Pseudocontact shifts in biomolecular NMR using paramagnetic metal tags

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Introduction
1. Scope of this review

1.1. Paramagnetic NMR of biological macromolecules

Unpaired electrons endow their host molecules with paramagnetism, and the detection of associated phenomena in the NMR spectrum is commonly referred to as paramagnetic NMR spectroscopy. The magnetic moment of a free unpaired electron is about 660 times greater than that of a proton. Therefore, single unpaired electrons, which may be associated with either organic radicals or metal ions, generate very significant effects in NMR spectra, which extend over a long distance range compared to any magnetic interactions between nuclear spins. The long-range nature of the paramagnetic effects arising from unpaired electrons renders them a powerful NMR spectroscopic tool for the study of the structure and dynamics of biological macromolecules. This review concentrates on proteins, because NMR studies of paramagnetic macromolecules NMR have mostly been performed with proteins. Nonetheless, the same experiments and conclusions evidently also apply to DNA, RNA and carbohydrates as well as complexes thereof with ligand molecules. The authors are not aware of articles describing experiments to modify DNA or RNA with the intent to generate pseudocontact shifts, which are at the centre of this review.

1.2. Radicals, transition metals, lanthanides

Unpaired electrons are found, inter alia, in organic radicals and transition metal ions. Organic radicals that are stable in aqueous solution are rare. Nitroxide radicals are used most frequently. They stand out for their stability and their inertness towards chemical reaction with proteins and DNA. Site-specific labeling with synthetic nitroxide tags presents a powerful tool for obtaining structural restraints from paramagnetic effects, and the literature associated with nitroxide tags is rich and large. This review discusses nitroxides only in passing, focusing instead on paramagnetic metal ions, lanthanides in particular.

Lanthanide ions are of particular interest because of their varied paramagnetic effects. Together with the actinide series, they make up the inner transition metals or f-block of the periodic table. For the purpose of this review, we refer to d-block elements as 'transition metals' and to lanthanide ions as a separate group.

Historically, metallo-proteins containing transition metal ions have played a key role in confirming theoretical predictions of the long-range effects of paramagnetism in NMR spectra. Iron-containing heme proteins such as myoglobin and cytochrome c were studied very early on, but the validity of the point-dipole approximation, which assumes that the
magnetic dipole moment is located at a single point, is compromised in these systems. Transition metal ions harbour unpaired electrons in d-orbitals that engage in binding interactions with the immediate chemical environment, leading to partial delocalisation of the unpaired electron across the ligand orbitals. In this situation, a quantitative description of the paramagnetic effects necessitates quantum mechanical computations to locate the unpaired spin-density [1, 2]. The conjugated double-bond system of a heme ring is particularly effective in delocalising unpaired electron density.

This review focuses on pseudocontact shifts (PCS) generated by metal tags. Among the transition metal ions, only high-spin Co\(^{2+}\) is well suited for metal tags on proteins, combining fairly large PCSs with small paramagnetic relaxation enhancements (PRE) and stability of its complexes in aqueous solution. The Mn\(^{2+}\) ion generates very large PREs but no PCSs. The Cr\(^{3+}\) ion generates relatively small PCSs [3]. In the case of iron, the ligand field determines whether Fe\(^{2+}\) is paramagnetic or diamagnetic and whether the electron configuration in Fe\(^{3+}\) ions is high-spin or low-spin [4]. Depending on the ligand field, PCSs generated by high-spin Fe\(^{3+}\) can be moderately large [5] or exceedingly small [6]. The Ru\(^{3+}\) ion generates sizeable PCSs [7], but most of its complexes are unstable. For these reasons, chromium, iron and ruthenium ions have not been used in paramagnetic tags for the purpose of generating PCSs. Ni\(^{2+}\) and Cu\(^{2+}\) generate only small PCSs [8, 9]. The paramagnetism and specific binding affinities of these two ions make them particularly suitable for the generation of PREs with the help of N-terminal peptide tags [10, 11].

Regarding PCSs, lanthanide ions are the only other metal ions that can produce effects as large as Co\(^{2+}\) or larger. The point-dipole approximation works well for lanthanide ions, as they harbour their unpaired electrons in f-orbitals, which do not interact as strongly with ligand orbitals as the d-orbitals of transition metals. Since lanthanides have no known function in biology, proteins with natural specific binding sites for lanthanide ions are rare. As the general chemical properties of lanthanide ions are broadly similar to those of calcium ions, calcium binding sites sometimes accept lanthanides in vitro. For example, calbindin D\(_{9k}\), a protein with two calcium binding sites, proved to be an excellent system for evaluating paramagnetic effects induced by lanthanide ions as, fortuitously, the Ca\(^{2+}\) ion of one of the two sites can readily be replaced by a lanthanide ion. Pseudocontact shift studies of this protein in the Bertini laboratory established a reference for determining the principal axes of the magnetic susceptibility tensors associated with paramagnetic lanthanide ions and the magnitude of their anisotropies [12].
Different lanthanide ions display different magnitudes of paramagnetic effects. Many lanthanide ions are much more paramagnetic than any transition metal ions and generate correspondingly large effects in NMR spectra. In addition, lanthanide ions are chemically very similar and their oxidation state (3+) is chemically very stable, so that a lanthanide binding site on a protein or in a synthetic lanthanide chelating compound can bind any of the lanthanide ions with similar affinity, although details of lanthanide coordination can vary with the ionic radius.

1.3. Diamagnetic reference

An important point is the availability of molecules and metal ions that can serve as a suitable diamagnetic reference, as paramagnetic effects are always measured by comparison with a diamagnetic reference. Even small paramagnetic effects can be measured accurately by comparison with a suitable corresponding diamagnetic sample.

Among the lanthanide ions, La$^{3+}$ and Lu$^{3+}$ are diamagnetic, but Y$^{3+}$ often is an even better diamagnetic reference, as its ionic radius is almost identical to the Ho$^{3+}$ ion. Strictly speaking, yttrium is not a member of the lanthanide series. Therefore, the group of lanthanides and chemically similar elements are sometimes referred to as lanthanoids. This review does not make this distinction, referring simply to lanthanides throughout.

Co$^{2+}$ generates fairly large PCSs without very large PREs, similar to the Yb$^{3+}$ ion. Unfortunately, no diamagnetic transition metal ion with a 2+ charge exists with exactly the same chemical properties. Zn$^{2+}$ is commonly used as the diamagnetic reference for the Co$^{2+}$ ion because of its similar ionic radius.

Similarly, Mn$^{2+}$ generates very large PREs, but no diamagnetic metal ion can exactly reproduce its chemical properties. Zn$^{2+}$ or Mg$^{2+}$ often serve as diamagnetic references.

In the case of nitroxide ions, chemical reduction removes the paramagnetic character by producing a diamagnetic hydroxylamine group. Ascorbate is a commonly used reagent to achieve the required one-electron reduction.

1.4. Paramagnetic tags

Diamagnetic proteins have the advantage that they can be site-specifically tagged with a paramagnetic compound at many different sites of choice. The paramagnetic effects observed by NMR are most easily interpreted if a protein can be furnished with a single paramagnetic centre rather than several. Site-specific tagging is open to a wide range of tags and tagging strategies. Among the 20 natural amino acids, cysteine residues offer the most
facile way of selective chemical modification without affecting any of the other amino acids, as the thiol group is highly nucleophilic and easy to engage in a disulfide bond.

At present, the MTSL tag (Fig. 1) is the paramagnetic tag most frequently used in protein NMR. It contains a chemically activated sulfur atom, which readily reacts with cysteine residues with formation of a covalent disulfide bond. The nitroxide group generates PREs without changing the chemical shifts. Reduction with ascorbate is a convenient way to eliminate the radical character of the tag and produce a diamagnetic reference.

![Chemical structure of MTSL](image)

**Fig. 1.** Chemical structure of MTSL. The tag reacts with the thiol group of cysteine residues with formation of a mixed disulfide bond and the release of methanesulfinic acid (CH$_3$SO$_2$H).

The obvious drawback of any tag designed to react with a single cysteine residue is the need to work with a protein that contains only a single reactive thiol group. This usually requires mutation of naturally occurring cysteine residues to other amino acids and positioning of a cysteine residue at the site of interest. Often, however, mutations are found to destabilise the protein fold. In other cases, some cysteine residues may be essential for protein function.

Recently, a more general approach has been developed that uses genetically encoded amino acids containing a nitroxide group and therefore does not require the mutation of cysteine residues [13]. So far, however, the system has been established only for *E. coli*, where the reducing environment of the cytosol leads to chemical reduction of a large fraction of the nitroxide amino acid, resulting in a mixture of paramagnetic and diamagnetic protein.

This review focuses on pseudocontact shifts and therefore is mostly concerned with tagging approaches using paramagnetic metal ions, in particular lanthanide ions. Lanthanide ions are inert with respect to the oxidising or reducing conditions encountered under physiological conditions. All paramagnetic lanthanide ions also generate PREs. Gd$^{3+}$ and Mn$^{2+}$ ions are the metal ions best suited for PRE measurements, due to their large and isotropic . As chelating compounds bind Mn$^{2+}$
ions more weakly than heavier transition metal ions [14], it is much easier to produce inert complexes with Gd$^{3+}$ than with Mn$^{2+}$ ions.

In the case of metalloproteins, labelling with a metal tag bears the risk of exchange between metal ions in the protein and the metal ion in the tag. This situation can be addressed with tags that are kinetically inert with respect to metal exchange, such as the cyclen tags described in Section 5.3.2.4.

1.5. Advantages of pseudocontact shifts over PREs

1.5.1. High sensitivity

PCSs are simply measured as the chemical shift difference between a sample tagged with a paramagnetic metal ion and the corresponding sample tagged with a diamagnetic ion as a reference. This means that PCSs can be measured even with samples of low concentration, and in shorter time than, for example, NOEs, RDCs, scalar couplings or quantitative PREs.

1.5.2. Suppression of intermolecular effects

Sizeable PREs can be observed regardless of whether the geometry between paramagnetic centre and nuclear spin is fixed (as for intramolecular effects) or variable (as for non-specific intermolecular effects). This can make it difficult to distinguish between specific intramolecular and non-specific intermolecular effects. In contrast, intermolecular PCSs easily average to zero, as the PCSs depend not only on the distance of the nuclear spin from the paramagnetic centre, but also on the orientation of the metal complex relative to the coordinate frame of the nuclear spin. Orientational averaging of the paramagnetic centre, as encountered for non-specific intermolecular effects, exposes nuclear spins to both positive and negative PCS effects, which average to zero.

1.5.3. Tolerance towards incomplete tagging yields

Classical PRE tags, such as nitroxide tags and Gd$^{3+}$ or Mn$^{2+}$ tags, do not change the chemical shift of the nuclear spins compared with the diamagnetic reference. As a consequence, failure to achieve 100% ligation of the tag leads to NMR spectra in which the peaks of paramagnetic and diamagnetic species overlap. This complicates the analysis of quantitative PRE measurements. In contrast, PCSs lead to resolved cross-peaks for the paramagnetic species irrespective of the yield achieved in the ligation reaction.

1.5.4. Superior distance range
PCSs decrease with increasing distance $r$ from the paramagnetic centre with a $r^3$ dependence (see Eq. 1 below). In contrast, PREs decrease with $r^6$. The lesser distance dependence of PCSs is useful in many respects, including structure analyses of large proteins, the possibility of attaching tags at sites remote from the site of interest, and in interpreting data obtained from tags that are linked to the target protein by a flexible tether. If the tether is short, the distance variation between the paramagnetic centre and nuclear spins in the protein can be small compared with the distance itself, but this requires that the paramagnetic effects be observable for remote spins. As a result, excellent correlations between experimental and back-calculated PCSs can be observed even for flexible tags.

A particular advantage associated with the long-range effects of PCSs is for studies of protein-protein complexes in situations, where chemical exchange leads to significant line broadening of the NMR signals from nuclear spins that are located at the protein-protein interface. In this case, PCS effects can be observed for nuclear spins with narrower NMR signals that are located at some distance from the interface itself (e.g. in the nearby interior of the protein) and thus too far to engage in intermolecular NOEs. PCSs induced by the most strongly paramagnetic lanthanide ions can be observed over greater distances than PCSs generated by any d-block transition metal ion.

1.6. Recent reviews on paramagnetic NMR

Studying proteins with the help of paramagnetic lanthanide ions is becoming increasingly popular. Notably, such analyses represent only a subset of paramagnetic NMR studies. Some excellent recent reviews on paramagnetic effects in NMR are listed below.

Comprehensive reviews on the physical background of paramagnetic effects in biomolecular NMR have been published by Bertini and co-workers [4, 15-17] and summarized in later reviews [18-20]. Reviews of applications in structural biology have been published with emphasis on metalloproteins [21-25], carbohydrates [26], solid state NMR [27-29], PREs for characterising transient, low-population states [30], protein-protein complexes [31], techniques for measuring PCSs [32], sparse protein labelling [33], paramagnetic tags [34-37] and paramagnetically induced residual dipolar couplings (RDC) and relaxation enhancements [18]. Additional reviews have focused on the use of PCSs and paramagnetically induced RDCs for structure analysis of flexible proteins [38] and comparisons of protein conformations in solution and in single crystals [39]. A number of reviews have specifically discussed the advantages of lanthanide ions for structure determinations by paramagnetic NMR, emphasising in particular the value of the
pseudocontact shifts generated by lanthanides [19, 31, 40-42]. Additional benefits in structural biology have been noted to be associated with the luminescent properties of Tb$^{3+}$ and Eu$^{3+}$ ions [43]. A comprehensive review of the chemical requirements for lanthanide coordination and the properties of lanthanide complexes was published by Parker and co-workers in 2002 [44].

The present review aims to provide a comprehensive overview of lanthanide and Co$^{2+}$ binding tags and the paramagnetic effects generated by these tags in the NMR spectra of biological macromolecules, together with a compilation of applications.

