard model can provide better fit to the power-law profile with the slope ( $\alpha$ ) of  $\sim -2$  for  $R \leq 80$  pc. The projected profile has a steeper profile ( $\alpha \sim -2.5$ ) in the outer part (80 < R < 250 pc) of the stripped nucleus: there is a significant difference between models and observations in the outer part of the halo. The derived  $\alpha$  is somewhat flatter in comparison with those derived by previous simulations in Küpper et al. (2010). The derived  $\alpha \sim -2$  for  $R \leq 80$  pc is slightly steeper than the observed  $\alpha \sim -1.24$  (Olszewski et al. 2009), though the observational results appear to fit to a range of values from  $\alpha \sim -2$  to -0.6 (1 $\sigma$  limits). The derived flat spatial distribution of the stellar halo in this study can be regarded as qualitatively similar to (yet slightly steeper than) those observed by Olszewski et al. (2009). Fine-tuning of the models could result in an improved fit.

#### 3.1.2 Parameter dependence

Whether or not nucleated dwarfs can be transformed into GCs (i.e. stripped nuclei) within ~10 Gyr depends strongly on  $R_i$  and  $f_v$  for a given  $M_{s,dw}$ . The ratios of dark matter masses to total masses (including dark matter, stellar envelopes and nuclei) within 200 pc of stripped nuclei ( $F_{dm}$ ) depend only weakly on model parameters. The mass ratios of stellar haloes around stripped nuclei ( $F_s$ ) are different in models with different  $M_{s,dw}$  and  $f_n$  (initial value) for a given orbit. In Fig. 6, we illustrate the derived dependences on model parameters. We find the following:

(i) The dwarfs in the models with larger  $f_v$  (=0.6 and 0.8) are much less strongly influenced by the Galaxy owing to the more circular orbits with larger pericentre distances. As a result of this, morphological transformation of nucleated dwarfs into GCs does not occur and  $f_n$  are large in these models. These results imply that highly radial orbits of the dwarfs are necessary for nucleated dwarfs to be transformed into GCs within ~10 Gyr. The models with lower  $f_v$  show smaller  $F_s$  and smaller total masses of stellar haloes around stripped nuclei ( $M_{halo}$ ). For example, the model with low  $f_v = 0.2$  shows a faint stellar halo with  $f_n = 0.05$  and  $M_{halo} = 5.1 \times 10^4 \, M_{\odot}$  around the stripped nuclei.

(ii) The models with  $R_i = 70$  kpc (i.e. large apocentre distances) do not show transformation of nucleated dwarfs into GCs for  $f_v = 0.4$  and  $M_{s,dw} = 10^8 M_{\odot}$ . This result suggests that GCs currently



**Figure 6.** The dependences of dark matter mass fractions ( $F_{dm}$ ; filled triangles) and stellar halo ones ( $F_s$ ; filled circles) in stripped nuclei on the velocity factor ( $f_v$ , upper left-hand panel), the initial distance of the dwarf from the Galactic Centre ( $R_i$ , upper right-hand panel), the initial stellar mass of the dwarf ( $M_{s,dw}$ , lower left-hand panel) and the initial nucleus mass fraction ( $f_n$ , lower right-hand panel). For each of these plots, only the indicated parameter (e.g.  $f_v$  in the upper left-hand panel) is changed, whereas other parameters are kept fixed.

located in the outer halo of the Galaxy ( $\sim$ 70 kpc) are less likely to be formed from nuclei of nucleated dwarfs. Both  $F_s$  and  $M_{halo}$  are smaller for models with smaller  $R_i$ . For example,  $f_n = 0.004$  and  $M_{halo} = 4.0 \times 10^3 \,\mathrm{M_{\odot}}$  in the model with  $R_i = 0.5$ . This suggests that if GCs originate from nuclei of nucleated dwarfs orbiting the inner regions of the Galaxy, the faint stellar haloes around GCs can be observationally difficult to detect separately from stars inside GCs.

(iii) Nucleated dwarfs with  $M_{s,dw} \le 2 \times 10^8 \,\mathrm{M_{\odot}}$  can be transformed into GCs for  $R_i = 35 \,\mathrm{kpc}$  and  $f_v = 0.4$ . The final  $f_n$  is larger for dwarfs with larger  $M_{s,dw}$ , because more massive nuclei in more massive dwarfs can trap a larger fraction of disc-field stars. These results imply that the most massive GCs will have higher surface brightness stellar haloes. Therefore, stellar haloes are more likely to be detected around the more massive GCs.

(iv) The models with larger  $f_n$  show larger  $F_s$  for  $f_n \le 0.01$ , because more massive nuclei can continue to trap their surrounding stars in their deeper gravitational potential wells during destruction of their host dwarfs. Although the model with  $f_n = 10^{-1}$  shows  $F_s$  slightly smaller than that in the model with  $f_n = 10^{-2}$ ,  $M_{halo}$  is larger in the model with  $f_n = 10^{-1}$  ( $M_{halo} = 1.5 \times 10^6 \,\mathrm{M_{\odot}}$ ). The models with  $f_n = 10^{-2}$  and  $10^{-3}$  show  $M_{halo} = 7.0 \times 10^3$  and  $5.1 \times 10^2 \,\mathrm{M_{\odot}}$ , respectively.

