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## The high pressure phase transformation behavior of silicon nanowires

L. Q. Huston,<sup>1,a)</sup> A. Lugstein,<sup>2</sup> J. S. Williams,<sup>1</sup> and J. E. Bradby<sup>1</sup>

<sup>1</sup>Research School of Physics and Engineering, The Australian National University, Acton ACT 2601, Australia <sup>2</sup>Institute for Solid State Electronics, Vienna University of Technology, Floragasse 7, A-1040 Vienna, Austria

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Si nanowires of 80–150 nm and 200–250 nm diameter are pressurized up to 22 GPa using a diamond anvil cell. Raman and x-ray diffraction data were collected during both compression and decompression. Electron microscopy images reveal that the nanowires retain a nanowire-like morphology (after high pressure treatment). On compression, dc-Si was observed to persist at pressures up to 19 GPa compared to ~11 GPa for bulk-Si. On decompression, the metallic  $\beta$ -Sn phase was found to be more stable for Si nanowires compared with bulk-Si when lowering the pressure and was observed as low as 6 GPa. For the smallest nanowires studied (80–150 nm), predominately a-Si was obtained on decompression, whereas for larger nanowires (200–250 nm), clear evidence for the r8/bc8-Si phase was obtained. We suggest that the small volume of the individual Si nanowires compared with bulk-Si inhibits the nucleation of the r8-Si phase on decompression. This study shows that there is a size dependence in the high pressure behavior of Si nanowires during both compression and decompression. *Published by AIP Publishing*. https://doi.org/10.1063/1.5048033

Nanoscale materials are known to have electrical, mechanical, and physical properties that differ from those of their bulk counterparts.<sup>1</sup> The phase transformation behavior of nanomaterials at high pressure is no exception. For example, some nanomaterials have been observed to require different pressures than the bulk material for a transformation to proceed.<sup>2,3</sup> Other nanomaterials have been found to undergo different phase transformation pathways to their bulk counterparts upon compression.<sup>4</sup> In bulk-Si, it is well established that high pressure can be used to access a number of metastable phases that have properties of technological significance such as r8-Si (rhombohedral structure, Si-XII,  $R\bar{3}$ ) and bc8-Si (a body centred cubic structure, Si-III, Ia3).5-7 For example, both r8 and bc8-Si have been found to have interesting narrow bandgap semiconducting properties.<sup>5,7,8</sup> Furthermore, nanowires are promising candidates for future electronic and optoelectronic devices, which can even have their properties tuned using strain, but Si nanowires (SiNWs) are only easily grown in the stable dc-Si structure.<sup>9,10</sup> Thus, it would be interesting to explore the combination of nanowire geometry with the attractive properties of r8-Si and/or bc8-Si, with the aim to fabricate bc8 or r8 Si SiNWs.

To understand the high pressure behavior of SiNWs, it is first necessary to review the behavior of bulk-Si. When subjecting bulk diamond cubic (dc, Si-I, Fd3m) Si to pressure in a diamond anvil cell (DAC), it undergoes a series of wellcharacterised phase transformations.<sup>11–13</sup> At ~11 GPa, dc-Si transforms to a metallic phase with a white tin ( $\beta$ -Sn, Si-II, I4<sub>1</sub>/amd) structure.<sup>11,13,14</sup> At higher pressures, Si will undergo a series of reversible metal to metal phase transformations such as  $\beta$ -Sn to Imma-Si (Si-XI) at 13.2 GPa and Imma to simple hexagonal (sh, Si-V, P6/mmm) at 15.6 GPa.<sup>12</sup> Notably, when unloading from the  $\beta$ -Sn phase, Si does not revert back to dc-Si; instead, it transforms to one of a number of metastable phases.<sup>15</sup> A fast pressure release (usually achieved in nanoindentation experiments) from the  $\beta$ -Sn phase yields amorphous silicon (a-Si) at and below ~9 GPa.<sup>16,17</sup> However, slower unloading results in r8-Si at 9 GPa which transforms to bc8-Si at 3 GPa.<sup>13</sup>

There have been limited studies on the phase transformation pathways of nanoscale Si under pressure. Studies on 10–50 nm Si nanoparticles and 7 nm diameter SiNWs suggested that dc-Si was stable to higher pressures than bulk Si.<sup>18,19</sup> In contrast, other work reported that SiNWs around 60–80 nm in diameter phase transform into  $\beta$ -Sn-Si at a *lower* pressure than bulk-Si, but this study did not report the behavior on decompression.<sup>20</sup> For larger diameter SiNWs (up to 700 nm), phase transformation under pressure occurred exactly like bulk Si.<sup>21</sup> In this study, the high pressure behavior of SiNWS in two size regimes (80–150 nm and 200–250 nm diameter) was studied during compression and decompression for pressures up to 22 GPa using Raman Spectroscopy, X-ray diffraction (XRD), scanning electron microscopy (SEM), and transmission electron microscopy (TEM).