2. Pseudocontact shifts

2.1. $\chi$ tensor and $\Delta \chi$ tensor

The pseudocontact shift (PCS) of a nuclear spin is manifested in NMR spectra as the change in chemical shift due to the presence of a paramagnetic centre (Fig. 2). In contrast to the Fermi contact shift, which is mediated through chemical bonds, the PCS is a through-space effect. For a point dipole in a rigid molecule, it can be described by a simple equation that reflects the location, orientation and degree of anisotropy of the magnetic susceptibility associated with the paramagnetic centre:

$$\Delta \delta_{\text{PCS}} = 1/(12\pi r^3)[\Delta \chi_{xx}(3\cos^2\theta - 1) + 1.5\Delta \chi_{th} \sin^2\theta \cos 2\phi]$$  

where $\Delta \delta_{\text{PCS}}$ is the PCS (a dimension-less number usually measured and reported in ppm), $r$ is the distance of the nuclear spin from the metal ion, $\Delta \chi_{xx}$ and $\Delta \chi_{th}$ are the axial and rhombic components of the magnetic susceptibility anisotropy ($\Delta \chi$) tensor, and $\theta$ and $\phi$ are the polar angles describing the position of the nuclear spin with respect to the principal axes of the $\Delta \chi$ tensor (Fig. 3).
Fig. 2. PCSs in a $\left[^{15}\text{N},^1\text{H}\right]$-HSQC spectrum. The PCS of a nuclear spin is measured as its chemical shift in the paramagnetic sample, measured in ppm, minus its chemical shift in the diamagnetic sample. The figure shows the superimposition of two spectra, one recorded with paramagnetic Tb$^{3+}$ (red spectrum), the other with diamagnetic La$^{3+}$ (black spectrum). The metal ions were bound to the protein e$_{186}$ selectively labelled with $^{15}\text{N}$-leucine. Note that PCSs can be positive (as in the case of, e.g., Leu43) or negative (Leu95). The peaks in the paramagnetic sample are displaced along nearly diagonal lines, because $^{15}\text{N}$ and $^1\text{H}$ nuclei experience very similar PCSs as their separation is small relative to the distance of each from the paramagnetic centre. Cross-peaks of amide protons within about 14 Å of the paramagnetic centre are broadened beyond detection due to PRE. (Reproduced with permission from ref. [42]. Copyright 2007 American Chemical Society.)

Fig. 3. Geometric parameters defining the PCS of a nuclear spin, I, due to unpaired electrons located in the paramagnetic centre, e.

The magnetic susceptibility tensor, $\chi$, can be regarded as an object with three orthogonal axes, centred about the paramagnetic centre, where the length of each of the axes describes the magnitude of the magnetic moment induced by an external magnetic field, if the axis happens to be aligned with the magnetic field. The $\chi$ tensor is spherical, or isotropic, if all three principal axes have the same length. While the magnitude of the $\chi$ tensor determines
the paramagnetic relaxation enhancements, PCSs are generated only if the $\chi$ tensor is anisotropic. The $\Delta\chi_{ax}$ and $\Delta\chi_{rh}$ components are defined by

$$\Delta\chi_{ax} = \chi_z - (\chi_x + \chi_y)/2 \quad \text{and} \quad \Delta\chi_{rh} = \chi_x - \chi_y$$

(2)

where $\chi_x$, $\chi_y$ and $\chi_z$ denote the susceptibility values along the three principal tensor axes. The $\chi$ and $\Delta\chi$ tensors share the same principal axes and the $\Delta\chi$ tensor vanishes for $\chi_x = \chi_y = \chi_z$.

In an alternative representation, the $\Delta\chi$ tensor can be depicted by isosurfaces that trace the coordinates of a given PCS value as calculated by Eq. 1. It is helpful to distinguish isosurfaces of positive and negative PCSs by different colours (Fig. 4).

![Fig. 4. PCS isosurfaces plotted on the structure of a protein (ERp29 C-terminal domain). The backbone of the protein is drawn in a ribbon representation (cyan). The isosurfaces correspond to PCSs of ±0.7 and ±0.2 ppm generated by a Tb$^{3+}$ ion complex attached to the protein. Positive and negative PCSs are indicated by blue and red isosurfaces, respectively.](image)

2.2. Unique $\Delta\chi$ tensor representation

Comparison between different $\Delta\chi$ tensors requires conventions. The unique tensor representation (UTR) established by Schmitz et al. labels the $\chi$ tensor axes such that $|\chi_z| > |\chi_y| > |\chi_x|$ in analogy to alignment tensor conventions [45]. With this convention, $\Delta\chi_{ax}$ and $\Delta\chi_{rh}$ always have the same sign and $\Delta\chi_{rh}$ is at most $2/3$ of $\Delta\chi_{ax}$. The orientation of the tensor relative to the protein is usually reported in terms of Euler angles $\alpha$, $\beta$ and $\gamma$ (Fig. 5). The UTR adheres to the “ZYX” convention for the rotation axes, i.e. the first rotation is by the angle $\alpha$ about the $z$ axis of the protein frame, the second rotation is by the angle $\beta$ about the new $y'$ axis and the final rotation by the angle $\gamma$ is about the new $z''$ axis (Fig. 4). By reporting all three Euler angles in the interval $[0,\pi]$ and setting $\gamma = 0$ if $\beta = 0$, the UTR conventions
generate a single unambiguous way of reporting a $\Delta \chi$ tensor [46]. It must be kept in mind, however, that these conventions also imply that an increase of $\Delta \chi_{rh}$ beyond $2/3 \Delta \chi_{ax}$ automatically causes a change in axis definitions and a change in sign of $\Delta \chi_{ax}$ and $\Delta \chi_{rh}$. It is thus quite possible that two lanthanide ions produce PCSs of opposite sign even though their $\Delta \chi_{ax}$ values are reported to have the same sign.

With the UTR conventions, $\Delta \chi_{ax}$ is always greater than $\Delta \chi_{rh}$, so that the magnitudes of two different $\Delta \chi$ tensors can be compared by referring to the axial component $\Delta \chi_{ax}$ only.

![Fig. 5. Euler angle definitions in the ZYZ convention. Euler rotations by the angles $\alpha$, $\beta$ and $\gamma$ define the relative orientation of the $\Delta \chi$-tensor frame with respect to the protein frame.](image)

(a) A right-handed rotation by the angle $\alpha$ around the z axis is applied to the protein frame xyz to give the frame x'y'z'. (b) A second rotation by the angle $\beta$ around the new axis z' is applied to the frame x'y'z' to give the frame x''y''z''. (c) A final rotation by the angle $\gamma$ around the z'' axis maps the protein frame onto the $\Delta \chi$-tensor frame.

3. Paramagnetic properties of lanthanides

Fig. 6 provides an overview of the different paramagnetic properties of the paramagnetic lanthanide ions (excluding promethium, which is radioactive). Gadolinium produces exceptionally large PREs, but its $\chi$ tensor is isotropic and, hence, does not generate PCSs. With seven unpaired electrons in the Gd$^{3+}$ ion, each of the seven f-orbitals can be populated with one electron, explaining the symmetry of the $\chi$ tensor. All other paramagnetic lanthanide ions produce PCSs.

3.1. $\Delta \chi$ tensors associated with lanthanide ions

The largest $\Delta \chi$ tensors are found for lanthanides heavier than Gd$^{3+}$. In the case of calbindin D$_{9k}$, for which the $\Delta \chi$ tensors are reported in Fig. 6, Tb$^{3+}$ produced the largest $\Delta \chi$ tensor and Tm$^{3+}$ generated a $\Delta \chi$ tensor of intermediate magnitude. This ranking, however, depends very much on the ligand field of the lanthanide. For example, in the case of the
exonuclease domain $\varepsilon_{186}$, the $\Delta \chi$ tensor associated with Dy$^{3+}$, measured by the magnitude of the $\Delta \chi$ component, is almost 50% larger than that of Tb$^{3+}$ [47]. Conversely, in the case of the CLaNP-5 lanthanide tag, the $\Delta \chi$ tensor associated with Tm$^{3+}$ is 50% larger than that of Dy$^{3+}$ [48]. Unfortunately, it is at present not possible to predict $\Delta \chi$ tensors by quantum-theoretical calculations that take the ligand field into account.

Generally conserved features of the $\Delta \chi$ tensors include the relative signs of the largest PCSs produced. Thus, the largest PCSs produced by Tb$^{3+}$, Dy$^{3+}$ and Ho$^{3+}$ are almost always of opposite sign to those produced by Er$^{3+}$, Tm$^{3+}$ and Yb$^{3+}$. This is not always reflected in the $\Delta \chi$ tensors reported, which can have different signs for the same metal ion (see section 2.2). In the same ligand environment, the directions of the principal axes of the $\Delta \chi$ tensors tend to be similar for different lanthanides, at least for the $\chi_z$ component. This feature greatly facilitates the assignment of paramagnetic NMR spectra, by conserving the relative sign and magnitude of PCSs generated by different Ln$^{3+}$ ions. It also means that PCS measurements of multiple samples that differ only in the type of Ln$^{3+}$ ion do not deliver entirely independent structural information.

The ideal lanthanide for PCS measurements is characterised by a small isotropic $\chi$ tensor and a large $\Delta \chi$ tensor, to minimise PREs and maximise PCSs. Fig. 6 shows that the magnitudes of the $\Delta \chi$ tensors correlate significantly but not completely. For example, Dy$^{3+}$, Ho$^{3+}$ and Er$^{3+}$ tend to generate relatively large PRE effects without producing very large PCSs, making them less attractive than, for example, Tb$^{3+}$, Tm$^{3+}$ or Yb$^{3+}$. 
Fig. 6. Properties of paramagnetic lanthanide ions. Promethium was omitted from the figure because it is radioactive. The radii of the yellow spheres indicate the distance from the metal ion where PRE would broaden the $^1$H NMR signals of a protein with a rotational correlation time of 15 ns by 80 Hz on an 800 MHz NMR spectrometer. PCS isosurfaces of ±5 ppm are shown for $\Delta\chi$ tensors reported for calbindin D$_{9k}$ [49]. Electronic relaxation times expected at 18.8 T are indicated at the bottom [50]. Reproduced with permission from ref. [42]. Copyright 2007 American Chemical Society.

3.2. Paramagnetic relaxation enhancements by lanthanide ions

Using lanthanides for PRE measurements is complicated by the extremely short electron relaxation times of all Ln$^{3+}$ ions apart from Gd$^{3+}$. Fundamentally, nuclear relaxation is driven by the dipole-dipole interaction between the nuclear spins and unpaired electrons. The precise mechanism by which this dipole-dipole interaction results in nuclear relaxation depends on the electron relaxation time. For slow electron relaxation, as in the case of the Gd$^{3+}$ ion, Mn$^{2+}$ ion or a nitroxide radical, the size of the electron magnetic moment does not change as the molecule rotates. This relaxation mechanism has been described mathematically by Solomon in 1955 and in the following is referred to as Solomon relaxation [51]. A different relaxation mechanism, however, applies when the electron relaxation occurs on a time scale much shorter than the rotational correlation time of the molecule, i.e. when the electron magnetic moment continuously changes in size as the molecule rotates. In this situation, the net magnetic moment generated by the unpaired electrons is referred to as Curie spin and the corresponding relaxation mechanism as Curie relaxation [52]. Curie spin relaxation is closely related to relaxation by chemical shift anisotropy (CSA) [53-55].

Lanthanide ions with anisotropic $\chi$ tensors are invariably associated with electron relaxation times in the picosecond range and cause Curie spin relaxation. The anisotropic $\chi$ tensors lead to anisotropic PREs [56] as well as cross-correlation effects between Curie spin relaxation and a range of different relaxation mechanisms [5, 53-55, 57-61]. This makes it difficult to extract accurate distances from PRE measurements with most Ln$^{3+}$ ions other than Gd$^{3+}$. Most notably, cross-correlation between CSA and Curie spin relaxation can potentially produce a narrower NMR signal in the presence of a paramagnetic ion than in its absence [53, 62].

4. Determining $\Delta\chi$ tensors
4.1. Principles

Δχ tensors depend on the ligand field of the metal complex and must be determined experimentally for each new metal complex. There are eight parameters to be determined, comprising the Δχax and Δχth values that define the χ tensor anisotropy, the x, y, z coordinates of the paramagnetic centre, and three rotation angles (e.g. Euler angles) to define the orientation of the Δχ tensor relative to the ligand coordinates. In principle, therefore, measurement of eight pseudocontact shifts of nuclear spins in the complex would be sufficient to determine the Δχ-tensor parameters, provided that the three-dimensional (3D) structure of the complex is known. In practice, the NMR resonances of nuclear spins in close proximity to a paramagnetic centre tend to be broadened beyond detection, due to PREs. Moreover, nuclear spins located within a few chemical bonds of the metal ion are subject to Fermi contact shifts, which arise from through-bond interactions with the unpaired electrons, analogous to scalar couplings between nuclear spins [4, 16]. Disentangling PCSs from contact shifts is difficult [63-65]. The problem is particularly stark for lanthanide ions because density functional theory (DFT) calculations, which have been remarkably successful at predicting contact shifts for transition metal ions [1], fail for lanthanide ions due to their large number of electrons. Therefore, determining the Δχ tensors associated with lanthanide ions is most readily achieved by measuring PCSs for a large set of nuclear spins that are located at a sufficiently long distance from the metal ion to avoid contact shifts and PREs, followed by a best fit to available 3D structure coordinates of the protein [49].

4.2. Quality factors

Fitting routines for Δχ tensors commonly minimize the sum of the squared deviations between experimental PCSs, PCSexp, and back-calculated PCSs, PCScalc [46]. As a measure of the quality of the fit, it is customary to report the quality factor

\[ Q = \text{Sqrt}[\Sigma (\text{PCS}_{\text{exp}} - \text{PCS}_{\text{calc}})^2/\Sigma (\text{PCS}_{\text{exp}})^2] \]  

(3)

where a smaller number corresponds to a better fit. An alternative definition of the quality factor is also in use [66, 67]

\[ Q = \text{Sqrt}[\Sigma (\text{PCS}_{\text{exp}} - \text{PCS}_{\text{calc}})^2/\Sigma (|\text{PCS}_{\text{exp}}| + |\text{PCS}_{\text{calc}}|)^2] \]  

(4)

that avoids large contributions from small PCScalc values. The definition of Eq. 4 results in smaller Q factors.

4.3. Effective Δχ tensors arising from flexible metal tags
When metal tags are used to endow proteins with a paramagnetic centre, almost all tags currently available are attached via somewhat flexible tethers. As a result, the $\Delta \chi$ tensor derived from PCSs measured for the protein represents an ‘effective’ $\Delta \chi$ tensor that fits the data but is affected by averaging over the different tag orientations and metal positions that arise from the flexibility of the tether. In this situation, the true $\Delta \chi$ tensor of the tag itself remains unknown. For practical applications, the true tensor may actually be of limited interest, as the metal tag is usually deployed to obtain structural restraints in the protein rather than the tag. If a metal complex undergoes rotational motion with respect to the protein without changing the location of the metal ion, the average $\Delta \chi$ tensor is perfectly described by an effective $\Delta \chi$ tensor, which obeys Eq. 1 and can be used to predict the PCSs of all other nuclei in the structure.