(v) The final  $M_{\rm halo}$  can be rather small in the LSB models with highly eccentric orbits, because larger fractions of stars in the dwarfs can be stripped by the tidal field of the Galaxy. For example, the LSB models with  $f_v = 0.4$  (M14) and 0.2 (M15) show  $M_{\rm halo} = 3.3 \times 10^4$  and  $4.2 \times 10^3 \, {\rm M_{\odot}}$ , respectively. The low-mass models ( $M_{\rm s,dw} = 10^7 \, {\rm M_{\odot}}$ ) with  $f_v = 0.4$  (M16) and 0.2 (M17) show  $M_{\rm halo} = 1.9 \times 10^4$ 

and  $2.1 \times 10^3 \,\mathrm{M_{\odot}}$ , respectively. As discussed later, these models can be in better agreement with the observationally estimated  $M_{\rm halo}$  in NGC 1851.

(vi) All models which show transformation of nucleated dwarfs into GCs show  $F_{\rm dm} < 0.01$ , which implies that if GCs originate from nuclei of dwarfs, they can have no/little dark matter within them. This is mainly because cored dark matter haloes are adopted in this study. The present results do not depend strongly on initial inclination angles of stellar discs ( $\theta_{\rm d}$  and  $\phi_{\rm d}$ ) in dwarfs.

### 3.2 GC merging within dwarfs

Fig. 7 shows the time-evolution of distances between GC1 (GC2) and its host dwarf (labelled as 'GC1–dwarf distance') and between GC1 and GC2 (labelled as 'GC1–GC2 distance') for model MG1 in which model parameters for the host are exactly the same as those adopted in the standard model M1. The formation of a new GC by merging of two GCs is *not* included in model MG1. Clearly, the two GCs can quickly sink into the nuclear region of the host owing to dynamical friction against disc-field stars so that they can finally be located within the central 100 pc. The GC1–GC2 distance can become well less than 100 pc within the first 1 Gyr of their evolution, though their distance is initially as large as  $\sim$ 500 pc.

Fig. 8 shows that as the two GCs get close to each other ( $R_{\rm gc}$  < 100 pc), both  $E_{\rm t}$  and  $V_{\rm r}$  become significantly smaller. The two GCs can have  $R_{\rm gc}$  < 10 pc and  $V_{\rm r}$  < 10 km s<sup>-1</sup> within the first ~1 Gyr so that they can have  $E_{\rm t}$  < 0: the two GCs are in a strongly bound orbit and can merge with each other to form a new GC in the central region of the host. Orbital evolution of GCs and merging processes

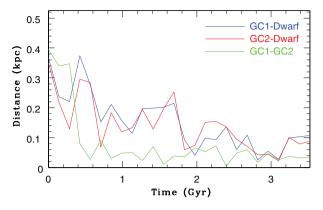
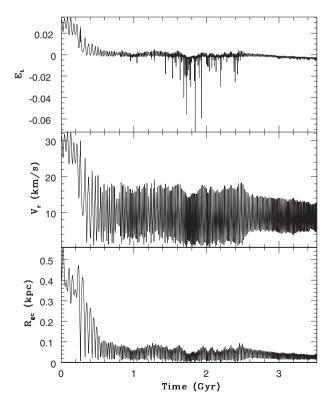
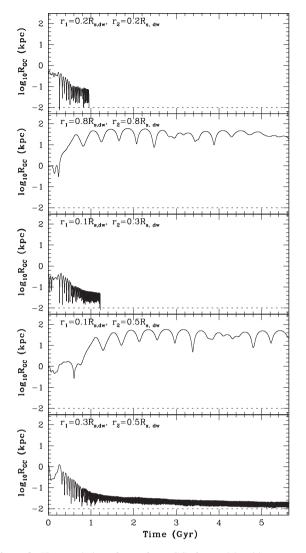


Figure 7. Time-evolution of distances between GC1 and its host dwarf (blue), GC2 and the dwarf (red), and GC1 and GC2 (green) in model MG1 with  $r_1 = r_2 = 0.2R_{s,dw}$ .

of two GCs depend strongly on where the GCs are born in the host. Fig. 9 shows the evolution of  $R_{GC}$  for different  $r_1$  and  $r_2$  and thereby describes when GC merging is possible in each model. It is clear that if  $r_1 = r_2$  and if  $r_1 \sim 0.2R_{s,dw}$ , then GC merging can occur in their host within ~1 Gyr for  $m_{gc} = 5 \times 10^5 M_{\odot}$ . GCs initially in the outer part of the host  $(r_1 \sim 0.8R_d)$  can be tidally stripped by the Galaxy so that they can finally become halo GCs: GC merging is highly unlikely for these GCs. Fig. 9 also shows that GCs with initially different  $r_1$  and  $r_2$  can merge within ~1 Gyr, as long as both  $r_1$  and  $r_2$  are smaller ( $\leq 0.3R_{s,dw}$ ). Such merging of GCs originating from different regions of their host could be responsible for the formation of GCs with abundance spreads in heavy elements, as discussed later.