The 80–150 nm SiNWs were synthesized in a hot wall CVD reactor by the VLS growth mechanism using diluted silane gas as a precursor.<sup>22</sup> Prior to the deposition of the catalyst, the native oxide on the Si(111) substrates was removed with a buffered hydrofluoric acid etch to create a hydrogenterminated surface. Gold served as a catalyst, which was deposited at room temperature as a film of 2 nm thickness via thermal evaporation. The growth was done at a total pressure of 3 mbar using a 100 sccm flow of silane (2% in a He mixture) and with 10 sccm hydrogen at a growth temperature of 500 °C. The growth was stopped by switching off the precursor gas, and the samples were cooled down in vacuum. The 200–250 nm thick Si nanowires were fabricated top down by common e-beam lithography and reactive ion etching.

The nanowires were removed from the substrate by ultrasonicating in a 4:1 mixture of methanol:ethanol or manually with a razor blade. They were then transferred into a DAC ( $400 \,\mu\text{m}$  cullet size, stainless steel gasket  $\sim 50 \,\mu\text{m}$ 

<sup>&</sup>lt;sup>a)</sup>Electronic mail: larissa.huston@anu.edu.au

thickness, and 200  $\mu$ m diameter hole) using a stainless steel needle. The pressure inside the cell was determined using the ruby fluorescence method, with a small ruby ball also loaded into the DAC.<sup>23</sup> Both Ne and 4:1 methanol:ethanol were used as a pressure medium to prevent the sample chamber from collapsing and to stop the nanowires from agglomerating together but also to create a quasihydrostatic pressure environment. The SiNWs were compressed up to 22 GPa and monitored using insitu Raman spectroscopy with a Renishaw inVia Reflex Raman system equipped with a 532 nm laser and an olympus SLWD  $20\times$  objective, with a spot size of  $\sim 2.6 \,\mu\text{m}$  and an intensity of  $\sim 2$  mW. XRD was conducted using 30 keV synchrotron radiation with a Pilatus 1M-F detector at the 16-ID-B beamline at HPCAT at the Advanced Photon Source. After unloading the SiNWs, the samples were recovered and examined using a FEI Verios SEM operating at 2kV, 13 pA, and TEM was performed with a FEI CM300 TEM operating at 300 kV.

Raman and XRD measurements for the 80-150 nm SiNWs up to 22 GPa and 17 GPa are shown in Fig. 1, respectively. The Raman measurements during compression are shown in Fig. 1(a). At 1 GPa, the Raman signal has a sharp dc-Si peak at 523 cm<sup>-1</sup>. At 14 GPa, this peak is still present but it has shifted to higher wavenumbers. It has also broadened, possibly due to the pressure medium no longer being hydrostatic.<sup>24</sup> This peak continues to shift towards higher wavenumbers until 20 GPa where it completely disappears, with no clear peaks from metallic phases observed above the background signal. Additionally, the second order 2TA dc-Si peak (marked with a star at  $\sim 230 \,\mathrm{cm}^{-1}$ ) becomes more prominent below 19 GPa. At 15 GPa, two weak peaks at  $\sim$ 115 and  $\sim$ 397 cm<sup>-1</sup> are observed. The higher wavenumber peak is observed until 18 GPa, whilst the lower wavenumber peak becomes indistinguishable from the background signal. These



FIG. 1. *In-situ* Raman spectroscopy and X-ray diffraction data of 80–150 nm SiNWs taken on compression (a) and (b) and decompression (c) and (d).

peaks are likely to be one of the two metallic phases,  $\beta$ -Sn-Si or Imma-Si, which have both been reported to exist in bulk-Si between 13.5 and 16.0 GPa.<sup>12,25</sup> At 19 GPa, only a trace amount of dc-Si is observed above the background signal. The majority of the sample has likely transformed to sh-Si, which is not Raman active.<sup>25</sup> At 20 GPa, only the background signal is observed, suggesting that the SiNWs have fully phase transformed to sh-Si.