As the PCSs depend on the distances of the nuclear spins from the metal ion, a fundamental problem arises when flexibility of the tag allows the metal ion to change its position relative to the protein. In principle, this situation could be simulated by fitting the observed PCSs with multiple $\Delta \chi$ tensors, but fitting so many parameters would require PCSs for a large number of nuclei and still leave doubts about the accuracy of PCS predictions for any other sites in the protein. In practice, it is common to fit the data with a single effective $\Delta \chi$ tensor regardless of the motions of the metal ion. The error associated with this approach has been assessed in a comprehensive theoretical analysis, which determined the accuracy of PCS predictions in regions of the protein that had not been used to fit the effective $\Delta \chi$ tensor [68]. The analysis showed that a surprisingly large amplitude of translational metal ion movement can be accommodated by the effective $\Delta \chi$-tensor approach, in particular, if nuclear spins closer than 10 Å to the metal ion and PCSs greater than ±3 ppm are excluded from the $\Delta \chi$-tensor fit. Obviously, the accuracy with which the PCSs of a group of nuclear spins can be predicted by an effective $\Delta \chi$ tensor deteriorates with their distance from the set of nuclear spins used to fit the $\Delta \chi$ tensor [69]. The predictive value of an effective $\Delta \chi$ tensor can be enhanced by determining the tensor through fitting to a subset of nuclear spins only, which are selected by their proximity to the region of interest [68, 69].

4.4. PCS measurements and assignment of paramagnetic NMR spectra

In the case of paramagnetic centres with an isotropic $\chi$ tensor (Gd$^{3+}$, Mn$^{2+}$, nitroxides), the chemical shifts are unaffected by the paramagnetism. In contrast, the chemical shift changes associated with PCSs require new assignments of the NMR signals in the
paramagnetic state. While the assignment strategies available for diamagnetic proteins can also be used for the resonance assignments of paramagnetic proteins, PREs present obstacles by broadening many resonances beyond detection. To circumvent these complications, approaches have been developed to transfer resonance assignments from the diamagnetic to the paramagnetic spectra.

4.4.1. Resonance assignment using $\Delta\chi$-tensor fits

Transfer of resonance assignments from diamagnetic to paramagnetic spectra is most easily achieved by HSQC spectra, as the $^1$H spin and the directly bonded heteronucleus experience very similar PCSs owing to their close proximity compared with the distance from the paramagnetic centre. Consequently, the HSQC cross-peaks of paramagnetic and diamagnetic samples are displaced along almost parallel lines with a slope close to one. In the example of amide cross-peaks in a $[^{15}\text{N},^1\text{H}]$-HSQC spectrum, the assignment is facilitated by recording three spectra, two of paramagnetic samples with different lanthanide ions and one of a diamagnetic reference. Superimposition of the three spectra shows three cross-peaks for each amide, which lie on the same line [32]. Using Tb$^{3+}$ and Tm$^{3+}$ as the paramagnetic lanthanides, the PCSs tend to be of opposite sign and their magnitude larger for Tb$^{3+}$ than Tm$^{3+}$. The resulting peak pattern greatly helps assignment of the paramagnetic cross-peaks. Nonetheless, spectral overlap always leads to ambiguities. To resolve these, an initial $\Delta\chi$ tensor can be fitted using the unambiguous PCSs measured from resolved cross-peaks, which allows prediction of unassigned PCSs and thus the assignment of further paramagnetic peaks. Rounds of $\Delta\chi$-tensor refinements and PCS prediction have been automated, e.g., in the program Echidna [47].

4.4.2. Resonance assignment by chemical exchange of metal ions

An alternative assignment strategy is available, if the metal ion exchanges in and out of its binding site. In the fast exchange limit, cross-peaks shift continuously, from the diamagnetic peak position towards the paramagnetic peak position, with increasing concentration of paramagnetic metal ion. If the exchange is slow on the chemical shift time scale but still within the time scale of $T_1$ relaxation, a sample prepared with a mixture of paramagnetic and diamagnetic metal ions can generate exchange cross-peaks that link the paramagnetic and diamagnetic auto-peaks. Exchange lifetimes on a suitable time scale have been observed for a protein containing a natural metal binding site [32, 70-72] and for
ubiquitin tagged with an iminodiacetic acid (IDA) tag to form a lanthanide coordination site together with a carboxyl side chain of the protein [73]. In a different protein, however, the strategy of combining the IDA tag with a protein carboxyl group failed to produce metal exchange rates that were sufficiently fast to generate sizeable exchange cross-peaks [74]. In view of the difficulty of designing metal binding sites with suitable metal exchange rates, other design criteria are usually considered more important, such as location and magnitude of the $\Delta\chi$ tensor as well as thermodynamic stability of the metal complex.

4.4.3. Using PCSs to assign diamagnetic NMR spectra

Selective isotope labelling of the target protein presents a straightforward way of spectral simplification that facilitates the assignment of paramagnetic peaks by reducing spectral overlap. With well-resolved cross-peaks in the paramagnetic and diamagnetic HSQC spectra, it becomes possible to measure complete sets of PCSs without having to rely on $\Delta\chi$-tensor fits and PCS predictions. Combined with the 3D structure of the protein and knowledge of the metal position, the PCSs can then be used to assign not only the paramagnetic but also the diamagnetic cross-peaks, especially if additional paramagnetic information is included, such as PREs, paramagnetically induced RDCs and cross-correlated relaxation effects [75]. In a related approach, it has been shown that, using the $\Delta\chi$ tensor determined from a well-resolved $^{15}$N-HSQC spectrum to predict PCSs, most side-chain methyl groups of a 21 kDa protein in a 30 kDa complex could be assigned both in the diamagnetic and paramagnetic state by comparison with experimentally measured PCSs [72].

The next step would be to try to assign side-chain methyl resonances without prior knowledge of the $\Delta\chi$ tensor, which would be attractive for high-molecular weight systems where side-chain methyl resonances are much easier to detect than backbone amides. A potential problem associated with this strategy is presented by intrinsic side-chain mobility, which would compromise the quality of the $\Delta\chi$ tensors that can be obtained. The problem associated with side-chain mobility has been highlighted by the difficulty of fitting accurate $\Delta\chi$ tensors to side-chain amides of the 19 kDa protein PpiB using PCSs generated with Tb$^{3+}$, Tm$^{3+}$ and Yb$^{3+}$ [76].

4.4.4. Additional aids for the assignment of paramagnetic NMR spectra

Owing to their smaller gyromagnetic ratio, the NMR resonances of heteronuclear spins are less affected by PREs than $^1$H NMR signals. Many protonless experiments have
been designed to observe nuclear spins located close to the paramagnetic centre [77]. These experiments are most valuable for probing the electronic properties of the paramagnetic centre and they generate a more complete set of PCSs. Notably, however, resonances with very large PCSs are more difficult to assign and, as \( \Delta \chi \)-tensor fits minimize the mean square deviation between observed and back-calculated PCSs, very large PCSs have a disproportionate weight in the fit, which tends to degrade the quality of back-calculated PCSs at greater distances from the metal ion. Moreover, close to the paramagnetic centre, the point-dipole approximation underlying Eq. 1 loses its validity even for lanthanide ions [2].

The Curie law implies that magnetic susceptibility increases with the inverse temperature \( T^{-1} \), leading to larger PCSs at lower temperature. Plots of chemical shifts versus \( T^{-1} \) can thus be used to determine the sign of a PCS and to discriminate between large and small PCSs, but it must be taken into account that the chemical shifts of the diamagnetic reference are also sensitive to temperature [12, 63, 78].

At very high magnetic fields, the PCSs decrease because of saturation of magnetic moments. The effect is proportional to the square of the magnetic field \( B_0 \) but still very small (of the order of 1%) at currently available NMR field strengths [79]. It is easily obscured by preferential molecular orientation in the magnetic field, which equally depends on \( B_0^2 \) [80] and, for nuclear spins displaying chemical shift anisotropies, generates residual anisotropic chemical shifts (RACS). RACS effects are distance-independent and in paramagnetic molecules can be greater than 0.1 ppm on a 800 MHz NMR spectrometer [81]. As the molecular alignment with the magnetic field originates from the anisotropy of the magnetic susceptibility of the metal complex, a flexibly attached metal tag confers less alignment on the protein it is attached to, downscaling the RACS effects and any other effects resulting from molecular alignment.

**4.5. Paramagnetically induced residual dipolar couplings**

Metal ions with non-vanishing \( \Delta \chi \) tensors confer a weak molecular alignment on the molecules they are bound to. The alignment is with respect to the external magnetic field \( B_0 \) and is manifested in the NMR spectra by residual dipolar couplings (RDCs) (in addition to the RACS effects mentioned in Section 4.4.4). The principal axes of the alignment tensor governing the paramagnetically-induced RDCs coincide with the principal axes of the \( \Delta \chi \) tensor governing the PCSs. RDCs contain distance-independent information about the orientation of spin pairs with respect to the molecular alignment tensor. For a rigid molecule
containing a paramagnetic centre with non-vanishing $\Delta \chi$ tensor, the RDC $D_{AK}$ (in Hz) between the spins A and K is given by [15]

$$D_{AK} = -(hB_0^2\gamma_A\gamma_K)/(240r_{AK}^3k_BT^3)[\Delta \chi_{ax}(3\cos^2\Theta - 1) + 1.5 \Delta \chi_{rh} \sin^2\Theta \cos 2\Phi],$$

(4)

where $\gamma_A$ and $\gamma_K$ denote the magnetogyric ratios of the nuclear spins A and K, respectively, $r_{AK}$ is the internuclear distance, $h$ is Planck’s constant, $k_B$ the Boltzmann constant, $T$ the temperature, and the angles $\Theta$ and $\Phi$ define the orientation of the vector that connects the coupled nuclei A and K with respect to the molecular alignment tensor (Fig. 7).

Fig. 7. Geometric parameters defining the RDC between the nuclear spins A and K, which arises from molecular alignment in the magnetic field owing to an anisotropic $\chi$ tensor with the principal axes $\chi_x$, $\chi_y$ and $\chi_z$.

4.6. Using RDCs to assess tag mobility

For a rigid molecule with a rigidly bound metal tag, the $\Delta \chi$ tensor can be derived from the alignment tensor determined from RDCs using

$$\Delta \chi_{ax,th} = (15\mu_0kT/B_0^2) A_{ax,th}$$

(5)

where $A_{ax}$ and $A_{th}$ are the axial and rhombic components of the alignment tensor, $B_0$ is the magnetic field strength, $\mu_0$ the magnetic permeability of vacuum, $k$ the Boltzmann constant, and $T$ the temperature [15]. In contrast to a $\Delta \chi$-tensor fit, which is affected by any tag motions that relocate the metal ion relative to the protein, the quality of an alignment tensor fit using RDCs is not compromised by tag mobility, as RDCs do not depend on the distance of the nuclear spins from the paramagnetic centre (eq. 3). Therefore, discrepancies between $\Delta \chi$ tensors derived from PCSs and RDCs can indicate tag mobility. Model calculations indicate that RDCs decrease with increasing amplitude of tag motions, while the effective $\Delta \chi$ tensor
determined from PCSs tends to increase. The magnitude of both effects, however, is sensitive to the orientation of the original $\Delta \chi$ tensor with respect to the protein, and $\Delta \chi_{\text{ax}}$ values determined from PCSs and RDCs can be the same within 20% even for tag motions in a cone with an opening angle of $120^\circ$ [68]. Therefore, the discrepancy between the tensors derived from RDCs and PCSs is not a good measure of the amplitude of tag motions.

4.7. Software using PCSs

4.7.1. Programs for $\Delta \chi$-tensor determination

Experimental determination of $\Delta \chi$ tensors from PCSs requires the coordinates of the atoms for which the PCSs have been measured. The required fitting routine has been implemented in many different software packages, such as the recent implementation in the MSpin software by MestreLab Research [82]. Only some of the more frequently used programs are explicitly described here. Fantasian [83, 84] comprises early standalone software for fitting $\Delta \chi$ tensors to proteins, which was designed to fit $\Delta \chi$ tensors for several different metals, provided their coordinates relative to the protein are known. The program Numbat [46] was written later to provide a convenient graphical user interface. It can simultaneously fit $\Delta \chi$ tensors from up to 4 different metal ions and determine the metal position, and includes a routine to take RACS corrections into account. pyParaTools [85] is a set of Python routines to fit $\Delta \chi$ tensors. The program can create libraries of tag conformations and identify the conformation that best fits the experimental PCS data. A very recent implementation is offered by the program FANTEN [86], which fits $\Delta \chi$ tensors and alignment tensors from PCSs and RDCs, using multiple metal ions. The program has a graphical interface, can perform a joint analysis of PCSs and RDCs, and allows rigid body docking of two molecules using $\Delta \chi$ and alignment tensors.

4.7.2. Programs using PCSs for NMR resonance assignments of proteins

$\Delta \chi$-tensor fits to protein structures often yield excellent correlations between back-calculated and experimental PCSs. This invites the use of PCSs for NMR resonance assignment of proteins of known 3D structure. As the same PCS value may be observed for different nuclei, PCSs alone are not sufficient to obtain specific resonance assignments. These ambiguities can be resolved in combination with additional paramagnetically generated restraints such as RDCs, PREs and cross-correlation effects between Curie-spin and dipole-dipole relaxation. This approach is particularly suitable for the assignment of the $^{15}$N-HSQC
cross-peaks of a selectively $^{15}$N-labelled protein, as demonstrated for the 30 kDa complex between the N-terminal domain of the ε subunit, ε186, labelled with $^{15}$N-leucine, phenylalanine or valine, and the θ subunit of *Escherichia coli* DNA polymerase III [75]. Among the paramagnetic restraints, PCSs and RDCs proved to be particularly valuable for resonance assignment. The algorithm, named PLATYPUS, was programmed in Mathematica (Wolfram Research). It assigns the resonances in both the diamagnetic and paramagnetic states, but needs the metal coordinates as input from the beginning. It is attractive that resonance assignments of the well-resolved $^{15}$N-HSQC spectrum can be obtained in this manner without the need for expensive $^{15}$N/$^{13}$C-labelled samples or 3D NMR spectra.