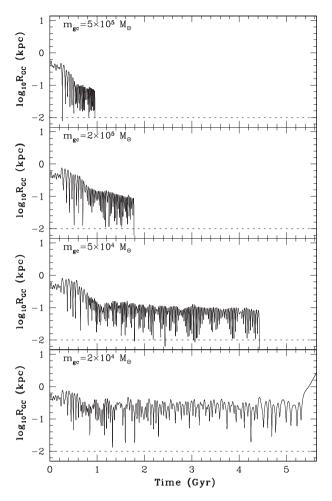
**Figure 8.** Time-evolution of the total energy of two GCs ( $E_t$ , top panel), the relative velocity ( $V_r$ , middle panel) and the mutual distance ( $R_{gc}$ , bottom panel) in model MG1.



**Figure 9.** Time-evolution of  $R_{gc}$  of two GCs for models with  $r_1 = r_2 = 0.2R_{s,dw}$  (top panel),  $r_1 = r_2 = 0.8R_{s,dw}$  (second panel from the top),  $r_1 = 0.1R_{s,dw}$  and  $r_2 = 0.3R_{s,dw}$  (third panel from the top),  $r_1 = 0.1R_{s,dw}$  and  $r_2 = 0.5R_{s,dw}$  (second panel from the bottom), and  $r_1 = 0.3R_{s,dw}$  and  $r_2 = 0.5R_{s,dw}$  (bottom panel). The  $R_{gc}$  evolution is shown for  $T < t_m$  in each model, where  $t_m$  is the time when two GCs merge.

Fig. 10 shows that the time-evolution of  $R_{gc}$  for two GCs depends strongly on  $m_{gc}$  for a given model of their host. The time-scale of GC merging is longer for smaller  $m_{gc}$ , because it takes a longer time for GCs with smaller  $m_{gc}$  to sink into their host's central region, where GC merging can occur: the time-scale of dynamical friction can be inversely proportional to  $m_{gc}$ . This means that GCs with smaller  $m_{gc}$  are more likely to be tidally stripped from their host by the Galactic tidal field before they merge with one another to become new GCs within the host. This also means that if the present GCs have multiple stellar populations with abundance spreads in heavy elements, they are likely to be quite massive GCs, in agreement with current observations.

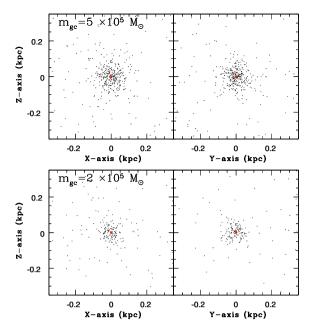
Fig. 11 shows the final distribution of stars around merged GCs in model MGM1 in which merging of GCs with  $m_{\rm gc} = 5 \times 10^5 \,{\rm M_{\odot}}$  and the evolution of merged GCs are included. For comparison, model MGM6 in which each of the two GCs has a smaller mass  $(m_{\rm gc} = 2 \times 10^5 \,{\rm M_{\odot}})$  is shown in Fig. 11. Although the two GCs in model MGM1 are initially in the central region of its host



**Figure 10.** The same as Fig. 9 but for models with different  $m_{gc}$ : 5 ×  $10^5 M_{\odot}$  (top panel), 2 ×  $10^5 M_{\odot}$  (second panel from the top), 5 ×  $10^4 M_{\odot}$  (second panel from the bottom) and 2 ×  $10^4 M_{\odot}$  (bottom panel)

 $(r_1 = r_2 = 0.2R_{s,dw})$ , they are initially not nuclear star clusters. While the host is being disrupted by the Galaxy, the two GCs can merge with each other and then sink into the nuclear region. The new cluster can finally become a new nuclear cluster (or a stellar galactic nucleus) surrounded by disc-field stars. After the complete disruption of the host, the naked nucleus can appear as a GC with a diffuse stellar halo. Although the numerical method for GC merging would be simplified in model MGM1, the results in Fig. 10 self-consistently demonstrate that NGC 1851 with a stellar halo can be formed as a result of GC merging in the central region of its host during the disruption of the host by the Galaxy.

The naked nucleus (i.e. merged GCs) has no dark matter and  $M_{\rm halo} = 1.5 \times 10^5 \,{\rm M_{\odot}}$ , which is smaller by a factor of ~3 than  $M_{\rm halo}$  derived for the standard model. Other models (MGM2–MGM5) with  $m_{\rm gc} \ge 5 \times 10^5 \,{\rm M_{\odot}}$  with different  $r_1$  and  $r_2$  show  $M_{\rm halo} \sim 10^5 \,{\rm M_{\odot}}$ . The final  $M_{\rm halo}$  around stripped nuclei depends on  $m_{\rm gc}$  such that  $M_{\rm halo}$  can be smaller in smaller  $m_{\rm gc}$ . Fig. 11 shows that the stellar halo appears to be more diffuse and compact in the model with  $m_{\rm gc} = 2 \times 10^5 \,{\rm M_{\odot}}$  ( $M_{\rm halo} = 6.9 \times 10^4 \,{\rm M_{\odot}}$ ). The final  $M_{\rm halo}$  depends on  $M_{\rm s,dw}$  and  $R_{\rm s,dw}$  such that  $M_{\rm halo}$  can be smaller in smaller  $M_{\rm s,dw}$  and larger  $R_{\rm s,dw}$ . For example, the LSB model MGM7 with  $M_{\rm s,dw} = 10^7 \,{\rm M_{\odot}}$  and  $R_{\rm s,dw} = 2.8 \,{\rm kpc}$  shows  $M_{\rm halo} = 2.7 \times 10^4 \,{\rm M_{\odot}}$ . Thus, we have demonstrated that the merging of two GCs with  $m_{\rm gc} \sim 5 \times 10^5 \,{\rm and} \, 2 \times 10^5 \,{\rm M_{\odot}}$  in a host dwarf could be the