Figure 1(b) contains a series of XRD measurements up to 17 GPa. Initially, the SiNWs are dc-Si. Note that, as well as the dc-Si peaks, there are additional peaks due to the Au seed used to grow the NWs. The NWs remain entirely in the dc-Si phase until 15 GPa where a small peak is observed at  $Q = 2.81 \text{ Å}^{-1}$  and a pair of very weak peaks are observed at Q = 3.84 and  $3.88 \text{ Å}^{-1}$ . These peaks correspond to either  $\beta$ -Sn or Imma-Si, but due to the low intensity of these peaks and overlap with the first Au peak, it is not possible to determine which phase is present.<sup>12,26</sup> At the maximum pressure applied of 17 GPa, the dc-Si peaks have noticeably decreased in intensity and the  $\beta$ -Sn-Si or Imma-Si peaks have been replaced by strong sh-Si peaks. A small dc-Si peak indicates that not all the dc structure had transformed at this pressure, consistent with the Raman data. Thus, at 17 GPa, the SiNWs are predominately sh-Si with some traces of dc-Si.

The Raman results of the 80–150 nm SiNWs during decompression are shown in Fig. 1(c). At the maximum pressure of 22 GPa, the NWs were presumably completely transformed to sh-Si (not Raman active).<sup>25</sup> At 16 GPa, two low intensity Raman modes are observed as indicated by the grey triangles. This indicates the transformation of at least some of the SiNWs to  $\beta$ -Sn-Si or Imma-Si. These peaks are more prominent at 13 GPa and are observed until 6 GPa. Between 6 GPa and 5 GPa, a final phase transformation occurs to a-Si, as indicated by the broad peaks centred at around 160 and 480 cm<sup>-1</sup>.<sup>27</sup>

The XRD results for decompression are shown in Fig. 1(d). It is first worth noting that for all pressures, the height of the (dc-Si) peaks from the remaining untransformed dc-Si (at 17 GPa) did not change significantly. This suggests that no additional dc-Si is formed during decompression. However, there were changes observed in the metallic phases. Between 16 GPa and 13 GPa, the sh-Si phase transforms into  $\beta$ -Sn-Si (most likely via the Imma-Si phase) which continued to exist until at least 8 GPa and disappears entirely between 8 GPa and 4 GPa. This disappearance is most likely due to the amorphisation of the NWs, as observed in the Raman spectra. It should be noted that the XRD signal of a-Si has very broad features and is very weak, given that the nanowires are loosely packed in the DAC. Also, in both experiments shown in Fig. 1, the SiNWs were decompressed in relatively large pressure increments. Given that it is known from nanoindentation experiments in Si that a fast decompression rate can favor the formation of a-Si over the crystalline metastable phases (bc8-Si and r8-Si), a new batch of SiNW was compressed to 20 GPa and decompressed from  $\sim 8$  GPa very slowly in  $\sim 0.2$  GPa increments over a day.<sup>17</sup> It was found (using Raman Spectroscopy) that the SiNWs were still predominately a-Si but a trace amount of bc8-Si was also observed.

The Raman spectra of the 200–250 nm SiNWs in compression and decompression are shown in Figs. 2(a) and 2(b), respectively. On compression, dc-Si was found to start transforming to  $\beta$ -Sn-Si/Imma-Si at 15 GPa as seen by the presence of two weak peaks indicated by grey triangles. At 20 GPa, these peaks have disappeared, again indicating a transition to sh-Si. On decompression,  $\beta$ -Sn-Si is found to form at 16 GP (possibly with some Imma-Si present), and the SiNWs remain entirely in a metallic phase (presumably  $\beta$ -Sn-Si<sup>11</sup>) 7.9 GPa. At this pressure, additional peaks (indicated by green crosses) are observed, corresponding to r8-Si.<sup>28</sup> Some  $\beta$ -Sn-Si is still present at this pressure, and it remains until between 5.8 GPa and 5.1 GPa where it appears to be replaced by a-Si (red squares) as indicated by the presence of two broad peaks.

