First-excited state g factors in the stable, even Ge and Se isotopes

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Transient-field g-factor measurements in inverse kinematics were performed for the first-excited states of the stable, even isotopes of Ge and Se. The g factors of 74 Ge and 74 Se were measured simultaneously using a cocktail beam, which eliminates most possible sources of systematic error in a relative g-factor measurement. The results are $g(^{74}\text{Se})/g(^{74}\text{Ge}) = 1.34(7)$, $g(^{70}\text{Ge})/g(^{74}\text{Ge}) = 1.16(15)$, $g(^{72}\text{Ge})/g(^{74}\text{Ge}) = 0.92(13)$, $g(^{76}\text{Ge})/g(^{74}\text{Ge}) = 0.88(5), g(^{76}\text{Se})/g(^{74}\text{Se}) = 0.96(7), g(^{78}\text{Se})/g(^{74}\text{Se}) = 0.82(5), g(^{80}\text{Se})/g(^{74}\text{Se}) = 0.99(7),$ and $g(^{82}Se)/g(^{74}Se) = 1.19(6)$. The measured g-factor ratios are in agreement with ratios from previous measurements, despite considerable variation in previous reported absolute values. The absolute values of the g factors remain uncertain, however, the Rutgers parametrization was used to set the transient-field strength and then compare the experimental g factors with shell-model calculations based on the JUN45 and ji44b interactions. Modest agreement was found between experiment and theory for both interactions. The shell-model calculations indicate that the $g(2_1^+)$ values and trends are determined largely by the balance of the spin carried by orbital motion of the protons.

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I. INTRODUCTION

A. Background and motivation

The Ge and Se isotope chains are of interest as they span the $A \approx 70$ shape coexistence region [1–5], exhibiting an interplay between single-particle and collective excitations, and shape changes [2,5-7]. A microscopic understanding of the structure of these nuclei, through validated shell-model calculations, is desirable. These nuclei have recently become amenable to large-basis shell-model calculations [8,9] utilizing a ⁵⁶Ni core and the $p_{3/2}f_{5/2}p_{1/2}g_{9/2}$ basis space. Two effective interactions, JUN45 [10] and jj44b [11], have been developed. Each uses different but overlapping data sets to define the interaction parameters. In order to test such calculations, accurate and precise g-factor systematics are needed. The $g(2_1^+)$ systematics in the even $^{70-76}$ Ge and $^{74-82}$ Se isotopes may be sensitive to subshell closures [12,13], providing a probe to test structural predictions as nuclear excitations shift from collective to single-particle behavior. However, the precise and accurate measurement of $g(2_1^+)$ in states such as these, with picosecond lifetimes, is challenging.

Along with this nuclear structure interest, the present work was motivated by the possibility to measure the g factors of neutron-rich Ge isotopes by the recoil-in-vacuum (RIV) method. Since the mid-2000s, there has been interest in the RIV technique [14] for measurements of nuclear g factors for short-lived ($\leq 10^{-7}$ s) states of Coulomb-excited radioactiveion beams [15]. For example, it has been used to measure the excited-state g factors of several nuclides near doubly magic ¹³²Sn [16–19]. It has also given a precise g factor for the sd-shell nucleus ²⁴Mg [20], where very simple (Hlike) atomic configurations are applicable. The present work developed from the intent to apply the RIV analysis method to Coulomb-excitation data taken on the neutron-rich isotopes ^{78–82}Ge, like that obtained at the Holifield Radioactive Ion Beam Facility at Oak Ridge National Laboratory [2]. However, further experiments using the stable Ge and Se isotopes to calibrate the relevant free-ion hyperfine fields found an unexpected difference in the RIV behavior along the two isotope chains [21,22]. Atomic structure effects may explain these differences, however, the possibility also remains that the adopted g-factor ratios within and/or between the two isotope chains may be responsible for some, or all, of the observed difference. The desire to verify previous measurements of the relative g factors along and between the Ge and Se isotope chains motivated the present work, for both the nuclear structure interest and to aid the interpretation of the RIV data. To this end, the relative g factors of the stable, even isotopes of Ge and Se were measured, and the first case of a relative g-factor measurement in inverse kinematics using a cocktail beam of ⁷⁴Ge and ⁷⁴Se was performed.

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B. Transient-field g-factor measurements

When an ion with a velocity of a few percent of the speed of light traverses a polarized ferromagnetic foil, it experiences a strong transient hyperfine field on the order of a few kilotesla. This transient field (TF) has been utilized to perform g-factor measurements on nuclear states with picosecond lifetimes since the mid-1970s [12,23]. While the magnitude of the transient field makes these measurements possible, a quantitative microscopic understanding of the field's origin and strength has still not been achieved [12,24]. As such, determination of the absolute value of a g factor often relies on parametrizations, which have inherent uncertainties. They are generally considered to be accurate to about $\pm 10\%$, but larger deviations can occur [25]. Therefore, experiments utilizing the TF technique are most reliable when measuring g factors relative to a nucleus, which is nearby on the nuclear chart and has an already known, independently determined g factor. The difficulty for the Ge and Se isotopes, with Z = 32 and 34, respectively, is that there is no nearby suitable calibration state with a sufficiently well-known g factor. These isotopes fall between two relatively precise calibration points used to establish the empirical parametrizations [26,27], namely the first-excited states of 56 Fe (Z=26) and 106 Pd (Z=46). (See Refs. [25,28] for further discussion.)

Although the absolute values of *g* factors determined by the TF method can be uncertain, relative values can be reliably determined. In particular, systematic uncertainties in relative *g* factors can be reduced by performing measurements using the same target foil, and most ideally when two or more isotopes are measured simultaneously so that any changes in the target, such as those induced by beam heating, affect both measurements equally. Relative *g*-factor measurements are the primary objective in the present work.

The g factors of the first-excited states in the stable, even Ge isotopes have been measured repeatedly by different groups over the years using the ion-implantation perturbedangular-correlation (IMPAC) [29] and TF [7,30,31] techniques. The most recent measurement performed on the Ge isotopes, by Gürdal et al. [7], provided the most precise values yet, with $g(2_1^+)$ determined using the TF technique in inverse kinematics and the Rutgers parametrization [26]. An older set of measurements, performed by Pakou et al. [30], had comparable precision, and used the same parametrization. However, Pakou et al. used iron hosts and conventional kinematics (target excitation), whereas Gürdal et al. used gadolinium hosts and inverse kinematics (beam excitation). The two approaches deduced significantly different $g(2_1^+)$ values in $^{74,\overline{16}}$ Ge. This difference raises the question as to whether the disagreement arises from the experimental method, or the accuracy of the parametrization, or both.