**Figure 11.** The final distributions of disc-field stars (i.e. stellar envelope) around the merged GCs projected on to the *x*–*z* plane (left-hand panels) and the *y*–*z* one (right-hand panels) for model MGM1 with  $m_{gc} = 5 \times 10^5 \text{ M}_{\odot}$  (upper panels) and model MGM6 with  $m_{gc} = 2 \times 10^5 \text{ M}_{\odot}$  (lower panels). The central big red particle represents the location of the merged GC in each model.

progenitor for NGC 1851. We reiterate that these simulations, and therefore results, make no assumption on the ages and/or chemical abundances of the two merging GCs. If two GCs have slightly different ages and *s*-process abundances, then the merged GC can show chemical abundances consistent with the NGC 1851 observations. We have so far assumed that massive progenitor GCs could be formed in the early history of the host with a smaller mass of  $\sim 10^9 \text{ M}_{\odot}$ . It is not observationally clear whether such massive GCs can form in a dwarf galaxy at a high redshift. However, Georgiev et al. (2009) found that old massive GC sexist in the present-day dwarfs, which implies that massive GC formation could be possible in high-redshift dwarfs. In a future study, we plan to investigate whether two GCs with different ages and chemical abundances can be formed in a dwarf interacting with the Galaxy, using more so-phisticated chemodynamical simulations.

# **4 DISCUSSION**

# 4.1 The total mass and stellar populations of the stellar halo around NGC 1851

This study did not consider the evolution of individual stars with different masses through supernova explosion and mass-loss in evolved stars. Therefore, the derived  $M_{halo}$  in NGC 1851 in simulations corresponds to the initial total mass of the stellar halo around NGC 1851 (not the present mass). Olszewski et al. (2009) estimated  $M_{halo}$  (~500 M<sub>☉</sub>) by assuming that the typical mass of the observed main-sequence stars in the halo around NGC 1851 is  $0.5 M_{\odot}$ . In order to make a more self-consistent comparison between the observed and simulated  $M_{halo}$ , we here estimate the mass fraction ( $F_{main}$ ) of main-sequence stars with masses ranging from  $m_{m,l}$  (lower mass cut-off for the observed main-sequence stars) to  $m_{m,u}$  (upper mass cut-off) in a stellar population. Only stars brighter

than V = 25 mag are observed in Olszewski et al. (2009), and V = 25 mag corresponds to  $\sim 0.45 \,\mathrm{M_{\odot}}$  ( $\sim 0.41 \,\mathrm{M_{\odot}}$ ) for [Fe/H] = -0.9 and [ $\alpha$ /Fe] = 0.3 ([Fe/H] = -1.5 and [ $\alpha$ /Fe] = 0.3) if the Yonsei-Yale isochrones for an age of 10 Gyr are adopted. Therefore, fainter stars with masses significantly smaller than 0.45 M<sub> $\odot$ </sub> would not be included in the observational estimation of  $M_{\rm halo}$ . We here estimate  $F_{\rm main}$  for different  $m_{\rm m,1}$  and a fixed  $m_{\rm m,u}$  (=0.5 M<sub> $\odot$ </sub>). We adopt an IMF with a slope of  $\alpha_{\rm imf}$ , a lower mass cut-off of 0.1M<sub> $\odot$ </sub> and an upper mass cut-off of 100 M<sub> $\odot$ </sub>.