To determine the morphology and structural integrity of the SiNWs after compression, scanning electron microscopy (SEM) was performed. Figures 3(a) and 3(b) show SEM and TEM images of the SiNWs before compression, respectively, and Fig. 3(c) shows an SEM image of a gasket full of 80-150 nm SiNWs after being removed from a DAC after compression to 17 GPa. The inset shows a region at a higher magnification. From these images, it is quite clear that the SiNWs maintained the nanowire shape during compression and did not merge together to form a bulk-like structure. Transmission electron microscopy was also performed on individual SiNWs. A bright field image with an inset of the selected area diffraction pattern (SADP) of an 80-150 nm SiNW loaded up to 22 GPa is shown in Fig. 3(d). The SADP shows a number of diffuse rings which correspond to a-Si, consistent with the XRD and Raman data. This image shows that the SiNW returned to essentially the same geometry as before it was loaded.

The high pressure behavior of SiNWs from this study and that of bulk-Si from the literature (Refs. 11 and 29) is summarized in Fig. 4. This figure shows the phases present in bulk-Si, 200–250 nm SiNWs, and 80–150 nm SiNWs at the pressures shown on the bottom axis. Compression is shown on the left and decompression is shown on the right. Solid colors represent a single phase being present whilst vertical lines indicate a transition region where two phases



FIG. 2. Raman spectra of 200–250 nm SiNWs taken on (a) compression and (b) decompression.



FIG. 3. (a) SEM image of SiNWs before compression. (b) Bright-field TEM image of a SiNW before compression selected area diffraction pattern (SADP) inset taken from the SiNW shown. (c) SEM image of 80–150 nm SiNWs after compression to 17 GPa. The SiNWs are within the red circled region and the outer region is the gasket. The inset is a higher magnification image. (d) Bright-field TEM image of a SiNW compressed to 22 GPa with a SADP inset taken from the SiNW shown.

are present. On compression, the onset and completion of phase transformation to metallic phases for both diameters were found to be much higher than in bulk-Si. This is consistent with a study of 10–50 nm Si nanoparticles<sup>18</sup> and a further study where no phase transformation was reported up to 15.6 GPa.<sup>19</sup> In contrast, two other studies found SiNWs to phase transform to metallic phases at similar pressure to bulk-Si.<sup>20,21</sup> In the first of these studies, a large size distribution of 50–700 nm SiNWs was used, suggesting that the large SiNWs may have biased the behavior to that of bulk-Si.<sup>21</sup> The other study found the onset of phase transformation to be slightly lower than bulk-Si,<sup>20</sup> but this observation could be a result of the manner in which the SiNWs and hence bulk-like behavior.

On decompression, the SiNWs in this current study were found to transform from sh-Si to  $\beta$ -Sn-Si/Imma-Si at a



FIG. 4. A summary of the high pressure phase transformation behavior of Si at different sizes. Bulk-Si data are from Refs. 11, 12, and 29.

similar pressure to bulk-Si. However,  $\beta$ -Sn-Si was found to be present at pressures as low as  $\sim 5$  GPa in the SiNWs, consistent with previous observations for 10-50 nm Si nanoparticles.<sup>18</sup> For the larger 200–250 nm SiNWs, partial transformation to r8-Si was observed at a slightly lower pressure than bulk-Si.<sup>29</sup> The remaining  $\beta$ -Sn-Si appeared to transform to a-Si at  $\sim$ 5 GPa, as revealed by a significant additional a-Si phase present, similar to the 80-150 nm SiNWs. We therefore deduce from our work (and the few previous studies) that the phase transformation behavior of Si depends strongly on the particle/SiNW size. Isolated SiNWs of a larger size (approximately 600-700 nm+) exhibit bulk-like phase transformation behavior. At smaller sizes, Si particles/SiNWs exhibit elevated pressures for the dc-Si to metallic phase transformation upon compression and depressed phase transformation pressures during decompression, with a-Si being the dominant end phase for the smallest sizes (below 200 nm) and r8/bc8-Si occurring for intermediate sizes.