The number of independent g-factor measurements of the first-excited states in the stable, even Se isotopes is much fewer than for Ge, with the most recent measurement performed by Speidel $et\ al.$ in 1998 [6]. Absolute $g(2_1^+)$ values were determined from their relative g-factor measurements by adopting $g(2_1^+; {}^{82}\text{Se}) = +0.496(29)$ as the reference. This absolute g factor was deduced from a previous measurement of ${}^{82}\text{Se}\ 2_1^+$ -state precession angles in iron and gadolinium hosts [32]. As the precession angles from Ref. [32] were

measured to study the TF, not to determine a g factor, it appears that the adopted g factor was obtained by re-analyzing those data using the Rutgers TF parametrization to calibrate the field strength. As such, this calibration g factor is not an independently determined quantity, and the accuracy of the magnitude of the reported g factors due to the normalizing g factor remains in question.

C. Present work

In the present work, a series of relative TF measurements of first-excited state g factors in the stable, even Ge and Se isotopes is reported. A rigorous relative measurement between $g(2_1^+; {}^{74}\text{Se})$ and $g(2_1^+; {}^{74}\text{Ge})$ was performed by simultaneous TF measurements using cocktail beams. The other stable, even isotopes of Ge and Se were measured using the same targets and during the same experimental runs as the A=74 isotopes. The measured g-factor ratios are compared to those from previously published measurements, and precise relative values for the g factors are derived from a weighted average of the present and previous measurements. Absolute g factors were determined from measured precession angles and the Rutgers parametrization [26], and are compared to large-basis shell-model calculations.

The paper is arranged as follows. Experimental procedures are described in Sec. II. Experimental results are described in Sec. III. A discussion of these results in light of previous work and shell-model calculations is presented in Sec. IV. The results are summarized and conclusions drawn in Sec. V.

II. EXPERIMENTAL PROCEDURES

The transient-field method in inverse kinematics was employed to measure relative $g(2_1^+)$ values in the stable, even isotopes of Ge and Se. The technique has been reviewed in Refs. [12,24], and previous measurements by this method using the Australian National University (ANU) Hyperfine Spectrometer [34] have been described in detail elsewhere [25,28,35,36]. Data were collected over five separate runs, the details of which are listed in Table I. Ion beams were delivered by the 14UD Pelletron accelerator at the ANU Heavy Ion Accelerator Facility. The beams were incident upon a multilayer target consisting of a front ^{nat}C layer, an iron or gadolinium foil, and a copper backing. The target details are presented in Table I. The front ^{nat}C layer served to Coulomb-excite the beam, the central iron or gadolinium foil served as the ferromagnetic host for the TF precession effect, and the copper backing served as a field-free environment to stop the recoiling beam particles. Relevant details of the reaction kinematics are summarized in Table II. A cryocooler kept the target at \approx 5 K. An external magnetic field of \approx 0.09 T was applied in the vertical direction to polarize the ferromagnetic layer of the target, and its direction was reversed periodically (\approx 15 min).

Forward-scattered C ions were detected by silicon photodiodes, arranged as shown in Fig. 1 for runs 1 and 2, and Fig. 2 for runs 3–5. The central detector for runs 1 and 2 was covered with a 1.7-mg/cm²-thick mylar sheet to stop any transmitted beam, knock-on target ions, or low-energy electrons (δ rays). Four HPGe detectors, positioned in the horizontal plane,

	Run 1	Run 2 ^a	Run 3	Run 4 ^b	Run 5 ^b
Beam Energy (MeV) Beam Species	190 ^{70,72,74} Ge, ^{76,78,80,82} Se ⁷⁴ Ge + ⁷⁴ Se ^c	180 ^{74,76} Ge	$^{74}Ge + ^{74}Se^{c}$	190 ^{80,82} Se	190 ^{78,82} Se
Target (C/Fe[Gd]/Cu) (mg/cm ²)	0.48/3.66/5.6	0.37/3.67/10.6	0.28/4.23/3.94	0.28/4.23/3.9	0.5/[5.92]/5.5
ϕ_p	90°	90°	0°, 45°, 90°, 135°, 180°	0°, 45°, 90°, 135°, 180°	0°, 45°, 90°, 135°, 180°
θ_{γ} , precession θ_{γ} , angular correlation	$\pm65^{\circ}, \pm115^{\circ}$ $0^{\circ}, \pm30^{\circ}, \pm45^{\circ},$ $\pm55^{\circ}, \pm60^{\circ}, \pm65^{\circ}$	$\pm 65^{\circ}, \pm 115^{\circ}$ $0^{\circ}, \pm 30^{\circ}, \pm 40^{\circ},$ $\pm 45^{\circ}, \pm 50^{\circ}, \pm 55^{\circ},$ $\pm 60^{\circ}, \pm 65^{\circ}, \pm 75^{\circ},$ $\pm 115^{\circ}, 235^{\circ}, \pm 135^{\circ}$	$\pm 50^{\circ}, \pm 130^{\circ}$ $0^{\circ}, \pm 30^{\circ}, \pm 45^{\circ},$ $\pm 50^{\circ}, \pm 55^{\circ}, \pm 65^{\circ},$ $\pm 75^{\circ}$	±65°, ±115° 0°, ±25°, ±55° ±65°, ±88°	$\pm45^{\circ},\pm135^{\circ}$

TABLE I. Summary of measurements.

detected γ rays emitted from the Coulomb-excited beam particles. Average particle-detector azimuthal angles (ϕ_p) and γ -ray detector angles (θ_γ) for each run are summarized in Table I. The coordinate frame defining these particle- and γ -detector angles has its origin at the beam spot on the target. The beam direction defines the z or polar axis $(\theta=0)$ and the magnetic field is applied along the γ -ray axis, which is along $(\theta,\phi)=(90^\circ,90^\circ)$ in spherical polar coordinates. The γ -ray detectors are located in the γ -ray detectors are located in the γ -ray detectors are positioned parallel to the γ -ray plane. In the following discussion of runs 3–5 the particle detectors are identified by their γ -ray angle as indicated in Fig. 2(b).

The γ -ray detector angles employed for the TF precession measurements were selected to maximize the measured precession effect for the available particle-detector angles [37]. Angular correlations were measured by moving two or three γ -ray detectors through a sequence of different angles with respect to the beam, while the remaining detector(s) remained

fixed. The angular correlation data sets were normalized using particle- γ coincidence counts in the fixed γ -ray detector(s). The data from runs 1 and 2 were recorded using a recently acquired XIA Pixie-16 digital pulse processor [38]; these results are the first published from this installation.

Angular precessions were measured using standard procedures [12], with some modification for the annular arrangement of the particle detectors in runs 3–5. The TF induces a rotation, $\Delta\theta$, in the angular correlation of the deexcitation γ rays, $W(\theta)$, for the nuclei traversing the ferromagnetic medium. Double ratios of observed counts were formed:

$$\rho_{ij} = \sqrt{\frac{N(\theta_i) \uparrow N(\theta_j) \downarrow}{N(\theta_i) \downarrow}}, \tag{1}$$

where $N(\theta_i)$ and $N(\theta_j)$ represent particle- γ coincidence counts in the photopeak measured in γ -ray detectors i and j at

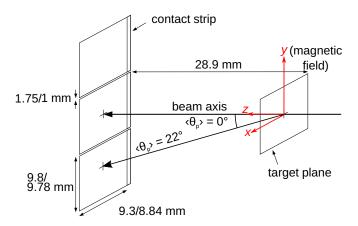


FIG. 1. Experimental geometry for run 1 and run 2 showing the beam axis and the particle detector dimensions (run 1/ run 2). The average scattering angles for the 12 C target ions are indicated by $\langle \theta_p \rangle$.