If we adopt  $\alpha_{imf} = -2.35$  (i.e. canonical Salpeter IMF), then  $F_{\text{main}} = 0.24$  for  $m_{\text{m},1} = 0.2 \,\text{M}_{\odot}$  and  $F_{\text{main}} = 0.05$  for  $m_{\text{m},1} =$  $0.4 \,\mathrm{M_{\odot}}$ . If  $m_{\mathrm{m,u}} = 0.4 \,\mathrm{M_{\odot}}$ , then  $F_{\mathrm{main}}$  is 0.19 for  $m_{\mathrm{m,l}} = 0.2 \,\mathrm{M_{\odot}}$ , which means that  $F_{\text{main}}$  does not depend so strongly on  $m_{\text{m,u}}$  for a reasonable range in  $m_{m,u}$ . If we adopt a top-heavy IMF with  $\alpha_{imf} =$ -1.35, then  $F_{\text{main}} = 0.014$  for  $m_{\text{m,l}} = 0.2 \text{ M}_{\odot}$  and  $F_{\text{main}} = 0.004$ for  $m_{\rm m,l} = 0.4 \,\mathrm{M_{\odot}}$ . The initial total mass of the stellar halo around NGC 1851 is the observed  $M_{halo}$  divided by  $F_{main}$ . Therefore, the initial halo mass is  $2.0 \times 10^3 \,\mathrm{M_{\odot}}$  for  $\alpha_{\rm imf} = -2.35$  (i.e. canonical Salpeter IMF) and  $m_{\rm m,l} = 0.2 \,\rm M_{\odot}$  and is  $1.0 \times 10^4 \,\rm M_{\odot}$  for  $\alpha_{\rm imf} =$ -2.35 and  $m_{m,l} = 0.4 \text{ M}_{\odot}$ . For a top-heavy IMF with  $\alpha_{imf} = -1.35$ and  $m_{\rm m,l} = 0.4 \,\mathrm{M_{\odot}}$ , the initial halo mass can be as large as  $\sim 1.3 \times$  $10^5 \,\mathrm{M_{\odot}}$ . If we adopt a rather shallow IMF slope (-1.3) for stellar masses of 0.08–0.5 M<sub>O</sub> in Kroupa's IMF, the initial halo mass can be significantly larger than those derived for the above canonical IMFs. The present models that have a canonical mass-size relation (i.e.  $C_d = 8.75$ ) and show the formation of naked nuclei have shown  $M_{\text{halo}}$  of (0.5–3.3) × 10<sup>5</sup> M<sub>☉</sub> for  $M_{\text{s,dw}} = 10^8 \text{ M}_{\odot}$ ,  $M_{\text{n}} = 10^6 \text{ M}_{\odot}$ (or  $f_n = 0.01$ ),  $R_i = 35$  kpc and  $f_v \le 0.4$ . In this study, only the LSB models (i.e.  $C_{\rm d} = 13.8$ ) with  $M_{\rm s,dw} = 10^7 \,\rm M_{\odot}, M_{\rm n} = 5 \times 10^5 \,\rm M_{\odot}$ (or  $f_n = 0.05$ ),  $R_i = 35$  kpc and  $f_v = 0.2$  have shown  $M_{halo}$  that can be as small as the above possible minimum initial mass (=2.0  $\times$  $10^3 \,\mathrm{M_{\odot}}$ ) of the stellar halo around NGC 1851. For example, the LSB model M14 with  $M_{s,dw} = 10^7 M_{\odot}, f_n = 0.005, R_{s,dw} = 2.8 \text{ kpc}$ and  $R_i = 35$  kpc, and  $f_v = 0.2$  shows  $M_{halo} = 4.2 \times 10^3$  M<sub>☉</sub>. These results suggest that if NGC 1851 originates from a stellar nucleus of a host dwarf, then the dwarf needs to have a very low surface brightness (or 'darker') galaxy and a highly eccentric orbit ( $e \sim$ 0.8) to explain the observed small  $M_{halo}$ . Such dwarf galaxies with highly eccentric orbits in a galaxy-scale halo can be seen in recent cosmological N-body simulations (e.g. Wetzel 2011).

GC merging can form diffuse stellar haloes around the remnant GCs (see fig. 1 in Bekki et al. 2004). If the remnants of GC mergers can sink into nuclear regions of their hosts and finally become stellar nuclei (or nuclear star clusters), then the merged GCs can trap surrounding field stars only after they become nuclear GCs, as shown in this study. Therefore, if nucleated dwarfs are transformed into GCs by tidal destruction of the dwarfs by the Galaxy, then the final GCs are likely to contain at least three different stellar populations with different abundances in heavy elements: two are from the original two GCs that merged with each other and the remaining one is from field stars surrounding stellar nuclei. If two GCs that are progenitors for NGC 1851 were formed in the nuclear region of their host, then there would be small differences in abundances in heavy elements between the two GCs and stars in the nuclear region. If this is the case, then the possible three stellar populations in the stellar halo (and NGC 1851 itself) would not show abundance spreads in heavy elements. Olszewski et al. (2009) already revealed two stellar populations in the colour-magnitude diagram of stars in the halo of NGC 1851, though they did not discuss the presence of the third population. We suggest that GC merging and trapping field stars by a stellar nucleus in NGC 1851's host dwarf can be responsible for the origin of the observed possible multiple populations in the halo around NGC 1851.

# 4.2 Other possible formation mechanisms for stellar halo formation around GCs

Although we have suggested that diffuse stellar haloes around GCs are fossil evidence for the formation of GCs in the central regions of nucleated dwarfs, there could be other formation mechanisms for the haloes. Recent theoretical studies on the origin of multiple stellar populations in GCs have shown that (i) GCs were originally much more massive than the present GCs; (ii) GCs originally have two generations of stars with the second generation (SG) being formed from gas from AGB or massive stars of the first generation (FG); and (iii) the FG of stars have more extended stellar distributions (e.g. D'Ercole et al. 2008; Bekki 2010b, 2011). They have shown that FG stars with much more extended distributions ( $R \sim 200 \text{pc}$ ) can be stripped quite efficiently by the tidal field of the Galaxy (D'Ercole et al. 2008) and by the host dwarf galaxy (Bekki 2011). During the tidal stripping, the faint FG population could be regarded as stellar haloes around the more compact SGs of stars. Therefore, it is possible that the observed diffuse stellar halo of NGC 1851 was stars that initially belonged to the FG of an originally massive GC. If this is the case, then the halo should have stars with chemical abundances consistent with those of the FG (e.g. N-normal, Cnormal stars), predicted in the above theoretical studies.