In many cases, the 3D structure and resonance assignments of the diamagnetic protein are known, but the resonance assignments in the paramagnetic state are unknown. To assist with resonance assignments in the paramagnetic state of uniformly $^{15}$N or $^{15}$N/$^{13}$C-labelled proteins, the program Echidna was devised, which uses the 3D structure of the protein together with peak lists of the $^{15}$N-HSQC or 3D HNCO spectra in the paramagnetic and diamagnetic state to determine the PCSs and Δχ tensors at the same time. Using spectra of the ε186/θ complex, the program was shown to deliver robust Δχ-tensor determinations, including refined metal coordinates [47].

Given the 3D structure of a protein and Δχ tensors determined from PCSs of backbone atoms, PCSs of methyl resonances measured in $^{13}$C-HSQC spectra can be used to obtain sequence-specific resonance assignments in the diamagnetic and paramagnetic states, including stereospecific resonance assignments of the methyl groups of valine and leucine residues. The approach was automated in the program Possum [72] and demonstrated with the $^{15}$N/$^{13}$C-labelled ε186/θ complex. The input to the program requires experimental PCSs and it helps to add information about which methyl groups belong to the same amino acid residue, as evidenced by HCCH-TOCSY cross-peaks.

More recently, the program PARAssign [87, 88] was developed to assign backbone amide and side-chain methyl resonances in proteins, both in the diamagnetic and paramagnetic state, using only PCSs measured in 2D NMR spectra. In contrast to previously published software, the program relies on PCSs measured for multiple samples, each with a paramagnetic metal ion attached at a different site, and on approximate estimates of Δχ-tensor magnitude, orientation and position, to obtain initial assignments and Δχ-tensor fits. It has been shown earlier that good initial estimates can be obtained with double-arm lanthanide tags such as CLaNP-5 [48].
All programs for resonance assignment follow an iterative approach, in which the $\Delta \chi$-tensor parameters are refined as more and more resonance assignments are being made.

4.7.3. Programs using PCSs for protein structure computation

Early on, refinement of protein structures by PCSs was achieved by treating PCSs like other structural restraints, e.g. by including an energy term for PCSs in the program XPLOR [89] or by including PCSs in the target function of DIANA [83] or in programs for energy minimization and molecular dynamics [90, 91]. In this way, PCSs have been incorporated as structural restraints also in the programs CYANA [92] and Xplor-NIH [93, 94], which currently are the most frequently used programs for 3D structure determinations of proteins from NMR data. A recent implementation of PCSs and self-orientation RDCs in the crystallography package REFMAC5 [95] demonstrated that protein crystal structures can also be refined using these long-range paramagnetic restraints without compromising the quality of the crystal structure, highlighting the similarity of protein structures in solution and single crystals [96].

The attempt to use PCSs for protein structure determination rather than refinement faces the intrinsic problem that 3D coordinates of at least a subset of atoms in the protein must be available prior to fitting $\Delta \chi$ tensors. The program PCS-Rosetta achieves this by starting from preliminary structural models (decoys) predicted from the amino acid sequence. To assist the structure predictions, it is helpful to begin with a fragment library that is in agreement with the backbone chemical shifts of the protein, as implemented in the CS-Rosetta [97] structure prediction algorithm. Already at the fragment assembly step, PCS-Rosetta fits $\Delta \chi$-tensors to every decoy structure and the quality of the fit is used to select the best models before further structure refinement [98]. This approach was extended in the program GPS-Rosetta, which uses PCSs from different protein samples prepared with paramagnetic metal ions at different sites. The program was shown to deliver the accurate 3D fold of the C-terminal domain of ERp29, using incomplete sets of PCSs of backbone amide protons measured in straightforward $^{15}$N-HSQC spectra of samples with lanthanide tags at four different sites [99]. In combination with an additional iterative resampling algorithm, the program produces accurate 3D structures even for proteins with over 200 residues, which is difficult to achieve with the original Rosetta algorithm [100]. While the algorithm is generally applicable, it hinges on the availability of suitable metal-ion tagged protein samples.

5. Lanthanide tags for the generation of pseudocontact shifts
This section discusses tags that can coordinate lanthanide ions, with a particular emphasis on tags that have been found to generate non-vanishing $\Delta \chi$ tensors in target proteins. Lanthanide tags designed to generate PCSs can also be used to generate PREs, which may sometimes present more informative structural restraints than the PCSs. All lanthanide tags can be used with Gd$^{3+}$ to generate PREs.

5.1. Lanthanide binding proteins

Lanthanides play no obvious role in biology and no lanthanide-specific structural motifs are known in proteins. In vitro, however, Ln$^{3+}$ ions can sometimes replace naturally occurring metal ions such as Ca$^{2+}$, Mg$^{2+}$ or Mn$^{2+}$. In this way, a natural metal binding site can be used to label the protein with a paramagnetic Ln$^{3+}$ ion. Substitutions for a lanthanide have been particularly successful in the case of Ca$^{2+}$-binding metalloproteins containing an EF-hand motif as, among all the biological metal ions, Ca$^{2+}$ is most similar to Ln$^{3+}$ ions in its ionic radius and complexation chemistry [101, 102]. Natural EF-hand motifs are usually paired to comprise two calcium binding sites, but the greater charge of Ln$^{3+}$ versus Ca$^{2+}$ ions hinders the simultaneous incorporation of two Ln$^{3+}$ ions.

Early studies reported paramagnetic shifts and $\Delta \chi$ tensors for Yb$^{3+}$ bound to parvalbumin, which naturally binds two Ca$^{2+}$ ions [103, 104]. The selectivity of the four Ca$^{2+}$-binding sites of calmodulin for Ln$^{3+}$ ions has been studied extensively, showing that lanthanides preferentially bind to the N-terminal domain while a single mutation, N60D, generates a binding site that is selective for lanthanides even in the presence of excess calcium ions [105-107]. Calbindin D$_{9k}$ is another protein that binds two Ca$^{2+}$ ions in two EF-hands, one of which can selectively be replaced by a single lanthanide ion. Calbindin D$_{9k}$ containing one Ca$^{2+}$ and one Ln$^{3+}$ ion has been used extensively by Bertini and co-workers to determine the $\Delta \chi$ tensors of paramagnetic lanthanides [49, 60, 108].

Similar strategies have been successfully applied to metalloproteins with different metal cofactors. For example, the activity of the exonuclease domain $\varepsilon$ of E. coli DNA polymerase III (PolIII) depends on two solvent-exposed Mg$^{2+}$ or Mn$^{2+}$ ions in the active site, which can be replaced by a single Ln$^{3+}$ ion. PCSs measured with a truncated 21 kDa form of $\varepsilon$, $\varepsilon_{186}$, have been used to determine the structure of its 30 kDa complex with another PolIII subdomain, $\theta$ [75, 109]. Similarly, the two Mg$^{2+}$ ions in the structurally related E. coli DNA polymerase I and bacteriophage T4 DNA polymerase can be replaced by a single Eu$^{3+}$ ion [110, 111] but, at least in the latter case, the Mg$^{2+}$-Ln$^{3+}$ substitution compromises the
enzymatic activity [111]. Substitutions of natural metal ions by lanthanides are therefore limited to special cases and may affect the biological activity and structure of the host protein.

5.2. Lanthanide binding peptides

Based on the capacity of EF-hands to bind Ln\(^{3+}\) ions, lanthanide-binding peptides (LBP) have been developed for tagging target proteins. In the first application of this approach, N-terminal fusion to a membrane-bound peptide was shown to generate paramagnetically induced RDCs with Yb\(^{3+}\) and Dy\(^{3+}\) [112]. Subsequently, an extensive peptide screen yielded 17-residue LBPs with greatly improved Ln\(^{3+}\) binding affinity [113, 114], which maintained the EF-hand fold [115]. N-terminal fusion to ubiquitin generated significant paramagnetically induced RDCs with different Ln\(^{3+}\) ions [116]. Concatenation of two LBPs into a 32-residue double-lanthanide-binding tag and N-terminal fusion to ubiquitin produced even larger RDCs and PREs [117], but fitting the PCSs with a \(\Delta\chi\) tensor for each metal would be impractical.

If the 3D structure of the target protein is known, a LBP can also be engineered into a loop of the protein structure [118-121]. This approach achieves a well-defined positioning of the lanthanide with respect to the protein but is limited to loop structures of suitable geometry. An LBP was successfully inserted into three different loops of interleukin-1\(\beta\) (IL1\(\beta\)) [121] and into a loop of a small immunoglobulin G binding protein [118, 119]. Nanomolar lanthanide binding affinities were achieved. Using IL1\(\beta\), it was also shown that LBPs can be engineered into two loops simultaneously, allowing Gd\(^{3+}\)-Gd\(^{3+}\) distance measurement by pulse electron paramagnetic resonance (EPR) spectroscopy but making it harder to fit \(\Delta\chi\) tensors [120].

In contrast to tags attached by chemical reactions, peptide fusions always deliver complete ligation yields, but they do have the intrinsic drawback that fusions limit the tagging sites to the N- or C-terminus or to specific loop regions of the target protein. In addition, isotope labelling labels the LBP together with the target protein, leading to increased complexity of the protein NMR spectrum, at least in the diamagnetic reference state.

To gain more freedom in positioning the LBP on the protein, LBPs have also been linked to a single cysteine residue via a disulfide bond [122, 123]. Preparation of both protein and LBP with a cysteine residue poses the challenge of selectively forming specific disulfide bonds between protein and LBP rather than between two protein or LBP molecules. The practical solution to this problem, which is applicable to any tag with a free thiol group, is to
activate the cysteine residue of the protein first with DTNB to form an activated disulfide bond. The activation reaction can be monitored by the release of yellow thionitrobenzoate and excess DTNB can readily be separated from the activated protein by centrifugal ultrafiltration. Addition of tag once again releases yellow thionitrobenzoate [122]. Notably, a large excess of LBP can lead to disulfide exchange reactions and decreased yields by favouring disulfide bonds between LBPs. As LBPs are strongly acidic, however, the protein-LBP ligation product can readily be isolated by ion exchange chromatography [36].

LBPs can be furnished with a single cysteine residue at different sites, so that the orientation of the $\Delta \chi$ tensor relative to the protein is easily altered by the choice of LBP. To improve the solubility of the LBP, a tryptophan residue present in the original design [113, 114] can be substituted by alanine [122]. 16-residue LBPs were found to be sufficient to produce significant PCSs in the N-terminal DNA-binding domain of the E. coli arginine repressor (ArgN) after attachment to the single cysteine residue present in ArgN [122, 123]. This approach offers the general advantage of chemically ligated tags, in that isotope-labelled proteins display the same number of NMR signals with and without tag, at the expense of possibly incomplete ligation yields.

In a hybrid approach, an LBP can also be fused to the N-terminus of a protein and a second linkage established via a disulfide bond. The two-point anchoring of the LBP decreases the tag mobility, thereby reducing the averaging of anisotropic paramagnetic effects and leading to larger PCSs in the protein [124]. The approach was demonstrated with a cysteine mutant of the B1 immunoglobulin-binding domain of protein G (GB1), where the cysteine residue was positioned at a site suitable for formation of a disulfide bond with an N-terminal cysteine residue in the LBP. Formation of the disulfide bond was achieved with DTNB. A drawback of the approach is that the structure of the protein must be known in advance and that the length of the peptide segment connecting the LBP to the protein must be optimized to avoid conformational exchange phenomena and distortion of the protein structure [124-126].

The difficulty of finding the optimal linkage to the target protein is a general challenge associated with LBPs, irrespective of whether they are attached by N- or C-terminal fusion or by disulfide bonds. Attachment to a highly solvent-exposed cysteine residue can easily lead to a tag that is too mobile to observe useful PCSs, whereas a linkage that is too short can prevent the LBP from folding [36]. To address this challenge, much effort has been devoted over the past decade to developing non-peptidic tags with broader applicability.
5.3. Synthetic tags

Some biological molecules can be made by total chemical synthesis, in which case a metal-binding chelating group can be part of the synthetic design from the beginning. In the special case of carbohydrates, relatively harsh reaction conditions can be used to achieve chemical modification with a metal-binding chelate. For example, the reducing end of an oligosaccharide can be selectively aminated and reacted in an organic solvent with a carboxyl-group containing tag with formation of an amide bond, and protection groups on the tag can be removed with strong acid afterwards [26]. Similarly, DNA molecules can be synthesized to contain reactive groups, such as thiol or amino groups, or the tag can already be part of the protected nucleotide used in the DNA synthesis. Various approaches have been reviewed previously [26, 36].

Attaching synthetic tags to proteins is much more challenging, as proteins contain a more diverse range of functional groups and they are prone to irreversible denaturation or degradation in organic solvents, at non-neutral pH or at elevated temperature. In native proteins, thiol groups stand out for their nucleophilicity and sensitivity towards oxidation reactions, allowing selective alkylation as well as tag ligation via disulfide bonds. More recently, methods for genetic encoding of unnatural amino acids have opened the door to new bioorthogonal chemistries for site-specific reactions with proteins under mild conditions. In some cases, tags can also be directed to specific sites by non-covalent bonding. Challenges beyond selectivity include broad applicability, stability, rigidity and stereochemical purity.

5.3.1. Chemical synthesis of ligands with metal tags

Low-molecular weight disaccharides, such as chitobiose or lactose, have been studied with PCSs generated by synthetically attached lanthanide tags that included a mono- or biphenylic linker between the carbohydrate and an EDTA-based lanthanide-binding moiety [26, 127-129]. More recently, a lanthanide-binding chelating group has been linked to a branched nonasaccharide to assess its conformation and flexibility by PCSs [130]. Based on these results, compound 1 (Fig. 8) was synthesized, which combines a disaccharide (lactose) with a lanthanide-binding moiety and can be used as a sensor to detect carbohydrate-protein interactions [82]. Large PCSs were observed with Dy\(^{3+}\) for most carbohydrate protons, indicating a well-balanced linker length that prevented overly strong PREs without compromising PCSs. Following binding to the lactose-binding protein galectin-3, PCSs were observed in the protein as far as 42 Å from the lanthanide ion but the Q-factors were fairly large, suggesting movements of the metal relative to the protein. Similarly, the fucose analog
2 was synthesized via click chemistry and used to probe interactions with a coat protein of human norovirus [131]. Finally, the low molecular weight anaesthetic sevoflurane was chemically modified with a lanthanide-binding DOTA moiety to yield 3 to probe binding to two separately expressed domains of calmodulin [132]. Due to weak binding (millimolar), only small PCSs were observed in the protein, limiting the accuracy with which the binding sites could be pinpointed on the protein surface.