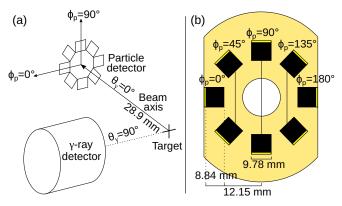


FIG. 2. (a) Experimental geometry for runs 3–5 showing the beam axis, a γ -ray detector and the particle detectors. (b) A schematic of the particle detector array indicating dimensions and joined detectors.

^aRuns 1 and 2 were separated in time because the ion source was contaminated after running the Se and cocktail beams, and the γ -ray energies associated with ⁷⁶Ge and ⁷⁶Se, 562.9 and 559.1 keV, respectively, are too close to separate reliably.

^bRuns 4 and 5 were consecutive, beginning with the ⁸⁰Se beam, followed by ⁸²Se and ⁷⁸Se beams. The target was changed during delivery of the ⁸²Se beam.

^cCocktail beam.

TABLE II. Measured transient-field precession angles and reaction kinematics for the 2_1^+ states of Ge and Se isotopes as their ions traverse the ferromagnetic layer of the target. $E_i(E_e)$ is average energy at entry into (exit from) the foil, $v_i(v_e)$ is the average velocity at entry into (exit from) the foil, $\langle v \rangle$ is the average velocity through the foil, T is the effective transit time, and $t_0 = c/137$ is the Bohr velocity. $t_0 = c/137$ is the Bohr velocity.

Nuclide	E_i (MeV)	E_e (MeV)	v_i/v_0	v_e/v_0	$\langle v/v_0 angle$	T(fs)	$\tau(ps)^a$	$-\Phi(\tau)$ (mrad)	$-\Delta\theta$ (mrad)
Run 1:									
$\langle \theta_{\rm p} \rangle = 22^{\circ}$									
⁷⁰ Ge	91.2	10.9	7.25	2.50	4.61	407	1.91	29.3	8.4(13)
⁷² Ge	92.6	11.9	7.20	2.58	4.59	444	4.75	31.8	7.3(12)
⁷⁴ Ge	93.9	12.9	7.15	2.65	4.59	462	18.1	33.2	9.2(8)
⁷⁴ Ge	93.9	12.9	7.15	2.65	4.59	462	18.1	33.2	$9.5(12)^{b}$
⁷⁴ Se	92.8	10.1	7.11	2.35	4.37	480	10.2	35.9	$13.3(9)^{b}$
⁷⁶ Se	94.1	11.1	7.07	2.43	4.41	481	17.8	36.2	12.4(8)
⁷⁸ Se	95.5	12.1	7.03	2.50	4.45	474	14.0	35.9	10.1(7)
⁸⁰ Se	96.9	13.1	6.99	2.57	4.49	467	12.3	35.6	13.3(9)
⁸² Se	98.1	14.1	6.94	2.63	4.51	468	18.6	35.8	15.2(10)
Run 1:									, ,
$\langle \theta_{\mathrm{p}} \rangle = 0^{\circ}$									
⁷⁰ Ge	80.2	7.16	6.79	2.03	4.06	452	1.91	30.7	11.1(16)
⁷² Ge	81.8	8.04	6.77	2.12	4.06	495	4.75	33.5	9.4(16)
⁷⁴ Ge	83.4	8.95	6.74	2.21	4.09	513	18.1	35.0	7.6(13)
⁷⁴ Ge	83.4	8.95	6.74	2.21	4.09	513	18.1	35.0	$8.4(17)^{b}$
⁷⁴ Se	82.3	6.78	6.69	1.92	3.86	537	10.2	38.0	13.7(12) ^b
⁷⁶ Se	83.9	7.61	6.67	2.01	3.92	536	17.8	38.2	14.2(10)
⁷⁸ Se	85.4	8.49	6.64	2.09	3.99	523	14.0	37.7	12.9(9)
⁸⁰ Se	87.0	9.39	6.62	2.17	4.04	514	12.3	37.3	13.6(13)
⁸² Se	88.4	10.3	6.59	2.25	4.08	513	18.6	37.4	16.3(13)
Run 2:									
$\langle \theta_{\rm p} \rangle = 22^{\circ}$									
⁷⁴ Ge	91.0	11.5	7.04	2.51	4.44	478	18.1	33.8	9.2(5)
⁷⁶ Ge	92.3	12.5	7.00	2.58	4.48	477	26.9	33.9	7.9(5)
Run 2:									(-)
$\langle heta_{ m p} angle = 0^\circ$									
⁷⁴ Ge	82.0	8.39	6.68	2.14	4.01	525	18.1	35.4	10.7(7)
⁷⁶ Ge	83.6	9.29	6.66	2.22	4.07	520	26.9	35.4	9.7(6)
Run 3:									211(2)
⁷⁴ Ge	111	13.0	7.76	2.66	4.87	505	18.1	37.2	9.5(5) ^c
⁷⁴ Se	110	10.1	7.74	2.34	4.63	525	10.2	40.3	13.5(6) ^c
Run 4:	110	10.1	,.,.	2.5	1.03	323	10.2	10.5	13.3(0)
⁸⁰ Se	114	13.0	7.57	2.56	4.72	516	12.3	40.1	13.8(10)
⁸² Se	115	13.9	7.51	2.62	4.74	517	18.6	40.3	17.3(15)
Run 5:	110	13.7	7.51	2.02	, .	517	10.0	10.5	17.3(13)
⁷⁸ Se	103	18.8	7.30	3.12	4.96	680	14.0	54.3	17.6(8)
⁸² Se	106	21.1	7.20	3.22	4.98	681	18.6	54.5	25.9(13)
	100	21.1	7.20	3.22	1.70	001	10.0	J 1.J	23.7(13)

^aFrom Ref. [33]. Uncertainties in τ can be neglected in the evaluation of $\Phi(\tau)$.

angles $+\theta_{\gamma}$ and $-\theta_{\gamma}$, respectively, and \uparrow and \downarrow represent the field direction.

For runs 1 and 2 the detectors had the usual particle- γ coincidence symmetry with the particle detectors at $\phi_p = 90^\circ$ and $\phi_p = 270^\circ$ (sometimes designated $\phi_p = -90^\circ$), so double ratios can be formed in the conventional way [23] for each of the three particle detectors.