This 'FG scenario' would have some potential problems as follows. First, it is unclear why only some of GCs have been so far observed to have diffuse stellar haloes around them (though this could be due to an observational bias). In other words, it is unclear why FG stars have been completely stripped for most GCs but not for NGC 1851. Some GCs like NGC 1851 would be massive enough to keep FG stars against tidal stripping of the stars by the Galaxy. Secondly, given the predicted short time-scale (<a few Gyr) of stripping of FG stars (D'Ercole et al. 2008; Bekki 2011), it would be hard to understand how a significant fraction of FG stars have continued to surround NGC 1851 for more than 10 Gyr. The observed extension ( $\sim$ 500 pc) and radial density profile of the halo would be difficult to be explained by the FG scenario, which is based on a nested cluster with a size of  $\sim 100$  pc. Thus, it is possible, yet unlikely, that the FG scenario can self-consistently explain the observed properties of the stellar halo around NGC 1851. As discussed by Olszewski et al. (2009), the lack of tidal tails within  $\sim$ 500 pc from the centre of NGC 1851 is inconsistent with a scenario in which the halo stars originate from stars stripped from NGC 1851 itself. The rather steep profiles of the stripped stars from GCs in Küpper et al. (2010) imply that the stellar halo of NGC 1851 is unlikely to originate from NGC 1851 itself.

If NGC 1851 really originates from a stellar nucleus of a defunct dwarf galaxy, and if the nucleus was formed *in situ*, then chemical abundances of the diffuse stellar halo around NGC 1851 should be similar to those of stars currently within NGC 1851. If the nucleus was formed from merging of two GCs that were initially located in the central regions of the host dwarf, then there could be some differences in chemical abundances between NGC 1851 and its stellar halo. The abundance differences would depend on both where GCs were formed within the host dwarf and the radial abundance gradient within the dwarf. Thus, future spectroscopic observations on chemical abundances of the stellar halo around NGC 1851 will provide important constraints on the origin of the stellar halo.

# **4.3** Radial metallicity gradients of dwarfs as an origin of dispersions in heavier elements of GCs

For GC merging to be really responsible for two distinct stellar populations with different chemical abundances, the host dwarf needs to have a radial metallicity gradient, because merger progenitor GCs are highly likely to form at different radii within the dwarf. Recent observations have revealed that nearby dwarf ellipticals (Crnojević, Grebel & Koch 2010) and dwarf spirals (Hidalgo-Gámez, Ramirez-Fuentes & Gonzalez 2010) have negative abundance gradients in [Fe/H] and oxygen with  $\sim -0.2$  dex kpc<sup>-1</sup>, though it is unclear whether there are also age gradients in these galaxies. Two GCs with different  $r_1$  and  $r_2$  (distances from the centre of their host) in the present standard model can quickly merge with each other to form a new GC, if both  $r_1$  and  $r_2$  are less than ~500 pc. This means that if the host dwarf has a radial abundance gradient similar to the above observed one, then NGC 1851 formed from GC merging is expected to have a spread in [Fe/H]  $\sim -0.1$  dex. Recently, Carretta et al. (2010) have reported the presence of a dispersion in [Fe/H] ( $\sigma$  $\sim 0.07$ ) between the two distinct stellar populations in NGC 1851. The similarity between the expected  $\sigma$  from GC merging and the observed one implies that the observed dispersion (Carretta et al. 2010) could be due to the radial metallicity gradient of the defunct host dwarf of NGC 1851. Thus, we suggest that if GC merging is a key formation process of GCs, then the radial metallicity gradients of their host dwarf can determine to what extent the merged GCs can show abundance spreads in heavier elements. It should be stressed that two merging GCs are likely to form at different epochs in their host dwarf and thus the observed two subpopulations of NGC 1851 could have different ages, and thus different chemical enrichment histories.

Recent observational studies have revealed that some of the Galactic GCs (e.g. NGC 2419 and M22) show small yet real spreads in heavier elements (e.g. Da Costa et al. 2009; Marino et al. 2009, 2011; Cohen et al. 2010). The origin of the observed spread in NGC 2419 is suggested to be due to a massive host galaxy that previously contained NGC 2419 in its centre and could retain stellar ejecta from supernovae for further star formation (Cohen et al. 2010). This study suggests that host dwarf galaxies are important for the formation of these GCs, because (i) low velocity dispersions of the dwarfs allow GCs to merge quickly; and (ii) there can be GCs that form in different regions within dwarfs and thus have different chemical abundances. Massive dark matter haloes surrounding the host dwarfs would have played a vital role in retaining stellar ejecta from massive OB stars and supernovae and thus in forming stars with different chemical abundances in different regions. As shown in our previous simulations (Bekki et al. 2003; Bekki & Freeman 2003; Bekki & Chiba 2004), dark matter haloes of dwarfs can be almost completely stripped by their environments during transformation of nucleated dwarfs into GCs and UCDs. Thus, although dark matter haloes of dwarfs would have played a decisive role in the formation of GCs with abundance spreads in heavy elements (e.g. NGC 2419), they are very hard to be detected in GCs directly by observations.