These examples illustrate the intrinsic difficulty associated with metal tags attached to ligands, as the tag must not interfere with the protein-ligand interaction, yet needs to be sufficiently immobilised to generate PCSs in the protein that can be interpreted with a single $\Delta\chi$ tensor.

![Fig. 8. Ligand molecules fused with lanthanide-binding moieties. The parts comprising the original ligand molecules are highlighted in bold.](image)

**5.3.2. Covalent protein tags**

Various chemical strategies have been reported to achieve selective covalent bond formation between proteins and paramagnetic tags. All examples reported to date either attach the tags to cysteine residues via disulfide or thioether formation, or 4-azidophenylalanine residues are targeted in a “click chemistry” approach (Fig. 9).
Fig. 9. General reaction schemes for covalently attached tags discussed in this review. The tag and its reactive moiety are shown in red. The targeted amino acid residue is shown in blue. The metal chelating part of the tags is not further specified and is referred to as R. Note that the exact chemical nature of the complete tag (not just its reactive moiety) contributes to the reactivity of a tag. For example, electron-withdrawing groups are often required. The figure does not specify any necessary catalysts or reaction conditions (e.g. pH). Particular care has to be taken with the iodoacetamide group, which can also react with the amino group at the N-terminus of a protein and with histidine or lysine side-chains [133].

5.3.2.1. EDTA tags and peak doubling due to chiral metal complexation

Most reported tags are attached to cysteine via a disulfide bond. The first non-peptidic NMR probes for tagging proteins with metal ions were based on EDTA. This universally used hexadentate chelating agent coordinates metal ions, with high stability constants. Modification with a thiol-reactive group, such as in the tags S-(2-pyridylthio)cysteaminyl-EDTA (4) and S-methanesulfonylcysteaminyl-EDTA (5), produces EDTA tags that spontaneously form a disulfide bond with a solvent-exposed cysteine residue. While EDTA itself is achiral, EDTA-metal complexes form two enantiomeric forms (Fig. 10). As proteins are always chiral, ligation with a racemic EDTA-metal complex leads to diastereomers and,
consequently, peak doubling in the NMR spectrum, which becomes particularly apparent with PCSs, as the different isomers are associated with different $\Delta\chi$-tensor orientations relative to the protein [134, 135]. This makes it difficult to derive $\Delta\chi$ and alignment tensors from PCS and RDC measurements.

![Diagram](image.png)

**Fig. 10.** EDTA forms two enantiomers in complex with a metal ion. Circles symbolise the carboxyl groups of EDTA, curved lines represent the ethylene groups and M denotes the metal ion.

Tag 4 was used to tag the N-terminal domain of signal transducer and activator of transcription 4 (STAT4NT), where peak doubling observed with Co$^{2+}$ was interpreted in terms of breaking the symmetry of the homodimer [136]. The tag allowed useful PRE measurements with metal ions with isotropic (Mn$^{2+}$) or nearly isotropic (Cu$^{2+}$) magnetic susceptibility [135-137]. Tag 4 was also linked to a membrane protein for RDC measurements with Tb$^{3+}$, Tm$^{3+}$ and Yb$^{3+}$, and peak doubling was observed but not commented on [138].

In principle, chiral metal complexation does not cause problems, if the metal complex interconverts sufficiently rapidly between the two chiralities. Notably, however, if fast interconversion between different chiralities is associated with release of the metal ion from the chelating agent, the metal ion can potentially bind also to other sites in the protein. In addition, fast metal dynamics can lead to smaller PCSs by averaging of different $\chi$-tensor anisotropies. In principle, population of a single tag enantiomer may be favoured by interactions with the protein, but this is difficult to engineer.

Fortunately, a single chiral centre in the tag can bias the geometry of the metal chelate to populate almost exclusively a single chiral form. For example, due to rapid inversion of tertiary amino groups, compounds containing a pseudoasymmetric nitrogen, as in the EDTA derivatives 4 and 5, cannot be isolated in enantiopure form. With a chiral centre elsewhere in the chelating molecule, however, the final metal complex assumes a single preferred chirality. This strategy has been successfully applied to a range of acyclic synthetic tags.
In the case of EDTA tags, a stereocentre at the attachment point of the linker moiety connecting the metal chelate with the protein (tags 6a/b of Fig. 11) proved to produce a single set of RDCs and significant PCSs with Dy$^{3+}$, following attachment of the tag to a cysteine mutant of trigger factor (TF). Very different Δχ-tensor orientations were obtained for epimers TF-6a and TF-6b [134]. 6a and 6b were also successfully used with a cysteine mutant of ubiquitin [139] and the closely related tags 7a and 7b were shown to produce RDCs and PCSs, albeit of modest magnitude, for TF and a cysteine mutant of apo-calmodulin [140]. Importantly, however, the Tb$^{3+}$ binding affinity of the tag was found to be nine orders of magnitude greater than that of apo-calmodulin, ensuring that the lanthanide bound selectively to the tag and not the protein. Therefore, these tags are suitable for studying metalloproteins.

**Fig. 11.** Thiol-reactive acyclic probes. The reactive parts for covalent cysteine tagging are highlighted (bold). Tags 4, 5, 6a/b, and 7a/b are EDTA-based (hexadentate), and probes 8 and 9 are derived from DTPA (octadentate) and TAHA (nonadentate), respectively. Asterisks identify pseudoasymmetric nitrogen atoms.

### 5.3.2.2. DTPA tag

DTPA is an octadentate chelating agent with an even higher binding affinity for Ln$^{3+}$ ions than EDTA, but the complex between DTPA and a lanthanide produces four pairs of enantiomers as the central symmetric nitrogen also becomes chiral in the complex [44]. Consequently, up to eight different diastereomeric species can be generated by linkage to a protein. Tag 8, referred to as caged lanthanide NMR probe (CLaNP), was designed to address this challenge by tying the tag to two solvent-exposed cysteine residues positioned with about 8-10 Å separation. The two-arm attachment rigidifies the tag and raises the possibility that the tag preferentially populates a single stereoisomer by interaction with the protein surface. A crystal structure of this tag tied to pseudoazurine showed that the tag did not affect the protein
structure [141]. Even with Yb$^{3+}$, PCSs could be observed at distances up to 40 Å from the metal centre, attesting to the rigidity of the tag. As there were no close contacts between the Ln$^{3+}$-chelating moiety and the protein, however, up to five different sets of paramagnetic peaks were observed, critically compromising the utility of this tag. Nonetheless, $\Delta\chi$ tensors could be determined from the three most intense sets of PCSs. While for small proteins it may be possible to unravel the NMR effects of three different $\Delta\chi$ tensors, the data analysis becomes prohibitively difficult for larger proteins. In general it is preferable to obtain multiple tensors from different samples, where each paramagnetic or diamagnetic sample produces a single set of NMR peaks.

5.3.2.3. **TAHA tag**

Following attachment of the nonadentate TAHA-based tag 9 to two different cysteine mutants of ubiquitin with Tm$^{3+}$ and Tb$^{3+}$, four sets of PCSs were measured and the corresponding $\Delta\chi$ tensors determined [142]. Each sample yielded a single set of peaks, indicating the absence of diastereomers. The PCSs and RDCs were sizeable and $\Delta\chi$-tensor fits to the known ubiquitin structure produced good (i.e. small) quality factors. The alignment tensors determined from the RDCs were smaller than expected for the size of the $\Delta\chi$ tensors, indicating mobility of the tag relative to the protein, which is a common observation for tags attached to a single cysteine residue. Remarkably, sizeable PCSs were observed also for a 90 kDa sample of dimeric Lac repressor tagged with the TAHA tag and in complex with DNA and IPTG, and the complex was stable for at least two weeks at elevated temperature [142].

5.3.2.4. **Cyclen tags**

The cyclic ring structure of tetraethyleneamine alone (commonly referred to as cyclen) does not bind lanthanides with significant affinity. In contrast, the tetraacetic acid derivative DOTA (Fig. 12) binds lanthanides and other metal ions with very high affinities, producing complexes that are also kinetically inert with regard to the release of metal ions under biological conditions. Loading a DOTA-type complex with a lanthanide ion is also slow and often requires high temperatures, so that the lanthanide complexes must be prepared before they can be ligated with a protein. It may seem like a disadvantage that their extraordinary stability prohibits metal exchange after tagging of the protein, but in practice it is a big advantage not having to titrate the tagged protein with lanthanide ions, as the exact protein concentration is often unknown making accurate titrations difficult. The Cys-Ph-TAHA tag 9
has also been described for use in Ln-preloaded form [142], but other non-cyclen tags are usually loaded with lanthanides after attachment to the target protein.

DOTA tags have long been used in magnetic resonance imaging (MRI) and nuclear medicine [143]. Both the ring structure and the acetic acid pendants, however, can assume two different conformations, resulting in two pairs of enantiomeric species after lanthanide binding [144]. These conformers interconvert with a rate that is slow on the NMR time scale and therefore present distinct sets of PCSs [145, 146].

![Chemical structure of DOTA](image)

**Fig. 12.** Chemical structure of DOTA.

### 5.3.2.4.1. Double-arm cyclen tags

Early tests with the double-arm DOTA tag **11** (CLaNp-3) tied to pseudoazurine showed that bidentate anchoring to the protein was not sufficient to select a single tag conformation (Fig. 13) [147]. While the experiments revealed observable PCSs up to 35 Å from Yb$^{3+}$, peak doubling was pronounced. In addition, $^{15}$N-HSQC cross-peaks were broadened beyond detection for amides within 18 Å of the metal ion. The latter effect, however, cannot be attributed solely to PREs, as cross-peaks could be observed for amides much closer to the metal for tag **12** attached to the same protein and cysteine mutant, indicating exchange broadening by conformational exchange within the tag as an alternative explanation [141].

Starting from these initial results, a number of DOTA-based probes have been evaluated. Double-arm cyclic DOTA tags such as **11** are symmetric in their free form, but lose their symmetry upon binding to a protein. The major advantage of double-arm tags arises from their better capacity to immobilize the metal ion relative to the target protein. While tag **11** did not completely suppress the occurrence of peak doubling, the CLaNp-5 tag **12** showed no evidence for the formation of diastereomers [48, 148]. The substitution of two acetate pendants by pyridyl-$N$-oxide moieties effectively selects a single one of the diastereomeric DOTA-Ln$^{3+}$ species in solution [149, 150].
CLaNP-5 (12) has subsequently become a widely used lanthanide tag, as it avoids peak doubling and has an exceptional capacity to generate large $\Delta \chi$ tensors in proteins with Yb$^{3+}$ and Tm$^{3+}$, which are lanthanide ions that do not generate overly large PREs (Fig. 6). The superior metal immobilization and, consequently, larger $\Delta \chi$ and alignment tensors achieved by double-arm attachment of CLaNP-5 has been documented by comparison with the single-arm analogue 13 [148]. CLaNP-5 (12) has also been demonstrated to perform well at different sites of pseudoazurin, laying the foundation for the generation of different $\Delta \chi$ tensors at different sites, which ultimately allows pinpointing the location of a nuclear spin from PCSs alone [48]. Importantly, the $\Delta \chi$-tensor magnitudes measured for Yb$^{3+}$ were largely conserved at the three different protein locations, revealing this tag to be quite independent from the local environment. With Tm$^{3+}$, $\Delta \chi_{ax}$ tensor magnitudes of over $50 \times 10^{-32}$ m$^3$ have been observed with excellent correlation between experimental and back-calculated PCSs. In contrast to the $\Delta \chi$ tensors determined for calbindin D$_{9k}$ (Fig. 6), CLaNP-5 generates larger $\Delta \chi$ tensors with Tm$^{3+}$ than Dy$^{3+}$. Despite two-arm attachment, the CLaNP-5 tag is still mobile to some extent, as indicated by relaxation dispersion experiments performed with different tagging sites on pseudoazurine and cytochrome c [151]. The degree of tag mobility depends on the tagging site on the protein. This was most clearly shown by paramagnetic relaxation dispersion experiments performed with CLaNP-5 attached to adenylate kinase, where the data revealed a minor and major tag conformation differing predominately by a $23^\circ$ rotation around one of the tensor axes, with an exchange rate of 400 s$^{-1}$ [152]. CLaNP-5-Ln$^{3+}$ complexes carry a net charge of +3, which may in some cases affect the protein structure and function by altering its overall charge [40]. It has also been noted that the tagged constructs can be prone to precipitation and the tag can be lost within days or weeks. It is therefore recommended to prepare several double-cysteine mutants and use the most stable ones for further studies [67].

Further development produced CLaNP-7 (14), which contains two phenolic groups instead of N-oxides. Nitro groups lower the $pK_a$ values of the phenol hydroxyls so that deprotonation reduces the net charge of the tag-lanthanide complex to +1 [153]. Tag 14 was attached to pseudoazurine and cytochrome c. Comparison with CLaNP-5 (12) revealed slightly smaller PCSs and $\Delta \chi$-tensor magnitudes as well as different tensor orientations and metal positions. While the tag produced only a single set of PCSs with pseudoazurine, it produced two sets of peaks with cytochrome c. The effect of peak doubling was found to be pH-dependent, which could be explained by additional coordination of the Ln$^{3+}$ ion by the
imidazole ring of a histidine side chain to replace a water molecule at the ninth coordination site of the lanthanide ion, changing the symmetry of lanthanide coordination.

A more recent variation of CLaNP-5 is presented by CLaNP-9 (15), which contains two bromoacetanilide groups to react with cysteine residues by formation of chemically stable thioether rather than disulfide bonds. Tag 15 was studied with the model proteins pseudoazurine and T4 lysozyme [154]. As expected, the protein-tag complexes were inert towards reducing conditions, but the $\Delta \chi$ tensors were slightly smaller than with CLaNP-5 (12), suggesting greater mobility of the tag with respect to the protein, which may be a consequence of the overall longer tether between metal ion and protein. Unfortunately, the reactivity of tag 15 makes handling delicate and it is difficult to obtain quantitative ligation yields with target protein.

The latest double-arm tags 16a and 16b result in the same chemical linkers to two cysteine residues as the CLaNP-5 tag, but the other two pendant arms are chiral isopropanol moieties to coordinate the lanthanide ion [155]. Large $\Delta \chi$ tensors were obtained with double-cysteine mutants of ubiquitin and S. aureus 6-hydroxymethyl-7,8-dihydropterin pyrophosphokinase (HPPK).