To calculate ρ_{ij} for runs 3–5 using the detector type shown in Fig. 2, a modified procedure is required when using counts from the photodiodes with $\phi_p \neq \pm 90^\circ$. The symmetries

required to form the particle- γ coincidences in Eq. (1) can be inferred from Fig. 3, which represents a top-down view of the particle and γ -ray detectors projected onto the horizontal plane through the γ -ray detectors. For clarity, Fig. 3 shows only one pair of particle detectors at angles ϕ_p and $180^\circ - \phi_p$. By inspection of Fig. 3 it can be seen that the relative angle between the γ -ray detector at $+\theta_\gamma$ and the particle detector at ϕ_p is equivalent to that between the γ -ray detector at $-\theta_\gamma$ and the particle detector at $180^\circ - \phi_p$, as indicated by the dotted arcs. There is another pair of particle- γ combinations with the

^bSimultaneous measurement of ⁷⁴Ge and ⁷⁴Se with cocktail beam.

^cSimultaneous measurement of ⁷⁴Ge and ⁷⁴Se with cocktail beam.

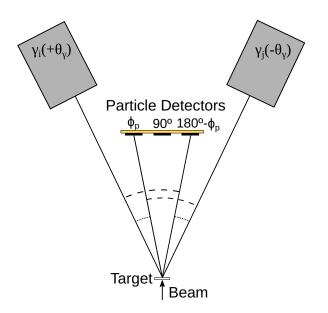


FIG. 3. Illustration of the particle- γ coincidence geometry, drawn from a top-down view. Symmetry is maintained when particle- γ coincidence pairs are formed with γ_i at $+\theta$ paired with the particle detector at ϕ_p and γ_j at $-\theta$ paired with the particle detector at $180^\circ - \phi_p$, shown by the equivalent dotted vs dashed angles. In short, $\gamma_i(\phi_p)$ must be paired with $\gamma_j(180^\circ - \phi_p)$. Figure 2 shows the definition of the angle ϕ_p .

relative angle indicated by the dashed arcs in Fig. 3; the angle between detectors at $+\theta_{\gamma}$ and $180^{\circ} - \phi_{p}$ is equivalent to that between the detectors at $-\theta_{\gamma}$ and ϕ_{p} .

These symmetries indicate that Eq. (1) should be constructed such that if $N(\theta_i)$ represents $N(\theta_i, \phi_p)$, then $N(\theta_j)$ must represent $N(\theta_j, 180^\circ - \phi_p)$, and if $N(\theta_i)$ represents $N(\theta_i, 180^\circ - \phi_p)$, then $N(\theta_j)$ must represent $N(\theta_j, \phi_p)$. A more detailed account of this procedure will be published elsewhere [37].

The spin-rotation (precession) angle $\Delta\theta$ is determined from:

$$\Delta\theta = \frac{\epsilon}{S},\tag{2}$$

where

$$\epsilon = \frac{1 - \rho}{1 + \rho},\tag{3}$$

and S is the logarithmic derivative of the angular correlation at $+\theta_{\gamma}$

$$S = S(\theta_{\gamma}) = \left. \frac{1}{W} \frac{dW}{d\theta} \right|_{\theta_{\gamma}}.$$
 (4)

Along with the double ratios used to determine the TF precession effect it is useful to form cross ratios, which should show no net effect, as a check on the validity of the data. For the conventional ($\phi_p = 90^\circ$) particle detector geometry cross ratios are given by Eq. (1) with $\theta_i = \theta_\gamma$ and $\theta_j = 180^\circ - \theta_\gamma$, for example. Such symmetrically placed particle and γ -ray detectors should have ρ values distributed around unity (or ϵ distributed around zero); departures from the null effect can indicate systematic errors.

The angular correlations were computed using routines based on the Winther-de Boer code [39] in order to determine the value of $S(\theta_{\gamma})$ [12,40,41], as the nuclei of interest were Coulomb-excited with known reaction geometry. The angular correlations were also measured in several cases to verify the calculations and experimental procedures. In particular, the measured angular correlations can determine if there is any significant offset of the γ -ray detector from the nominal angle. Such offsets have little impact on deduced relative precession angles, but can strongly affect absolute values, since S is a strong function of θ_{γ} at the detection angles used for the precession measurements.

For short-lived states the precession angle is weakly dependent on the level lifetime, which may be taken into account by expressing

$$\Delta \theta = g \, \Phi(\tau), \tag{5}$$

where g is the nuclear g factor and $\Phi(\tau)$ is given by:

$$\Phi(\tau) = -\frac{\mu_N}{\hbar} \int_0^T B_{\text{TF}}[v(t)] e^{-t/\tau} dt, \qquad (6)$$

where μ_N is the nuclear magneton, $B_{\rm TF}[v(t)]$ is the TF strength at the time-dependent ion velocity v(t), τ is the mean life of the state of interest, T is the transit time of the nucleus through the ferromagnetic medium, and t is time.

The TF strength has been parametrized in terms of the ion velocity and atomic number by fitting an empirical function to data. The most widely used parametrizations have the general form:

$$B_{\rm TF}[v(t)] = a_{\rm TF} Z^{p_v} (v/v_0)^{p_{\rm Z}},$$
 (7)

where v(t) is the time-dependent ion velocity, Z is the atomic number of the ion, v/v_0 is the ion velocity in atomic units, $a_{\rm TF}$ is a fitted scale parameter, p_v defines the velocity dependence and p_Z describes the atomic number dependence. Differences in the parameters arise from fitting data sets that cover different atomic-number ranges and span different velocity ranges. However, all parametrizations applicable to ion velocities in the regime considered here have $p_Z \approx 1$. For example, the linear parametrization [27] has $p_Z = 1$ and the Rutgers parametrization [26] has $p_Z = 1.1$.

The primary objective in the present work is to measure g-factor ratios for the Ge and Se isotopes. These are obtained by combining Eq. (2) and Eq. (5) to give

$$\frac{g_x}{g_y} = \frac{\epsilon_x}{\epsilon_y} \frac{S_y}{S_x} \frac{\Phi_y}{\Phi_x} = \frac{\Delta \theta_x}{\Delta \theta_y} \frac{\Phi_y}{\Phi_x},$$
 (8)

where x and y signify the two states being measured. The ratio Φ_y/Φ_x must be evaluated based on a parametrization of the TF strength. For this purpose we have adopted the Rutgers parametrization [26], for which $a_{\rm TF}(Fe) = 16.9\,{\rm T}$ for fully saturated iron hosts, $a_{\rm TF}(Gd) = 16.6\,{\rm T}$ for our gadolinium hosts [42], and $p_v = 0.45$ and $p_Z = 1.1$ for both hosts.

The ratio Φ_y/Φ_x is almost independent of any reasonable choice of parameters. The scale parameter a_{TF} cancels in any ratio, as does the atomic number dependence for ratios within an isotope chain. For nearby atomic numbers, such as for the ratio $\Phi(^{74}\text{Se})/\Phi(^{74}\text{Ge})$, the difference between taking

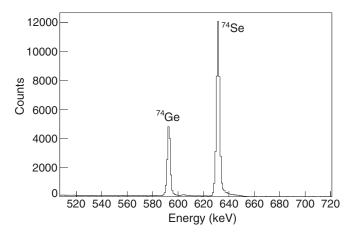


FIG. 4. Spectrum of γ rays at 65° to the beam in coincidence with ^{12}C recoils measured during run 1 with the $^{74}Ge/^{74}Se$ cocktail beam. Random coincidences have been subtracted. The resulting spectrum has almost no background. This spectrum represents $\approx 25\%$ of the data taken for the simultaneous measurement of ^{74}Ge and ^{74}Se during run 1.