# **5** CONCLUSIONS

We have numerically investigated (i) the dynamical evolution of nucleated dwarfs orbiting around the Galaxy; and (ii) the merging of two GCs in dwarfs in order to understand the entire formation history of NGC 1851. NGC 1851's host galaxy is modelled as a small bulge-less disc galaxy that has a stellar nucleus (or nuclear star cluster) and is embedded in a cored dark matter halo. The host is assumed to have two GCs represented by point-mass particles in some models so that physical processes of GC merging can be investigated in detail. The main results are summarized as follows:

(1) The host dwarf disc galaxy of NGC 1851 can be almost completely destroyed within ~10 Gyr by the strong tidal field of the Galaxy for a reasonable orbital model of the dwarf. Although the dark matter halo and the stellar disc of the dwarf can be almost completely stripped from the dwarf, a tiny fraction of the disc-field stars can remain trapped by the nucleus. As a result of this, the stripped nucleus and the surrounding field stars can be observed as a GC and its LSB stellar halo, respectively. The mass fraction of dark matter ( $F_{\rm dm}$ ) in NGC 1851 is typically less than 10<sup>-2</sup>, which means that NGC 1851 can have little dark matter even if it originates from the central region of a dwarf galaxy dominated by dark matter.

(2) The simulated stellar halo around NGC 1851 has a symmetric and spherical distribution within 200 pc from the centre of NGC 1851. The halo does not show tidal tails and it has a projected radial density profile with the power-law slope  $\alpha$  of  $\sim$ -2 in the inner 80 pc and steepens beyond that radius. The derived slope is steeper than the best-fitting one in observations ( $\sim$ -1.2), though the observational data can also fit to  $\alpha \sim$  -0.58 and  $\sim$ -1.9 within the 1 $\sigma$  errors. The mass fraction of the halo ( $F_s$ ) is typically  $\sim$ 0.1 and depends strongly on  $R_i, f_v$  and  $M_{s,dw}$ .  $F_s$  can be as small as  $10^{-3}$ (or  $M_{halo} \sim 10^3 \text{ M}_{\odot}$ ) in LSB models. These results imply that the observed mass fraction of the diffuse stellar halo around NGC 1851 can give constraints on the orbit and the mass/size of the defunct host dwarf.

(3) For NGC 1851's host dwarf to be transformed into a GC with a stellar halo within ~10 Gyr, the host needs to have certain ranges of  $R_i$  and  $f_v$  for a given  $M_{s,dw}$ . For example, models with  $f_v \ge 0.6$  for  $R_i = 2R_{d,mw}$  do not show naked nuclei that can be observed as NGC 1851, whereas the models with  $f_v \le 0.2$  show fainter stellar haloes ( $F_s \ll 0.1$ ). Also, the nucleated dwarfs in the models with  $R_i \ge 4R_{d,mw}$  cannot be destroyed by the Galactic tidal field for  $0.2 \le f_v \le 0.8$ .

(4) Two equal-mass GCs initially in NGC 1851's host dwarf can merge with each other to form a new GC in the central region of the host within  $\sim 1$  Gyr, if each of the two GCs has a mass of  $\sim 5 \times 10^5 \,\mathrm{M_{\odot}}$  and if they are located at  $R \approx 0.2 R_{\rm s,dw}$ . Merging between two GCs (GC1 and GC2) with different initial distances from the host's centre ( $r_1$  and  $r_2$ , respectively) can occur within a few Gyr, though the time-scale of GC merging depends strongly on  $r_1$  and  $r_2$  for a given  $m_{gc}$ . GC merging with different initial GC masses can also occur within  $\sim 1$  Gyr if the total mass of the two GCs is as large as  $10^6 \,\mathrm{M_{\odot}}$ . The merging time-scale of two GCs can be significantly longer than  $\sim$ 1 Gyr for rather small GC mass ratios (<0.05). Given that interstellar gas at different R might well have different chemical abundances in the host (owing to a possible radial metallicity gradient), these results imply that the observed abundance spreads in s-process elements for NGC 1851 can be closely associated with GC merging in the central region of the host.

(5) Merged GCs can quickly sink into the central region of its host owing to dynamical friction and finally become a nuclear star cluster (or stellar nucleus) surrounded by disc-field stars. However, not all merged GCs can become nuclear clusters surrounded by field stars. Merged GCs with low masses cannot continue to trap field stars in their gravitational potentials owing to their low masses, even if they become nuclear clusters. These imply that not all of GCs that were formed from GC merging within their host dwarfs can show diffuse stellar haloes.

(6) GCs initially located in the outer regions of the host dwarf  $(R > 0.6R_{s,dw})$  and those with lower masses  $(m_{gc} < 5 \times 10^4 \text{ M}_{\odot})$  are more likely to be stripped to become the Galactic halo GCs without GC merging during the orbital evolution of the host. Only more massive GCs formed initially in the inner regions of the host can merge with each other to become nuclear GCs (i.e. stellar nuclei) before the host can be completely destroyed by the Galactic tidal field. These results imply that more massive GCs are more likely to show abundance spreads even in *s*-process and heavy elements.