Fig. 13. Thiol-reactive and bioorthogonal cyclen probes and ligation products. The reactive groups for covalent attachment to cysteine (11-24) or for click reactions (25, 26) are drawn in bold. Activating groups for covalent attachment to cysteine are drawn in bold. Tags 11, 12, 14, 15 and 16a/b are double-arm tags.

5.3.2.4.2. Single-arm cyclen tags binding to cysteine
Double-arm tags carry two reactive groups for ligation to two reactive groups on the target protein so as to reduce metal mobility; however, such tags also carry the potential to form covalent dimers and multimers. An alternative is presented by single-arm tags, which require only a single reactive group on the protein. As a drawback, single-arm tags are almost always associated with greater metal mobility relative to the protein.

The first single-arm cyclen tag was the DOTA-M8 tag 17. This tag contains eight methyl groups and is enantiomerically pure at all corresponding stereo-centres, to bias the conformational equilibria of the cyclen ring and its pendant arms towards a single conformation. Loaded with Dy\(^{3+}\) and linked to two different sites of ubiquitin, the tag delivered very large PCSs and \(\Delta\chi\) tensors, whereas the corresponding tag without methyl groups (tag 18) produced only very small PCSs and displayed broad lines due to conformational exchange [156]. In both samples, the tag also generated a second species (15-20% at 25 °C, 50% at 50 °C), which displayed a \(\Delta\chi\) tensor similar in magnitude, but different in orientation and metal position compared to the main species. Initially, the minor species was suggested to arise from \(cis/trans\) isomerization of the peptide bond within the linker, but it was later shown to stem from a slow conformational equilibrium between two different lanthanide coordination geometries, referred to as square antiprism (SAP) and twisted square antiprism (TSAP) [157]. The population ratio between the two forms depends on the ionic radius of the lanthanide. At 25 °C and pH 6.5, the complex with Pr\(^{3+}\) populates the SAP conformation to 98%, whereas the complex with Yb\(^{3+}\) is 95% in the TSAP conformation and both conformations are approximately equally populated in the complex with Ho\(^{3+}\). In complex with the DOTA-M8 tag, only lanthanide ions with larger ionic radii can coordinate a hydration water molecule, which results in greater temperature sensitivity of the \(\Delta\chi\) tensors [158].

In a very recent variation of the DOTA-M8 tag 17, referred to as M8-CAM-I, the ethylenedithiopyridyl group in tag 17 was replaced by a propylidioacetamide (\(-\text{C}_3\text{H}_6\text{NHCOCH}_2\text{I}\)) group for reaction with cysteine by formation of a thioether bond, which is stable under the reducing conditions of in-cell NMR [159]. Due to the greater length of the tether, smaller \(\Delta\chi\) tensors were observed for two different cysteine mutants of ubiquitin than with the original DOTA-M8 tag 17 and the quality factors of the \(\Delta\chi\)-tensor fits were generally worse. Conformational heterogeneity with SAP and TSAP conformations was avoided by measuring PCS data only for Dy\(^{3+}\).
Tag 19a (named C1) solves the problem of multiple species [160]. Initially studied with ubiquitin and ArgN, this tag contains amide instead of carboxylate pendants, yet it still binds lanthanide ions with high affinity. Loading the tag with a lanthanide ion requires harsh conditions (80 °C, overnight) and therefore must be completed before the tag can be reacted with a protein. The C1 tag produces only a single set of paramagnetic peaks and, dependent on the solvent exposure of the tagging site, the $\Delta \chi$ tensors can be large as the bulkiness of the tag limits motions of the lanthanide relative to the protein. The magnitudes of the $\Delta \chi$ tensors follow the usual sequence observed for calbindin D$_{9k}$ (Fig. 6), with $\Delta \chi_{ax}$ magnitudes decreasing in the sequence Dy$^{3+} >$ Tb$^{3+} >$ Tm$^{3+} >$ Yb$^{3+}$. The tag contains three chiral centres in its pendant arms.

Tag 19b (C2) is the enantiomer of C1 of opposite chirality. In combination with C1, the C2 tag is useful for producing a different $\Delta \chi$ tensor with the same protein tagging site. Both tags have been used at three different sites of the dengue virus protease NS2B-NS3. Using C1-Tm$^{3+}$, C1-Tb$^{3+}$, C2-Tm$^{3+}$ and C2-Tb$^{3+}$ tags, 12 sets of PCSs were obtained to elucidate the conformation of the protein [161]. The bulky, hydrophobic pendant arms shield the net charge of the tags (+3) to some extent, but may generate unintended binding sites for hydrophobic ligand molecules.

The C5 tag (20) is a variant of the C1 tag, containing three pendant arms consisting of chiral (S)-2-hydroxypropyl groups instead of phenethylacetamide groups [162]. Additional variants of C5 were produced with different tethers to the cysteine sulfur atom, where C6 (21) contains a different, more rigid, picolinic acid-derived linker and C7 (22a) and C8 (22b) employ yet another tether that generates a more symmetric coordination sphere for the lanthanide ion [162]. In addition, C8 was synthesised, which is the enantiomer of C7. Following ligation to the A28C mutant of ubiquitin, PCSs measured with Dy$^{3+}$, Tb$^{3+}$, Tm$^{3+}$ or Yb$^{3+}$ produced the lowest $Q$ factors for the C7 and C8 tags. Their $\Delta \chi_{ax}$ values were larger on average than those obtained with the C1 and C2 for the same ubiquitin mutant. In contrast to C1 and C2, which reliably generate PCSs of opposite sign with Tb$^{3+}$ and Tm$^{3+}$, the relative order and size of PCSs induced by the C5 – C8 tags proved to be variable, suggesting changes in coordination environment with each lanthanide ion. Unexpectedly, some of the largest $\Delta \chi$ tensors were obtained with Tm$^{3+}$ (also confirmed with a cysteine mutant of GB1) and an unusually large $\Delta \chi$ tensor was obtained with the C7-Tm$^{3+}$ tag attached to a single-cysteine mutant of HPPK [162].
The C9 tag forms a tether to cysteine as short as the C7 and C8 tags but contains phenethylacetamide pendants like the C1 – C4 tags. To date, data have been published only for C9 loaded with Gd\(^{3+}\) for distance measurements by EPR spectroscopy, where it produces particularly narrow distance distributions [163].

Lanthanide complexes of the recently published DO3MA-6MePy (23) and DO3MA-Py (24) tags have a net neutral charge and only a single aromatic group [164]. In addition, these tags form thioether bonds with cysteine residues, resulting in chemically stable ligation products and short tethers between protein backbone and lanthanide ion, generating very large \(\Delta\chi\) tensors. As a drawback, the ligation reactions are slow even at pH 9, raising the possibility of incomplete ligation yields.

5.3.2.4.3. Single-arm cyclen tags binding to p-azido-L-phenylalanine

The chemical inertness of cyclen-lanthanide complexes opens up opportunities to consider chemistries other than disulfide or thioether linkages for site-specific tagging. As most wild-type proteins contain cysteine residues, altering the protein construct to contain only a single reactive thiol group at a selected site can be cumbersome and have unintended consequences for the protein stability and activity. p-azido-L-phenylalanine is an unnatural amino acid that can readily be encoded by an amber stop codon [165], and selectively reacted with a tag containing an acetylene group in a cycloaddition reaction that can be performed in the presence of cysteine.

Cu\(^{+}\)-catalysed click-reaction with the septadentate tag 25 (C3) has been demonstrated with three different proteins. The resulting tether between lanthanide ion and protein backbone is quite long, but the triazole formed presents a rigid unit that can also coordinate to the metal ion. The alternative octadentate tag 26 (C4) produced greater ligation yields but smaller PCSs, which proved more difficult to fit by a single \(\Delta\chi\) tensor, as expected for a more flexible tether [166]. His\(_6\) tags were found to inhibit the ligation reaction, which may be attributed to their copper binding capacity. Subsequent work showed that many proteins are sensitive to precipitation in the presence of copper, even when the copper catalyst is provided as a complex with a multi-dentate ligand such as BTTAA [167, 168].
Fig. 14. Probes for covalent (thiol-reactive or bioorthogonal) tagging based on pyridine or iminodiacetic acid (IDA) or nitrilotriacetic acid (NTA) derivatives. Some of the smallest probes are based on dipicolinic acid (DPA). The 8-hydroxyquinoline probe \( \text{45} \) has only been used as a tag with transition metal ions. The reactive groups for covalent attachment to cysteine (\( \text{27-41, 45} \)) or click reactions (\( \text{42-44} \)) are drawn in bold.

5.3.2.5. Tags based on dipicolinic acid

Dipicolinic acid (DPA) binds lanthanide ions with nanomolar binding affinities despite being no more than a tridentate ligand (Fig. 15). The complex between a DPA molecule and a \( \text{Ln}^{3+} \) ion is non-chiral, avoiding the problem of peak doubling associated with chiral metal complexes [169]. In addition, DPA-based tags are much smaller than any EDTA or cyclen tags, minimizing their possible impact on the protein structure. The first DPA tag developed for PCS measurements was \( \text{4MMDPA (27)} \). Following attachment to ArgN, a comparison between the \( \Delta \chi \) tensors determined from PCSs and alignment tensors determined from RDCs indicated good immobilization of the metal ion, but the \( \Delta \chi \) tensors were smaller in magnitude than for, e.g., cyclen tags [170]. Conceivably, filling most lanthanide coordination sites with water molecules does not promote large \( \chi \)-tensor anisotropies. On the
other hand, the accessibility of the lanthanide ion allows additional coordination by side chain carboxyl groups from the protein, contributing to immobilization of the metal by an effective two-point attachment as suggested for the ArgN-4MMMDPA construct. As the thiol group of tag 27 is not activated, attachment to the cysteine residue of a protein requires prior activation of the cysteine thiol group with, e.g., DTNB, as in the case of lanthanide binding peptides.

![Chemical structure of the complex between dipicolinic acid (DPA) and a lanthanide ion.](image)

**Fig. 15.** Chemical structure of the complex between dipicolinic acid (DPA) and a lanthanide ion.

An even smaller tag than 4MMMDPA is presented by 3MDPA (28), which is less symmetrical than 4MMMDPA but produces a shorter linker with the protein as the reactive thiol group is directly linked to the aromatic ring. 3MDPA is one of the smallest reported lanthanide tags [171]. The tag was studied with ArgN using seven paramagnetic lanthanide ions and Co$^{2+}$. As expected, the tag produced different $\Delta\chi$-tensor orientations from the 4MMMDPA tag. The smaller magnitude of the $\Delta\chi$ tensors seemed to arise from the difficulty of coordinating with a side-chain carboxyl group of ArgN. Dy$^{3+}$ produced the largest PCSs, whereas Er$^{3+}$ unexpectedly produced smaller PCSs than Tm$^{3+}$ and Co$^{2+}$. The 3MDPA tag may depend more critically on additional immobilization, either by steric restraints or by metal coordination with protein side chains, as only very small PCSs could be observed with a cysteine mutant of T4 lysozyme [171].

The disulfide-linked dimer of 4MDPA (29) was synthesized to produce a more symmetrical analogue of the 3MDPA tag. The dimer can be used directly as tagging reagent, as 4-mercaptopo-DPA is a good leaving group [172]. Lanthanide complexes of ArgN tagged with 29 displayed similar $\Delta\chi$-tensor magnitudes to those with the 3MDPA tag, whereas significantly larger $\Delta\chi$ tensors were observed with the 4MDPA tag attached to the intracellular domain of the rat p75 neurotrophin receptor, which was attributed to additional metal coordination by a side chain carboxyl group of the protein [172]. The effective $\Delta\chi$ tensors generated by the small DPA tags thus seem to be particularly sensitive to additional coordination by protein carboxylates.
Whereas tags 27-28 are all attached to the protein of interest via disulfide bridges to cysteine residues, the DPA-based tag 30 can be added to cysteine residues via a thiol-ene reaction to create chemically more inert thioether tethers [173]. The alkene function acts as a Michael acceptor for thiol groups, no further activation of the tag or protein is required, and an excess of tagging reagent can be used, greatly facilitating high ligation yields. The resulting ligation product resembles the product obtained with the 4MMDPA tag 27, except that one of the sulfur atoms is replaced by a methylene group. Following attachment to ArgN, similar $\Delta\chi$ tensors were obtained to those with 4MMDPA. Following attachment to the ubiquitin mutant T22C, the metal ion was found in the proximity of the carboxyl group of Asp21, indicating immobilisation by this additional interaction. The Michael addition reaction produces a stable product, which is inert towards reducing agents, but the reaction rate is much slower than that of tags activated with methylsulfonyl or thiopyridyl groups. Therefore, inaccessible cysteine thiol groups buried inside proteins remain unmodified.

Michael addition reactions using a vinyl group offer an elegant escape from the dilemma that conventional maleimide tags create a new chiral centre upon ligation to thiol groups, resulting in diastereomers with proteins and, hence, peak doubling in NMR spectra. This has been demonstrated experimentally with a DPA tag (31) attached to maleimide [173].

The concept of Michael additions via vinyl groups was subsequently extended to a larger tag with greater lanthanide ion affinity. 4VPyMTA (32) shows even higher binding affinities toward lanthanides than EDTA [174]. The tag was tested with two different cysteine mutants of ubiquitin. In each case, only a single set of cross-peaks was observed in the presence of a paramagnetic lanthanide ion. Despite the greater bulkiness of 4VPyMTA compared with 4MMDPA (27), tag flexibility resulted in relatively small $\Delta\chi$ tensors. Recently, the 4MMPyMTA tag (33) has been reported, which reacts with a cysteine residue by formation of a disulfide linkage [175]. The resulting tether is the same as for the 4VPyMTA tag, except that a CH$_2$ group is replaced by a sulfur atom.

Similarly, the terpyridine-based tag 4MTDA (34) is a bulkier tag, related to DPA but designed to deliver a greater binding affinity. Its ligation to proteins via a disulfide bond follows the conventional approach, where cysteine residues are first activated with DTNB. Titration experiments with DPA confirmed that the lanthanide binding affinity of ubiquitin tagged with 4MTDA was very high. Attached to a cysteine residue in position $i$ of an $\alpha$-helix, the tag allows additional metal coordination by the carboxyl group of a glutamate residue in position $i-4$ of the same helix, resulting in large $\Delta\chi$ tensors and outstanding quality factors.
Similarly good results were obtained for a non-helical attachment site with a glutamate carboxyl group in the vicinity of the tag. While the observed Δχ tensors were significantly larger than for other DPA tags, the ligation yields were only about 50-70%.