 $p_Z=1.1$ versus $p_Z=1$ is negligible (0.6% in this case). $\Phi_y(\tau_y)/\Phi_x(\tau_x)$ is therefore sensitive only to the parameter p_v , and then only if one of the lifetimes is short compared to the transit time of the ion through the ferromagnetic foil. In the cases encountered here, the difference in Φ_y/Φ_x that comes about from taking $p_v=1$ versus $p_v=0.45$ is altogether negligible. Furthermore, Φ_y/Φ_x is near unity for most of the cases reported here.

III. RESULTS

In order to evaluate the *g*-factor ratios, photopeak counts were obtained from background-subtracted integrals of the photopeak region of the $2_1^+ \rightarrow 0_1^+$ transition, after random-coincidence subtraction in particle- γ coincidence spectra. An example of a random-subtracted particle- γ coincidence spectrum for ⁷⁴Ge and ⁷⁴Se from run 1 is shown in Fig. 4.

Selected measured angular correlations are shown in Figs. 5–8. Figures 5 and 6 compare the angular correlations for the central and outer particle detectors in runs 1 and 2 (see Fig. 1). There is a less pronounced dip at $\theta_{\gamma}=0^{\circ}$ for the outer detectors, but the slope at $\theta_{\gamma}=\pm65^{\circ}$ is very similar for both the central and outer detectors. These figures also show that the calculated angular correlations agree very well with experiment and that the angular correlations are almost identical between the isotopes measured. Thus, the ratio S_{γ}/S_{x} in Eq. (8) is very near unity in all cases considered here.

Figures 7 and 8 show angular correlations for the five particle detectors at $\phi_p = 0^\circ$, 45° , 90° , 135° , and 180° in run 3 (see Fig. 2). The similarity of the angular correlations for $\phi_p = 90^\circ$ to those for the outer detectors in Fig. 5 and Fig. 6 can be noted. Also evident in Fig. 7 and Fig. 8 is that for $\phi_p = 0^\circ$, 45° , 135° , and 180° , the angular correlation has a pronounced slope at $\theta_\gamma = \pm 45^\circ$ and $\theta_\gamma = \pm 90^\circ$, in some cases of similar magnitude to that at $\theta_\gamma = \pm 65^\circ$ for the conventionally used $\phi_p = 90^\circ$. These angles of maximum slope determined the placement of γ -ray detectors indicated for runs 3–5 in Table I.

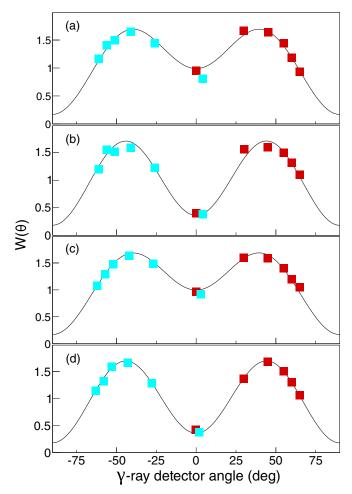


FIG. 5. Angular correlations for the ⁷⁴Ge and ⁷⁴Se $2_1^+ \rightarrow 0_1^+$ transitions from run 1 for the two unique particle-detector angles. (a) ⁷⁴Ge, top and bottom particle detectors. (b) ⁷⁴Ge, center particle detector. (c) ⁷⁴Se, top and bottom particle detectors. (d) ⁷⁴Se, center particle detector. Statistical errors are smaller than or similar in size to the data points. Dark red (light blue) points correspond to the γ -ray detector that moves to positive (negative) angles. The measured data are normalized to the theoretical angular correlations shown as continuous lines. Although there is a distinct difference between the correlations for the top/bottom and center particle detectors near 0°, they are similar near $\pm 65^\circ$, meaning the two sets of particle detectors have similar sensitivity for the *g*-factor measurement. An offset of $\pm 3^\circ$ was required on the negative angle data (all taken with the same γ -ray detector) to optimize the fit.

Precession angles were evaluated as per Eq. (2), with $S(\theta_{\gamma})$ calculated from angular correlation theory [40,41,43]. The measured precession angles are listed in Table II. In order to check that systematic errors were minimal, cross ratios [12] were calculated for all particle- γ pairs. The cross ratios showed a normal distribution around unity, indicating no evidence of systematic error.

Indirect population of the 2_1^+ state by feeding from the 4_1^+ states was determined from the 74,76 Ge and 74 Se spectra as these nuclides have the lowest 4_1^+ -state excitation energies. Population of the 4_1^+ state was measured to be no greater than $\approx 2\%$ of the 2_1^+ state population in the strongest case,

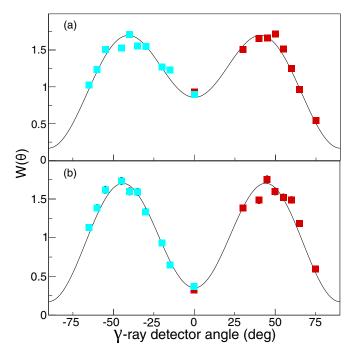


FIG. 6. Angular correlations for the 76 Ge $2_1^+ \rightarrow 0_1^+$ transition from run 2 for the two unique particle-detector angles. (a) Top and bottom particle detectors. (b) Center particle detector. See also the caption of Fig. 5.

and therefore the effect of feeding on the measurement of the 2_1^+ -state precession angle could be neglected in all cases.

The *g*-factor ratios determined from the measured precession angles and $\Phi(\tau)$ values in Table III are listed in Table III, and shown in Fig. 9 (Ge isotopes) and Fig. 10 (Se isotopes). The Ge isotopes are referenced to ⁷⁴Ge, the Se isotopes are referenced to ⁷⁴Se, and the Ge and Se isotopes are related through the ratio $g(^{74}\text{Se})/g(^{74}\text{Ge})$. The value of this ratio from the cocktail beam data in runs 1 and 3 alone is $g(^{74}\text{Se})/g(^{74}\text{Ge}) = 1.325(77)$. With the additional data collected for ⁷⁴Ge alone from run 1 the ratio becomes $g(^{74}\text{Se})/g(^{74}\text{Ge}) = 1.338(71)$, which is the value given in Table III. Runs 4 and 5 did not include either of the reference isotopes, ⁷⁴Ge and ⁷⁴Se, but they give independent measures of $g(^{80}\text{Se})/g(^{82}\text{Se})$ and $g(^{78}\text{Se})/g(^{82}\text{Se})$, respectively. These data were included in the evaluation of the *g*-factor ratios for

TABLE III. $g(2_1^+)$ ratios from the present and previous work [6,7,30,31].