We suggest that the suppression of the dc-Si to metallic phase transition is a direct result of difficulty in nucleating the  $\beta$ -Sn phase. It should be noted that, even in bulk-Si,  $\beta$ -Sn-Si is difficult to nucleate, being described as "sluggish" in the literature.<sup>30</sup> This phase transformation is considered as a reconstructive transition since it involves the breaking of dc-Si bonds to form  $\beta$ -Sn-Si, thus requiring a significant amount of energy.<sup>31</sup> We propose that this phase is even more difficult to nucleate in the SiNWs, as a result of both the higher surface to volume ratio and the smaller volume of individual SiNWs compared with bulk-Si. Since  $\beta$ -Sn-Si is already difficult to nucleate in bulk-Si, fewer potential nucleation sites that are available in a SiNW may raise the pressure necessary to initiate phase transformation to  $\beta$ -Sn/Imma for SiNWs. For smaller SiNWs, the data suggest that there is a direct dc-Si to sh-Si phase transformation at and above 17 GPa. For the 200–250 nm SiNWs, the situation is not so clear cut and a dc-Si to  $\beta$ -Sn/Imma-Si may be occurring at 15 GPa prior to sh-Si formation at higher pressures.

It was mentioned earlier that a sh-Si to  $\beta$ -Sn-Si/Imma-Si phase transformation on decompression occurs at similar pressures for all sizes of nanoparticles/NWs. This metallic to metallic phase transition is displacive, involving the movement of some atoms in the unit cell from the sh-Si positions to those in the Imma and  $\beta$ -Sn phases.<sup>31</sup> A theoretical study of high pressure phases of Si found that the total free energies  $\beta$ -Sn-Si, Imma-Si, and sh-Si are similar.<sup>32</sup> These similarities in total energy and the displacive nature of the atomic transitions may explain why there is little to no size effect on the sh-Si to Imma-Si/ $\beta$ -Sn-Si (metallic to metallic) phase transformation of SiNWs compared with bulk-Si.

As decompression continues, the metallic nature of the bonding changes to covalent bonding with the  $\beta$ -Sn-Si to r8-Si phase transformation. Following on from the previous argument, it would be expected that there is a significantly high kinetic barrier to nucleation of r8-Si. As the small size (volume) of SiNWs limits the number of potential nucleation sites for r8-Si, the SiNWs may remain as  $\beta$ -Sn-Si until significantly lower pressures compared to bulk-Si. Hence, we might expect that there would exist an increased difficulty in nucleating r8-Si from  $\beta$ -Si-Si on decompression compared with bulk-Si. We further suggest that the formation of a-Si upon decompression of SiNWs may be similar to rapid unloading during nanoindentation experiments.<sup>16,17</sup> In nanoindentation, a sharp diamond tip pressed into Si forms  $\beta$ -Sn-Si and rapid decompression leads to the formation of a-Si when there is insufficient time to nucleate r8-Si within the small  $\beta$ -Sn volume.<sup>17</sup> However, by slowly unloading the indenter tip, r8/bc8-Si can be formed.<sup>17</sup> In terms of our observed behavior of SiNWs during decompression, we suggest that for the 200-250 nm SiNWs, the smaller volume (like the nanoindentation case) results in a nucleation problem in r8-Si formation. Incomplete transformation to r8-Si occurs by 5 GPa and the remaining  $\beta$ -Sn-Si then transforms to a-Si somewhat like fast unloading for nanoindentation. In smaller SiNWs (80-150 nm), there appears to be almost total suppression of r8-Si nucleation and a-Si forms directly from  $\beta$ -Sn-Si at and below 6 GPa. In light of these observations, it would be interesting to explore the temperature dependence of phase transformation of SiNWs during decompression, since it has previously been possible in nanoindentation studies to enhance the formation of r8/bc8-Si phases by increasing the temperature.<sup>33</sup>

In conclusion, a clear size effect in some but not all of the pressure-induced phase transformations of SiNWs was observed during both compression and decompression. On compression, dc-SiNWs are found to suppress phase transformation to metallic phases until higher pressures than for bulk-Si, possibly even a direct dc to sh phase transformation for smaller SiNWs at and above 17 GPa. During decompression, the sh-Si to Imma/ $\beta$ -Sn-Si transformation was found to be similar to bulk Si. However,  $\beta$ -Sn-Si was found to remain until much lower pressures than bulk-Si. For the intermediate size SiNWs, strong evidence was observed for a phase transformation to r8-Si that occurred at pressures between ~8 and 5 GPa on decompression but significant a-Si occurred below ~5 GPa. For the smallest SiNWs below 200 nm, a phase transformation to predominately a-Si occurred below 6 GPa.

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