Another bulky tag with high lanthanide affinity is 35 [177]. It reacts spontaneously with a cysteine residue. Using the D82C mutant of S. aureus sortase A, complete ligation was observed within 8 hours without affecting the more buried cysteine residue at the active site.

A direct bond between a pyridine ring, as in DPA, and a cysteine thiol group presents the shortest conceivable tether. As a good leaving group, the phenylsulfonyl group allows this bond to be formed in aqueous solution, resulting in a thioether. The approach was demonstrated by the 4PS-DPA tag (36), the 4-PS-PyMTA, (37) [178] and 38 [177]. Tag 36 showed that the ligation reaction is selective and complete after about 10 hours at 25 °C. Like other DPA tags, however, additional coordination by a protein carboxylate is required to obtain useful PCSs. Attached to the highly solvent-exposed site of Gly47 of ubiquitin, the 4PS-PyMTA tag 37 produced sizeable PCSs, throughout the protein, that were much larger than for tag 32 at the same site. This result demonstrates the value of a shorter tether (two methylene groups fewer than in tag 32) at a site where no protein carboxylates are nearby. Tag 38 was ligated to the D82C mutant of S. aureus sortase A at pH 7.6 overnight in about 80% yield and produced intermediate size Δχ tensors with good quality factors. The ligation rate is faster at pH 8. Importantly, tag 38 did not react with the less solvent-exposed cysteine residue in the active site.

Regardless of whether additional complexation by a side-chain carboxyl group of the protein occurs or not, cyclen-based tags tend to deliver larger Δχ tensors than DPA-based tags.

5.3.2.6. Tags based on NTA

Nitrilotriacetic acid (NTA)-based tags were designed in an attempt to minimize the size of the tag without compromising metal binding affinity. As in the case of DPA tags, Ln3+ ions complexed by an NTA tag retain unoccupied coordination sites, allowing immobilization of the metal ion by additional coordination to a protein carboxylate. Following attachment to ArgN and cysteine mutants of ubiquitin, the NTA-SH tag 39 produced single sets of paramagnetic cross-peaks for all four paramagnetic lanthanides analysed. As the metal binding affinity of NTA is lower than that of EDTA, EDTA can be used to remove the bound lanthanide to allow substitution by another lanthanide [179]. In the case of ArgN, the PCSs measured were comparable in magnitude to those observed with 4MMDPA (27), although the
lanthanide ion appeared to be at a distance of 4.7 Å from the nearest carboxyl group of the protein, which would be too far for direct complexation. In contrast, ubiquitin produced smaller PCSs despite the presence of two protein carboxyl groups in proximity to the metal ion. Compared with the lanthanide-DPA complexes, the lanthanide-NTA complex seems to engage less readily in complexation by additional carboxyl groups of the protein, possibly due to its smaller net charge (0 for the NTA-Ln$^{3+}$ complex, +1 for DPA-Ln$^{3+}$). Most interestingly, a two-point anchoring approach has been realized with the NTA-SH tag 39 by attaching a tag to each of two cysteine residues located at positions $i$ and $i+4$ of the $\alpha$-helix in ubiquitin. This generated large PCSs, excellent correlations between experimental and back-calculated PCSs, and also an alignment tensor in agreement with the $\Delta\chi$ tensor [179].

5.3.2.7. Tags based on IDA

To reduce the size of the lanthanide tag even further, the iminodiacetic acid (IDA)-based tags 40/41 contain only two carboxyl groups. The complex with Ln$^{3+}$ ions carries a positive net charge (+1), promoting additional coordination by a carboxyl group of the protein. This was demonstrated with the A28C mutant of ubiquitin, where the IDA-SH tag 40 was found to position the lanthanide ion close to the carboxyl group of Asp32 located in the same $\alpha$-helix [73]. The magnitudes of the $\Delta\chi$ tensors observed for six different paramagnetic lanthanide ions followed the sequence observed for calbindin D$_{9k}$ (Fig. 6), with a very large $\Delta\chi$ tensor for Dy$^{3+}$, excellent correlations between experimental and back-calculated PCSs, and very good agreement between the $\Delta\chi$ tensor and alignment tensor determined with Tb$^{3+}$, indicating outstanding rigidity for such a small probe. Most interestingly, addition of an excess of a 1:1 mixture of diamagnetic La$^{3+}$ and paramagnetic Dy$^{3+}$ allowed the observation of exchange cross-peaks between the auto-peaks of the diamagnetic and paramagnetic protein, facilitating the assignment of the paramagnetic NMR spectrum [73], using an NMR experiment applied previously to measure PCSs in $\varepsilon_{186}$ [70]. Unfortunately, exchange cross-peaks have proven difficult to observe in other proteins (see Section 4.4.2).

5.3.2.8. Prediction of assisted complexation by protein carboxylates

The performance of the NTA- and IDA-based tags 39 and 40 relies strongly on opportunities for additional coordination by neighbouring side-chain carboxyl groups in the protein. A systematic study conducted to assess the predictability of such additional coordination positioned either the NTA-SH tag 39 or the IDA-SH tag 40 at position $i$ of an $\alpha$-
helix in the C-terminal domain of ERp29, and either an aspartate or glutamate residue at position \( i+4 \) or \( i-4 \) in the same helix. For NTA-SH tag, the largest \( \Delta \chi \) tensors were obtained with a glutamate residue in position \( i-4 \). For the IDA-SH tag, only an aspartate residue in position \( i+4 \) produced significant \( \Delta \chi \) tensors [74]. The \( \Delta \chi \) tensors obtained with the IDA-SH tag were somewhat smaller than those reported previously for ubiquitin [73] and exchange cross-peaks between diamagnetic and paramagnetic samples were difficult to observe, suggesting that the performance of the tag is sensitive to small conformational differences between \( \alpha \)-helices in different proteins.

It is interesting to note that all NTA- and IDA-based tags are expected to coordinate lanthanide ions in a chiral fashion, but peak doubling has never been observed in NMR spectra of proteins ligated with these tags, probably because of rapid exchange between the diastereomeric species or because the chiral centre next to the attachment site of the tether biases the population of the diastereomers.

5.3.2.9. NTA and IDA tags for ligation by click chemistry

Recently, “clickable” versions of NTA- and IDA-based tags have been reported, comprising the alkyne-NTA tag 42, the alkyne-IDA1 tag 43 and the alkyne-IDA2 tag 44, which can be attached to \( p \)-azido-\( L \)-phenylalanine [167]. In this work, the azido group was found to be prone to inactivation by the reducing conditions of the \( E. \) coli cytosol, ultimately limiting the ligation yields to between 50 and 80\%. The alkyne-NTA tag was tested for two sites of ubiquitin and three sites of GB1, and the alkyne-IDA1 and alkyne-IDA2 tags were tested for the same sites of GB1. Titrating the constructs with \( \text{Tb}^{3+} \) or \( \text{Tm}^{3+} \), sizeable \( \Delta \chi \)-tensor magnitudes were observed irrespective of the presence of additional protein carboxyl-groups to assist the coordination of the lanthanide ion, which was attributed to the limited conformational freedom of the tether between the protein backbone and the lanthanide ion. Notably, however, all these tags result in rotatable, barely constrained bonds next to the metal complex, which allows the metal ions to move to some extent, making the tensor magnitudes and quality factors hard to predict. It was concluded that fewer bonds (tag 43 versus tag 44) make better tags, even if the additional degrees of rotational freedom of a longer tether may put a protein carboxyl group within reach. In the absence of additional coordination by protein carboxyl groups, NTA tags may be preferable over IDA tags in view of their greater affinity for lanthanides [167].
5.3.2.10. Commercial availability

Owing to a largely experimental character, some of the tags discussed above have been reported in single articles only. Nonetheless, a number of tags are commercially available at the time of this review. These include the EDTA tags 4 and 5 (Fig. 11), the CLaNP-5 tag 12, the DOTA-M8 tag 17 (Fig. 13), the DPA tags MMDPA 27, 3MDPA 28, 4-vinyl-DPA 30, the alkyne-IDA tags 43 and 44 and the 2-vinyl-8-hydroxyquinoline tag 45 (Fig. 14).

5.3.3. Non-covalently binding tags

Site-specific attachment of tags to a target protein does not necessarily depend on the formation of covalent bonds, but can also be achieved by non-covalent association. In principle, this approach does not require any chemical modification of the protein, allowing recovery of the protein after the experiment. If the tag exchanges rapidly between the protein-bound and free state, the paramagnetic cross-peaks can be assigned in a straightforward titration experiment to observe gradual spectral changes from the free protein towards the tagged protein. Unfortunately, binding specificity and rapid chemical exchange between bound and free tag tend to be mutually exclusive requirements, and it is a challenge to obtain a defined orientation of the $\Delta\chi$ tensor relative to the protein for a rapidly exchanging tag. Only a few examples of PCSs generated in this way have been reported to date.

5.3.3.1. Non-covalently binding synthetic tags

Many proteins that are not metallo-proteins, such as ubiquitin, contain weak binding sites for the aquo ions of paramagnetic lanthanides, which can generate small PCSs. Soluble lanthanide complexes, however, can bind more specifically. In an early example, DTPA complexes of different lanthanides were shown to change chemical shifts in the protein FKBP, which were proposed to assist resonance assignments by resolving accidental chemical shift degeneracies [180]. No $\Delta\chi$ tensors were determined.

$[\text{Ln(DPA)}_3]^{3-}$ complexes carry an even greater charge than Ln-DTPA complexes and were successfully used for PCS, RDC and PRE measurements [181-184]. The dipicolinic acid molecules bind the lanthanide ion in a nonadentate complex with propeller-like geometry. Despite the chirality of this complex, only a single set of paramagnetic cross-peaks was observed for the protein. Fast exchange between the different propeller chiralities is not unexpected, as the exchange can proceed without dissociation of the DPA ligands from the lanthanide ion.
Predicting the binding sites of DTPA or DPA complexes on proteins is not always straightforward. In the case of the IDA-Cu$^{2+}$ complex, high selectivity for a single solvent-exposed histidine residue has been reported, allowing determination of distance restraints from PRE measurements [185]. Unfortunately, this approach is not available for lanthanide ions as their affinity for nitrogen ligands is very low.

In the case of [Ln(DPA)$_3$]$^{3-}$ complexes bound to ArgN, Δχ-tensor fits located the complexes in the vicinity of positively charged amino acid side-chains [181]. Beyond electrostatic attraction, cation–π interactions may contribute to the binding [186]. A comprehensive study of many proteins concluded that two basic residues (arginine or lysine) suffice to generate a binding site for [Ln(DPA)$_3$]$^{3-}$, provided that no acidic side chains from aspartate or glutamate are nearby that could engage the arginine and lysine residues in salt bridges. In wild-type proteins, it is rare to find situations where two basic residues are nearby without either of them being able to engage in a salt bridge. Therefore, one or two mutations suffice to generate a binding site [183]. Notably, however, the magnitudes of the Δχ tensors obtained with [Ln(DPA)$_3$]$^{3-}$ complexes were almost always much smaller than those obtained with covalently bound tags, which may in part be due to the flexibility of the long side chains of arginine and lysine. As the binding affinities of [Ln(DPA)$_3$]$^{3-}$ complexes to proteins are weak (high micromolar to low millimolar range), it is not always possible to obtain 1:1 complexes with the target protein without also starting to populate alternative binding sites, although the chance of populating a single binding site is high if protein and DPA complex are used in equimolar ratio [181].

As PREs are effective regardless of lanthanide mobility, use of PREs generated by binding of [Gd(DPA)$_3$]$^{3-}$ has been explored. Gd$^{3+}$ generates much larger PREs than nitroxide radicals and there is no paramagnetic metal ion with isotropic χ tensor that would give PREs of intermediate size. However, scaling of PREs can be achieved by titration with [Gd(DPA)$_3$]$^{3-}$. Due to the fast exchange between bound and free [Gd(DPA)$_3$]$^{3-}$ complex, the PRE effects are correspondingly smaller with substoichiometric ratios of complex to protein than they are in the 1:1 complex with the paramagnetic agent [182]. [Gd(DPA)$_3$]$^{3-}$ also binds to His$_6$-tags or RAAAR peptide tags with submillimolar affinity, which can be used to elicit PREs [183].

A recent study analysed the effect of additional bromide, -CO$_2$H or -CH$_2$OH substituents at two different positions of the aromatic ring of the DPA molecule [184]. Using ubiquitin as the model protein, the lanthanide complexes formed with these DPA derivatives
displayed different $\Delta \chi$-tensor magnitudes and orientations. The lowest $Q$-factor of the $\Delta \chi$-tensor fit was obtained with the asymmetric bromide derivative.

5.3.3.2. Non-covalently binding protein tags

Metal ions can also be attached to proteins by tags that bind non-covalently and achieve site-specificity by recognizing specific structural features of the protein. This strategy was first demonstrated using calmodulin loaded with four Tb$^{3+}$ ions as the paramagnetic tag. Binding to a calmodulin binding peptide fused with the target protein was shown to generate significant RDCs in the target protein while the PCSs remained small [187]. The concept was extended in recent experiments that used the Erbin PDZ domain tagged with CLaNP-5 (12) to bind to the short peptide TGWETWV fused to ubiquitin or maltose binding protein. A single lanthanide attached to the PDZ domain was sufficient to generate significant RDCs and allowed fitting of the PCSs observed in the target protein by a single $\Delta \chi$ tensor [188]. The PDZ domain is fairly small (103 residues) and recognizes the fusion peptide with high affinity. Importantly, by using different double-cysteine mutants of the Erbin PDZ domain tagged with CLaNP-5, different molecular alignments of the same target protein were readily generated.

5.4. Metal-binding unnatural amino acids

Over 100 different unnatural amino acids can be incorporated into proteins by genetic encoding [189]. Some of these amino acids can bind metal ions. Unfortunately, the only unnatural amino acid that can bind lanthanides with adequate affinity is 2-amino-3-(8-hydroxyquinolin-3-yl)propanoic acid (HQ-Ala), which has a side chain with an 8-hydroxyquinoline (8HQ) moiety. Many trials have shown that binding of lanthanides to solvent-exposed 8HQ residues results in quantitative protein precipitation [190], presumably because the coordination of the lanthanide is only bidentate, leaving too many coordination sites free to be occupied by other metal binding substituents from the protein.