Ratio	Present	[30]	[31]	[6,7]	Average
⁷⁰ Ge/ ⁷⁴ Ge	1.16(15)	1.08(8)	1.06(26)	1.27(12)	1.138(59)
72 Ge/ 74 Ge	0.92(13)	0.92(7)	1.05(14)	1.15(9)	0.999(48)
76 Ge/ 74 Ge	0.88(5)	0.97(7)	0.95(13)	0.92(6)	0.918(34)
74 Se/ 74 Ge	1.34(7)			1.22(8)	1.288(53)
76 Se/ 74 Se	0.96(7)			0.942(20)	0.944(19)
78 Se/ 74 Se	0.82(5)			0.898(22)	0.877(19)
80 Se/ 74 Se	0.99(7)			1.017(16)	1.015(16)
82 Se/74 Se	1.19(6)			1.159(16)	1.166(15)

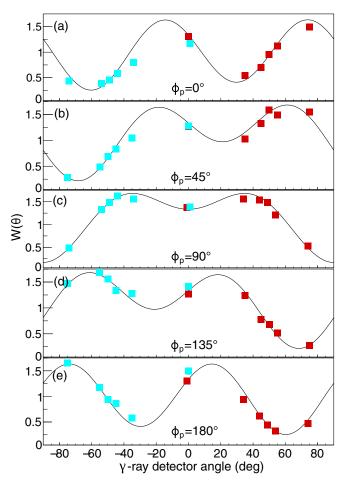


FIG. 7. Angular correlations for the $^{74}\text{Ge}\ 2_1^+\to 0_1^+$ transition from run 3, with measurements taken at varying γ -ray detector angles for the five particle detector angles. (a) Particle detector at $\phi_p=0^\circ$. (b) Particle detectors at $\phi_p=\pm 45^\circ$. (c) Particle detectors at $\phi_p=\pm 90^\circ$. (d) Particle detectors at $\phi_p=\pm 135^\circ$. (e) Particle detector at $\phi_p=180^\circ$. The measured data are normalized to the theoretical angular correlations. Dark red (light blue) points correspond to the γ -ray detector that moves to positive (negative) angles. Note the reflection symmetry between the correlations for $\phi_p=0$ and $\phi_p=180^\circ$, $\phi_p=45^\circ$ and $\phi_p=135^\circ$.

the Se isotopes relative to 74 Se by performing a χ -squared fit to the complete data set. Such a procedure gives the correct average values with the correct uncertainties in a straightforward way.

The Rutgers parametrization was used to set the absolute scale of the relative *g*-factor measurements. Rather than normalize to a particular reference *g* factor, a global fit was performed that included the present precession data in Table II and previous *g*-factor ratios from Table III. A 10% uncertainty was assigned to the TF strengths for the iron and gadolinium hosts. The reduced χ -squared value from this fit, $\chi^2_{\nu} = 1.06$, shows the internal consistency of the present measurements and their consistency with the previous *g*-factor ratios. The resultant absolute *g* factors are shown in Table IV and in Fig. 11.

In the process of fitting these data and testing the sensitivity of the relative *g* factors to alternative parametrizations of the

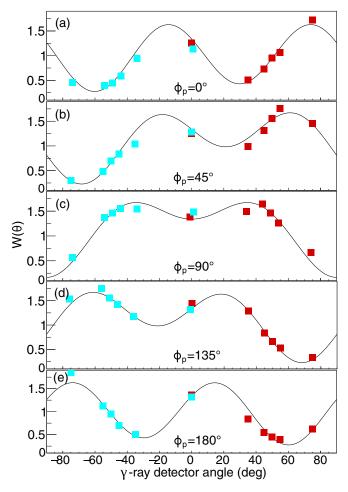


FIG. 8. As for Fig. 7, for the ⁷⁴Se $2_1^+ \rightarrow 0_1^+$ transition in run 3.

TF strength, it was observed that assuming a linear velocity dependence for the TF strength gives almost identical *g*-factor ratios, but has an increased χ -squared value, $\chi^2_{\nu} = 2.0$. Thus, it is clear that the present *g*-factor ratios are not sensitive to the velocity dependence of the transient field.

IV. DISCUSSION

A. g-factor measurements

The g-factor values measured previously by the TF technique are shown in Table IV. For the Ge isotopes, there have been measurements by the Oxford [30], Melbourne [31], and Rutgers [7] groups based on the Rutgers parametrization. Scrutiny of the $g(2_1^+;^{74}\text{Ge})$ values, having the smallest relative uncertainty, indicates that the Oxford measurement generally gave a larger magnitude for the $^{70-76}\text{Ge}$ g factors than obtained in the Melbourne and Rutgers measurements. However, as shown in Fig. 9, the relative g factors of the previous and present measurements are in overall good agreement. In making this comparison, the data from the Rutgers group [7] were restricted to those taken using the same target (their target II with gadolinium as the ferromagnetic host). Figure 10 shows overall good agreement between the present and previous [6] g-factor ratios for the Se isotopes.

TABLE IV. Measured g factors in Ge and Se using the TF technique. Measurements are ordered chronologically from left to right. Although not explicitly listed, the signs of all g factors in this table are positive.

Nuclide	[30]	[31]	[6,7]	Presenta
⁷⁰ Ge	0.468(26)	0.370(89)	0.44(4)	0.322(29)
⁷² Ge	0.399(33)	0.367(44)	0.44(2)	0.281(25)
⁷⁴ Ge	0.433(20)	0.350(22)	0.35(1)	0.282(22)
⁷⁶ Ge	0.419(23)	0.334(39)	0.32(1)	0.263(21)
⁷⁴ Se	, ,	, ,	0.428(27)	0.368(27)
⁷⁶ Se ^b			0.403(23)	0.350(27)
⁷⁸ Se			0.384(25)	0.325(24)
⁸⁰ Se			0.435(27)	0.374(28)
⁸² Se			0.496(29)	0.430(32)

^aThese results are from a global fit to the present data in Table II together with previous *g*-factor ratios from Table III. The uncertainties include $\pm 10\%$ uncertainty on the TF parametrizations for the iron and gadolinium hosts.

^bThe only independently determined g factor, by an IPAC measurement [44], gives g = +0.35(5) for ⁷⁶Se (see text).

Concerning the ratio of the g factors between the Se and Ge isotopes, the most precise measurements in previous work for 74 Se and 74 Ge are g = +0.428(27) [6] and g = +0.35(1) [7], respectively, giving $g(2_1^+; ^{74}\text{Se})/g(2_1^+; ^{74}\text{Ge}) = 1.22(8)$. The measurements were both made using gadolinium as the ferromagnetic host, sampling the TF in overlapping but different velocity ranges. The present simultaneous measurement ensures that the ions sample the TF over effectively the same velocity range, and gives $g(2_1^+; ^{74}\text{Se})/g(2_1^+; ^{74}\text{Ge}) = 1.34(7)$, which agrees with the previous work (the error bars overlap).