(7) If NGC 1851 originates from the stellar nucleus of a host dwarf, and if the nucleus was formed from GC merging, the stellar halo is highly likely to contain at least three different stellar populations with different heavy and *s*-process elements. The three populations are from two GCs and field stars in the nuclear region of the host dwarf. The host needs to be a dwarf with a very low surface brightness ( $M_{s,dw} \sim 10^7 \, M_{\odot}$  and  $R_{s,dw} \sim 1 \, \text{kpc}$ ) and a highly eccentric orbit ( $e \sim 0.8$ ), if the total mass of the stellar halo around NGC 1851 is  $\sim 10^3 \, M_{\odot}$ .

Thus, we have demonstrated that transformation of nucleated dwarfs into GCs, GC merging within dwarfs, and nucleus formation by GC merging are all possible in a self-consistent manner. This study suggests that the formation processes of NGC 1851 are different from those of normal GCs in the following two ways: (i) it experienced GC merging; and (ii) it was once located in the nuclear region of its host dwarf. This study suggests that some of the Galactic GCs, such as NGC 5694 with a diffuse stellar halo, can be formed in a similar way to NGC 1851. Furthermore, this study predicts that a larger fraction of GCs at higher redshifts could have diffuse stellar haloes, if GCs originate from nuclei of dwarfs. Dispersions in heavier elements observed in some GCs (e.g. NGC 2419 and M22) can be closely associated with radial metallicity gradients of dwarfs, where GC merging is possible. GC merging, however, could be important for GC formation processes only for a minor fraction of GCs, and other physical processes such as secondary star formation from AGB ejecta (D'Ercole et al. 2008), capture of diffuse interstellar gas and molecular gas for secondary star formation (Bekki & Mackey 2009; Pflamm-Altenburg & Kroupa 2009), and gas fuelling to nuclei of nucleated dwarfs (Bekki & Freeman 2003) could also be important for GCs with multiple stellar populations. We plan to extensively discuss the relative importance of these physical processes in the formation of GCs with different degrees of abundance inhomogeneity in our future papers.

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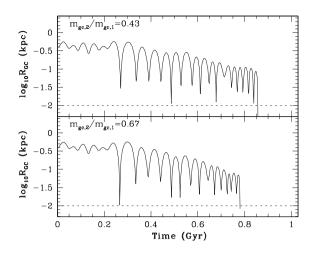
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# APPENDIX A: MERGING OF GLOBULAR CLUSTERS WITH DIFFERENT MASSES

We investigate whether and how GC merging can occur for models in which the two GCs have different initial masses. We here consider that (i) the models for the host dwarf of NGC 1851 and its orbital evolution are the same as the standard model; (ii) the total mass of two GCs is fixed at  $10^6 M_{\odot}$ ; and (iii) the initial masses of GC1 and GC2 ( $m_{gc,1}$  and  $m_{gc,2}$ , respectively) are free parameters. Fig. A 1 shows the model in which  $r_1 = r_2 = 0.2R_{s,dw}$ , and  $m_{gc,1}$  and  $m_{gc,2}$ are  $7 \times 10^5$  and  $3 \times 10^5 M_{\odot}$ , respectively. The adopted mass ratio (~0.43) of the two GCs is consistent with the observed mass ratio of two subpopulations in NGC 1851 by Han et al. (2009). Clearly, two GCs with different masses can merge within ~1 Gyr in this model, and the merging time-scale is quite similar to that derived for equal-mass GC models (shown in Fig. 9). Fig. A1 also shows that two GCs can merge within ~1 Gyr for the model with  $m_{gc,1}$  and



**Figure A1.** The same as Fig. 9 but for the GC merger models with the GC mass ratio of 0.43 (upper panel,  $m_{gc,1} = 7 \times 10^5 \,\mathrm{M_{\odot}}$  and  $m_{gc,2} = 3 \times 10^5 \,\mathrm{M_{\odot}}$ ) and with the GC mass ratio of 0.67 (lower panel,  $m_{gc,1} = 6 \times 10^5 \,\mathrm{M_{\odot}}$  and  $m_{gc,2} = 4 \times 10^5 \,\mathrm{M_{\odot}}$ ). Here  $r_1 = r_2 = 0.2R_{s,dw}$  and the models for the dwarf and its orbit around the Galaxy are the same as those adopted in the standard model.

 $m_{\text{gc},2}$  being 6 × 10<sup>5</sup> and 4 × 10<sup>5</sup> M<sub> $\odot$ </sub>, respectively. These results strongly suggest that GC merging is highly likely in the host dwarf of NGC 1851, if GC masses are larger than  $\sim 3 \times 10^5 M_{\odot}$ .

It should be stressed that if the mass ratio of two GCs is less than 0.05, then the time-scale of GC merging can become significantly longer than ~1 Gyr (for  $r_1 = r_2 = 0.2R_{s,dw}$ ): GC merging before dwarf destruction becomes less likely for rather small GC mass ratios. This is mainly because one of the two GCs has a small mass ( $<5 \times 10^4 M_{\odot}$ ) so that the dynamical friction time-scale of the GC can become rather large (i.e. cannot sink rapidly into the nuclear region of the host dwarf). This result suggests that the observed mass ratio of two subpopulations in NGC 1851 should not be so small (<0.05), if NGC 1851 is a merger remnant of two GCs with different masses. Indeed, the observed range for the possible mass ratio of two subpopulations (Milone et al. 2008, 2009; Han et al. 2009; Caretta et al. 2010) is consistent with the above result.

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