From these results two conclusions may be drawn. First, the TF parametrization assumed in the previous work appears

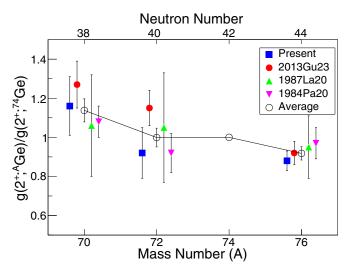


FIG. 9. Ratios of $g(2_1^+)$ in the Ge isotopes relative to ⁷⁴Ge, from present and previous work: 1984Pa20 [30], 1987La20 [31], and 2013Gu23 [7]. Values from Ref. [7] are taken from their target II measurements only.

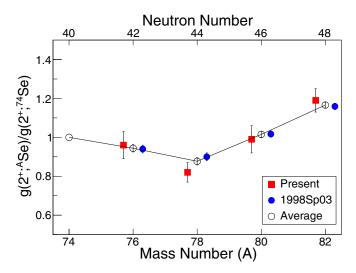


FIG. 10. Ratios of $g(2_1^+)$ in the Se isotopes relative to ⁷⁴Se, from present and previous work: 1998Sp03 [6].

to describe the velocity dependence of Ge and Se ions traversing gadolinium hosts within the precision of the data. Second, the TF strength must change smoothly between Z=32 and Z=34 for both iron and gadolinium hosts. The agreement of ratios between present and previous work gives confidence in adopting the weighted average of present and previous g-factor ratios. The remaining challenge then is to determine the absolute scale.

The IMPAC data on the Ge and Se isotopes [29] cannot determine the absolute g factors, mainly because the static hyperfine field takes several picoseconds to reach its full strength following implantation [45,46]. This equilibration time (\approx 5 ps) is a significant fraction of the 2_1^+ -level lifetime in all of the isotopes studied. All that the IMPAC data can provide is a lower estimate on the absolute g factors by making the extreme assumptions that all implanted ions reside on

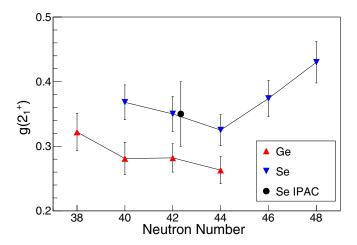


FIG. 11. Comparison of the adopted Ge and Se *g*-factor values (Table IV). There is a shift in magnitude between the two isotope chains but the trend with neutron number appears to be similar. The independently measured IPAC result for ⁷⁶Se [44] is shown for reference (slightly displaced from N = 42 for clarity).

full-field sites and that the static hyperfine field reaches its full strength promptly after implantation. Under these conditions the absolute g factors would be about 20% smaller than those in the last column of Table IV. More realistic assumptions about the effective hyperfine fields at the implanted ions readily accommodate both the present and previous g factor values. (This discussion of the IMPAC data has excluded the g-factor ratios reported here and in Ref. [6].)

To our knowledge the only independently measured g factor that can serve to set the magnitude of the Ge and Se g factors is an integral $\gamma\gamma$ perturbed-angular-correlation (IPAC) measurement on ⁷⁶Se [44], populated by the radioactive decay of ⁷⁶As. With a more recently measured static-hyperfine-field strength of $B_{\rm hf}=67.9(10)\,{\rm T}$ [47] and lifetime of $\tau=17.75(29)\,{\rm ps}$ [33], this measurement gives $g(2_1^+;^{76}{\rm Se})=+0.35(5),\,$ i.e., with 14% uncertainty. The present absolute g factor for ⁷⁶Se, $g=+0.350(27),\,$ happens to agree perfectly with this value. The IPAC g factor is smaller than, but nevertheless consistent with, $g(2_1^+;^{76}{\rm Se})=+0.403(23)$ as reported in Ref. [6].

The present absolute *g*-factor values are about 80% of those reported previously. It is not certain why, given that the present and previous measurements are all based more or less directly on the Rutgers parametrization. There are, however, two important differences between the present and previous work: (i) the ion velocities in the present work are higher than those used to determine the Rutgers parametrization, and (ii) the present work primarily used iron rather than gadolinium hosts. The more recent statistically precise measurements [6,7] used gadolinium hosts whereas iron hosts were chosen for the present measurements to help avoid the possible beam heating effects that have been noted by Benczer-Koller and Kumbartzki [12]. Beam heating is more likely to affect gadolinium hosts with a Curie temperature of 293 K than iron hosts with Curie temperature 1043 K.

In summary: the present and previous relative g-factor measurements are robust, but the absolute scale remains uncertain on the level of $\pm 20\%$. Nevertheless the absolute g factors adopted here agree well with the only independent g-factor measurement on 76 Se, and so we proceed to compare these values with theory.

B. Shell-model calculations

Shell-model calculations were performed using the shell-model program NUSHELLX [48] with the JUN45 [10] and jj44b [11] interactions. Previous studies with these interactions include a comparison between calculated level energies and E2 observables for $^{78-82}$ Se by Srivastava and Ermamatov [49], as well as calculations of level energies and E2 transitions for 76 Ge [50] and 76 Se [51] by Mukhopadhyay *et al.* The Appendix of Ref. [50] gives a detailed description of the model space and two-body matrix elements. In brief, both interactions are based on a renormalized Bonn-C potential with the same assumed mass dependence. The differences between the interactions arise from fitting different sets of bindingenergy and excitation-energy data. The jj44b interaction fits data for Z=28-30 (N=28-50) and also for N=48-50

\overline{Z}	A	N	$\langle L_p angle$	$\langle S_p \rangle$	$\langle L_n angle$	$\langle S_n \rangle$	μ_p	μ_n	μ	g(2 ⁺)
32	70	38	0.772	0.0044	1.192	0.0297	0.790	-0.079	0.710	0.355
32	72	40	0.760	0.0023	1.176	0.0605	0.769	-0.162	0.607	0.304
32	74	42	0.770	0.0032	1.150	0.0764	0.782	-0.205	0.578	0.289
32	76	44	0.897	0.0039	1.018	0.0813	0.912	-0.218	0.694	0.347
32	78	46	1.017	0.0027	0.895	0.0852	1.028	-0.228	0.800	0.400
32	80	48	1.002	-0.0120	0.907	0.1033	0.955	-0.277	0.679	0.339
32	82	50	2.162	-0.1622	0.000	0.0000	1.528	0.000	1.528	0.764
34	72	38	0.847	-0.0123	1.110	0.0469	0.799	-0.126	0.673	0.337
34	74	40	0.814	-0.0104	1.132	0.0568	0.773	-0.152	0.621	0.310
34	76	42	0.745	-0.0025	1.174	0.0787	0.735	-0.211	0.525	0.262
34	78	44	0.866	0.0064	1.044	0.0814	0.891	-0.218	0.674	0.337
34	80	46	1.044	0.0090	0.865	0.0822	1.079	-0.220	0.859	0.429
34	82	48	1.163	0.0064	0.744	0.0869	1.188	-0.233	0.955	0.478
34	84	50	1.972	0.0279	0.000	0.0000	2.081	0.000	2.081	1.041

TABLE V. Component breakdown of the Ge and Se 2_{1}^{+} -state magnetic-moments (μ) for the JUN45 interaction [10].

(Z = 28-50), whereas JUN45 fits nuclei in the ranges Z = 30-32 (N = 32-50) and N = 46-50 (Z = 31-46). In relation to the present results, JUN45 includes all Ge isotopes and 80,82 Se in its fits, whereas jj44b includes only 82 Se.

The effective M1 operator $g_s^{\text{eff}} = 0.7 g_s^{\text{free}}$ and $g_l^{\text{eff}} = g_l^{\text{free}}$ for both protons and neutrons was taken from Ref. [10]. A breakdown of the spin contributions to the g factors is given for the JUN45 interaction in Table V. The theoretical g factors are compared with experiment in Fig. 12. As the absolute values of the g factors are not well determined experimentally, we focus on the trends. Both interactions predict a marked increase in the g factor at N = 50, the neutron shell closure. Among the observed g factors, the smallest value occurs at N=44 for both isotope chains, however, for the Ge isotopes there are no data beyond N = 44 to determine if the downward trend observed from 70Ge to 76Ge continues, or whether the g factors begin to increase as both calculations predict. The qualitative V-shaped trend observed in the mass dependence of the Se isotopes is evident in both calculations, which agree with each other from ⁷⁴Se to ⁸⁰Se, but place the smallest g factor at N = 42, rather than at N = 44 as observed experimentally. This observation of the smallest g factor being at N = 44, which is the midpoint of the neutron $p_{1/2}g_{9/2}$ shell, has been interpreted in terms of the interacting boson model as evidence for a firm (sub)shell closure at N = 38 along with the well-established shell closure at N = 50 [6].

The g factor can be broken down into its contributions from the orbital (L) and spin (S) angular momenta of the protons and neutrons. Specifically, $g(2^+) = \mu(2^+)/2$, where the magnetic moment is separated into a proton and a neutron component: $\mu = \mu_p + \mu_n$ with $\mu_p = g_l(p)\langle L_p \rangle + g_s(p)\langle S_p \rangle$, and likewise for μ_n . Inserting the effective nucleon g-factor values gives

$$g(2^+) = (\langle L_p \rangle + 3.91 \langle S_p \rangle - 2.68 \langle S_n \rangle)/2, \tag{9}$$

or, noting from Table V that $3.91\langle S_p\rangle\approx 0$ and $2.68\langle S_n\rangle\approx 0.2$,

$$g(2^+) \approx (\langle L_p \rangle - 0.2)/2.$$
 (10)

Similar behavior can be anticipated for the jj44b interaction. Thus, the trends shown in Fig. 12 for the theoretical g factors reflect primarily the proton orbital contribution to the angular momentum. Small variations in $\langle L_p \rangle$ directly impact on the calculated g factor. Experimentally, the variation in the g factors from the average value along each chain of stable isotopes is on the order of $\approx \pm 0.05$, which corresponds to changes in $\langle L_p \rangle$ on the order of $\approx \pm 0.1$. This estimate can be made despite uncertainties in the absolute magnitude of the g factors.

Neutron scattering studies of ⁷⁶Ge [50] and ⁷⁶Se [51] have allowed the band structures of these isobars to be observed, and low-energy shape coexistence to be identified in ⁷⁶Se. Overall, a good description of the low-lying level structures was obtained by the same shell-model calculations as discussed here. Given the considerable sensitivity of the $g(2_1^+)$ values to the balance of the spin carried by orbital motion of the protons, it is suggested that these shell-model calculations should not be expected to reproduce in detail the massdependent variation of the g factors of the stable isotopes. Indeed, the stable Ge and Se isotopes are challenging to interpret due to their shape-transitional nature, together with the occurrence of shape coexistence in many of the isotopes [1,3,4,52]. Evidently, the $g(2_1^+)$ values will be affected by configuration mixing and by the degree of mixing between shapes.

It is relevant to note that the shell-model calculations give a reasonable description of the E2 transition strengths in 76 Ge and 76 Se [50,51] using standard effective charges for the region [10]. A firm statement on whether or not there is additional collectivity in the 2_1^+ states of these nuclei not captured by the shell-model calculations, as suggested by Gürdal *et al.* [7], requires that the absolute values of the g factors be measured accurately and with some precision.

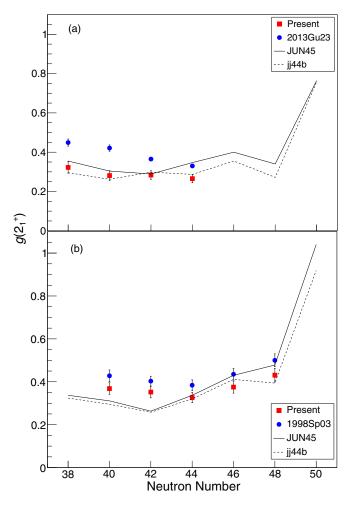


FIG. 12. Measured 2_1^+ -level g factors for (a) Ge and (b) Se isotopes from the present work (red squares) and the literature (blue circles). Previous work is designated by the Nuclear Science Reference code, namely 2013Gu23 [7] and 1998Sp03 [6]. Shell-model calculations using the JUN45 and jj44b interactions are shown as solid lines and dashed lines, respectively. Experimental g factors from Ref. [7] shown in (a) are their reported weighted-averages that include the previous measurements [30,31] along with their own data. (See also Table IV.)

V. CONCLUSION

Relative g factors have been measured for the first-excited states of the stable, even isotopes of Ge and Se. The new relative g factors agree well with relative g factors taken from literature.

Although there remains a need for reliable, independent calibration of the TF strength for Ge and Se ions, the present

confirmation of previously reported g-factor ratios also confirms that any marked difference in free-ion hyperfine interactions observed for Ge and Se ions recoiling in vacuum (see Refs. [21,22]) must stem from atomic physics and not from the nuclear g factors. Extensive atomic physics calculations are in progress, with the hope that the free-ion fields can be understood well enough in multielectron systems, such as Nalike ions, that they can be used to perform accurate, absolute g-factor measurements on short-lived nuclear states using the time-dependent RIV technique [20,53]. For example, a precise, accurate, and absolute measurement of $g(2_1^+; {}^{74}\text{Ge})$ would set an absolute scale for the present relative g-factor measurements.

Even if an absolute RIV measurement remains elusive for the stable isotopes, the present relative g factors, together with extensive studies of the relevant free-ion hyperfine fields [21,22], make it feasible to attempt an analysis of the g factors in the neutron-rich isotopes 78,80,82 Ge based on the vacuum deorientation of angular correlations observed following Coulomb excitation [2]. Both interactions predict marked variations in the g factors between N=46 and N=50 that may be detectable even with a low-intensity radioactive beam measurement [19].

Comparisons of the measured relative g factors with largebasis shell-model calculations gives a reasonable degree of agreement and suggest that the g-factor variations are strongly correlated with the orbital angular momentum carried by the protons. A detailed description of the more subtle massdependent variations in the g factors of the first-excited states remains a challenge for these complex transitional nuclei that display mixing of prolate, oblate, and spherical structures.

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