6. Generating PCSs with Co$^{2+}$

6.1. Co$^{2+}$ binding proteins

Co$^{2+}$-binding proteins are relatively rare, but zinc-binding proteins constitute a very large class of metalloproteins and often zinc can be replaced by Co$^{2+}$ [191], allowing PCS measurements. Although the affinity of zinc fingers for Co$^{2+}$ is about four orders of
magnitude lower than for Zn$^{2+}$, binding affinities in the nanomolar range can still be observed [192]. In an early example, PCSs were measured in this way for the transcription factor ADR1 that comprises a two-finger array of His$_2$-Cys$_2$ zinc fingers [193]. The $\Delta\chi$-tensor parameters of the Co$^{2+}$ ions were assumed to be the same as those determined previously for a consensus His$_2$-Cys$_2$ zinc finger [194] and the observation of PCSs for an accessory polypeptide segment in the presence, but not the absence, of DNA was interpreted in terms of a disorder-to-order transition upon DNA binding [193]. Fitting $\Delta\chi$-tensors for both Co$^{2+}$ centres from the single set of experimental PCSs would be challenging, as this would involve optimising a total of 16 tensor parameters. Substitution of Zn$^{2+}$ by Co$^{2+}$ in a Cys$_2$-His-Cys zinc finger motif has also been shown to produce large PCSs [195].

In another example of zinc-binding proteins, bovine and human carbonic anhydrase II, large PCSs were observed in the Co$^{2+}$-substituted enzymes. The magnitude of PCSs allowed determining the $\Delta\chi$ tensor using random coil chemical shifts as the diamagnetic reference and the tensor was interpreted in terms of metal coordination geometry [196, 197].

PCSs were similarly observed in the two-domain protein PA0128 from Pseudomonas aeruginosa by substituting a Zn$^{2+}$ ion in the N-terminal domain by a Co$^{2+}$ ion. Although no $\Delta\chi$-tensor parameters could be determined, the PCSs generated by the Co$^{2+}$ ion made it possible to interpret line-broadening effects in the C-terminal domain in terms of concerted domain motions [198].

As a final example, PCSs measured for the Co$^{2+}$-substituted matrix metalloproteinase 12 (CoMMP-12), which naturally binds Zn$^{2+}$, have been used to obtain structural information about neighbouring molecules in a single-crystal environment and refine the 3D structure of the protein [199, 200]. The protein was used to show that nuclear spins in close proximity to the Co$^{2+}$ ion become observable by solid-state NMR with ultrafast magic angle spinning [201]. A very recent study used these data to validate a novel multi-scale quantum-chemical approach for accurate PCS predictions in metalloproteins [202].

6.2. Co$^{2+}$ complexes generating sizeable PCSs

Many lanthanide tags, for example EDTA, NTA and IDA tags, also bind Co$^{2+}$ and Zn$^{2+}$ (as the diamagnetic reference) very well. Tagging strategies using Co$^{2+}$ as well as lanthanides have been discussed above. Unlike lanthanide ions, however, cobalt has a greater affinity for nitrogen ligands and binds more easily to bidentate ligands, which makes it possible to attach Co$^{2+}$ ions to sites where lanthanides would not bind. An early example was
the complex between the DNA octamer d(TTGGCCAA)$_2$ and chromomycin-A$_3$, where Co$^{2+}$ was bound to two oxygens of the chromophore [203, 204]. The measured PCSs greatly improved the quality of the NMR structure of the DNA-drug complex. PCSs restraints from Co$^{2+}$ were also used to characterize complexes of helical peptides covalently connected to a cobalt-affine bipyridyl moiety [205]. Another early attempt used EDTA tag 4 attached to the E. coli arginine repressor [135]. As discussed in section 5.3.2.1, the racemic nature of the EDTA-Co$^{2+}$ complex resulted in peak doubling arising from two sets of PCSs.

The IDA-tag 41 attached to two cysteine residues in an $i, i+4$ arrangement within the $\alpha$-helix of ubiquitin has been shown to lead to a hexadentate EDTA-like motif with Co$^{2+}$, producing a good correlation between predicted and measured PCSs with a fairly large $\Delta \chi_{ax}$ value of $-7.3 \times 10^{-32}$ m$^3$ [206]. Recently, Co$^{2+}$ bound to the cysteine-reactive 8-HQ probe 45 was used to measure PCSs, RDCs and PREs in ubiquitin, and $\Delta \chi_{ax}$ values up to $-10.3 \times 10^{-32}$ m$^3$ were reported [207]. While these magnitudes are respectable, larger paramagnetic effects can be obtained with lanthanide than with Co$^{2+}$ ions. For example, a direct comparison between lanthanides and Co$^{2+}$ using the 3MDPA tag (28) attached to ArgN gave $\Delta \chi_{ax}$ values of $-17.0 \times 10^{-32}$ m$^3$ and $-4.6 \times 10^{-32}$ m$^3$ for Dy$^{3+}$ and Co$^{2+}$, respectively [171]. An exceptionally large $\Delta \chi_{ax}$ value of $12.6 \times 10^{-32}$ m$^3$ has recently been reported for a special Co(II) clathrochelate compound dissolved in CDCl$_3$ [208].

6.3. Creating a Co$^{2+}$ or Mn$^{2+}$ binding site with an unnatural amino acid

The first example of generating PCSs by directly binding a paramagnetic metal ion to an unnatural amino acid employed (2,2'-bipyridin-5-yl)-L-alanine (BpyAla) incorporated at three different sites of the West Nile virus NS2B-NS3 protease [209]. The amino acid binds Co$^{2+}$, but for two of the mutants only PREs and no PCSs were observed, indicating conformational averaging of the PCSs due to side-chain flexibility. The third mutant produced PCSs that could be used to derive the corresponding $\Delta \chi$ tensor, suggesting that immobilization of the metal ion was aided by additional interaction with a histidine side chain of the protein.

More recently, HQ-Ala incorporated into two different membrane proteins in DHPC micelles has been shown to produce specific binding sites for Mn$^{2+}$ which could be substituted by Zn$^{2+}$ for PRE measurements [210]. In contrast to previous results with water-soluble proteins, metal ion binding did not trigger precipitation of the protein.
7. Macromolecular structure from pseudocontact shifts generated by lanthanide and cobalt tags

7.1. 3D protein structure refinements using PCSs from lanthanides

PCSs present structure restraints that provide highly useful information in 3D structure refinements, like numerous other, more traditional NMR parameters, such as nuclear Overhauser effects (NOE) and scalar coupling constants. Structure restraints from PCSs have been used to assist 3D structure refinements of metallo-proteins for over 20 years [89]. Structure refinement using PCSs from a metal tag (the EDTA tag 4 loaded with Co²⁺) was demonstrated in 2004, where the tag was attached to cysteine residues at three different sites [211].

With lanthanides bound to proteins, not only do large PCS effects (spanning over 40 Å [12]) become available, but also significant RDCs. Therefore, lanthanides have been used in structure refinements not only to obtain PCSs but also RDCs. For example, a study of two different calmodulin-peptide complexes used the N60D mutant of calmodulin with three different paramagnetic lanthanides, to refine the corresponding crystal structures by PCSs and ¹H-¹⁵N RDCs. The results highlighted the much better fit of back-calculated to experimental data for PCSs than for RDCs prior to structure refinement [212]. This feature is readily explained by the relative insensitivity of PCSs to small changes in bond angles. PCSs are thus particularly helpful in structure refinements that aim for the global fold of the protein rather than fine structural detail.

A recent proof-of-principle study demonstrated that 3D protein structures can also be determined with the help of PCS data measured in the solid state using magic angle spinning (MAS). PCSs were measured of ¹³C and backbone ¹⁵N spins of GB1 with the MMDPA (27) tag attached at three different sites, using Co²⁺, Yb³⁺, and Tm³⁺ ions to generate PCSs [213]. To avoid intermolecular PCSs, tagged GB1 was diluted 4 to 8-fold with untagged GB1. The root mean square deviation (RMSD) of the Cα atoms was as low as 0.7 Å with respect to the crystal structure. Solid-state MAS NMR has the advantage that solid-state signals are not subject to Curie spin relaxation [214], allowing observation of NMR signals of ligands that directly coordinate the paramagnetic metal ion [201].

Starting from a crystal structure, PCS data measured in solution have also been used to judge whether a protein structure is conserved in solution. PCSs and ¹H-¹⁵N RDCs of backbone amides were measured of a double-cysteine mutant of metalloproteinase MMP-1
ligated with a CLaNP-5 tag (12) (loaded with Tb$^{3+}$, Tm$^{3+}$ or Yb$^{3+}$) and the data were combined with the electron density observed in the crystal structure in order to determine a solution structure that fulfils the paramagnetic restraint while being closely similar to the crystal structure [215]. Very good agreement between experimental and back-calculated data was obtained for the refined structures, and the backbone RMSD between crystal and refined structures was lower than 0.4 Å. The same protocol applied to the N60D mutant of calmodulin complexed with DAPk peptide yielded less good fits.

Recently, PCSs generated by the tags 35 and 38 loaded with Tm$^{3+}$ or Tb$^{3+}$ and ligated to a cysteine residue in position 82 of S. aureus sortase A were used to determine the structures of loop segments of this protein in a transient intermediate [177]. More details are discussed in Section 7.4.5.

7.2. 3D protein structure determinations using PCSs generated by lanthanide tags

Going beyond structure refinement, PCSs can also be used for 3D structure determinations, if initial models of the protein can be built that allow fitting of $\Delta\chi$ tensors, as in the strategies implemented in the programs PCS-Rosetta and GPS-Rosetta [98, 99]. Although Rosetta can model the structures of small proteins without any experimental input beyond the amino-acid sequence [216], experimental restraints not only allow verification, but actually gain critical importance for determining the folds of proteins with more than about 120 residues. PCSs are uniquely suited in this context due to their long-range nature. Furthermore, PCSs of backbone amide protons can be measured in sensitive two-dimensional $^{15}$N-$^1$H correlation spectra, which present the best-resolved 2D NMR spectra of proteins.

While the concept of de novo protein structure determination (as opposed to structure refinement) exclusively from PCSs generated by lanthanide tags has been established, actual experimental examples are still rare. GPS-Rosetta was demonstrated using the C-terminal domain of ERp29, which is a construct of 127 residues [217]. The 3D structure was obtained using backbone amide PCSs generated from four different tagging sites using IDA-SH (40) or C1 (19a) tags loaded with either Tb$^{3+}$, Tm$^{3+}$ or Y$^{3+}$ ions [99]. The resulting structure corrected the NMR structure determined previously from NOEs and scalar couplings [217]. Notably, the structure calculations converged well even though the PCS data were relatively sparse, with PCSs from more than a single tagging site observed for less than half the amino acid residues.

In contrast, it proved difficult to determine the fold of the 7-transmembrane-helix protein pSRII exclusively from PCS restraints derived from C2 (19b) lanthanide tags attached
to four different positions of the protein, even though four different paramagnetic lanthanides were used (Dy\textsuperscript{3+}, Tb\textsuperscript{3+}, Tm\textsuperscript{3+} or Yb\textsuperscript{3+}) \cite{218}. A total of 737 PCSs were measured for backbone amides and tryptophan side-chains, with at least one PCS assigned for two thirds of the residues. Assuming literature values for the $\Delta\chi$ tensors and imposing restraints for 132 backbone hydrogen bonds in the structure calculations, the backbone RMSD to the previously published NMR structure was 5 Å. It is unclear, how much the structure could have been improved by refining the $\Delta\chi$-tensor parameters during the structure computations. Ultimately, the RMSD to the target structure was reduced to 2.6 Å by inclusion of over 200 NOEs, including a number of inter-helix NOEs, which by themselves were insufficient to determine the global fold of this protein.

Determining the 3D structure of another $\alpha$-helical protein, cytochrome $c'$ from \textit{Rhodobacter capsulatus}, also proved to be difficult from paramagnetic data only. Although the PCSs were complemented by paramagnetically induced RDCs, PREs and cross-correlated relaxation effects, the authors felt it necessary to define the helices by H-bond restraints \cite{91}. Notably, however, the protein contained only a single paramagnetic centre (Fe\textsuperscript{2+}), which was associated with a relatively small $\Delta\chi$ tensor.

More recently, the GPS-Rosetta approach was used to determine the structure and location of the NS2B co-factor in the 27 kDa NS2B/NS3 protease of serotype 2 dengue virus, using PCSs measured with C1 (19a) and C2 (19b) tags loaded with either Tb\textsuperscript{3+}, Tm\textsuperscript{3+} or Y\textsuperscript{3+} ions at two different sites of NS3 \cite{219}. While this example does not constitute a full structure determination, as the structure of NS3 was assumed to be the same as in previous crystal structures, the work demonstrated that PCSs elicited from two tagging sites can be sufficient to obtain correct folds of protein segments.

Recently, the structure of GB1 was determined with the help of backbone amide PCSs and $\textsuperscript{1}H-\textsuperscript{15}N$ RDCs by 2D in-cell NMR in frog oocytes \cite{220}. GB1 was tagged at three different sites with the DOTA-M7Py tag loaded with Tm\textsuperscript{3+} or Lu\textsuperscript{3+} and GPS-Rosetta \cite{99} was used for structure calculation. A different study used the related PyMTA tag loaded with Tb\textsuperscript{3+}, Tm\textsuperscript{3+} or Yb\textsuperscript{3+} attached at two different sites of GB1 to determine its structure in frog oocytes, using GPS-Rosetta from PCSs of backbone amide protons only \cite{221}. The Rosetta algorithm performs very well in computing the structures of small proteins such as GB1 without any protein-specific experimental data \cite{213}, so that these structure determinations can equally well be considered as structure refinements.
7.3. Structure determinations of protein-protein complexes using PCSs from lanthanides

Intermolecular PCSs across a protein-protein interface deliver excellent restraints to define the 3D structure of the protein-protein complex, particularly in situations where the NMR resonances of interfacial residues are broadened by chemical exchange, or their chemical shifts change so much in the complex compared with the free proteins that new resonance assignments need to be established. The concept of this approach was established with a cytochrome f – plastocyanin complex, where intermolecular PCSs generated by the heme Fe$^{3+}$ ion in cytochrome f allowed determination of the complex structure by rigid-body docking [222]. Subsequent work showed that for the corresponding complex from Prochlorothrix hollandica a significantly improved fit of the data could be obtained by assuming an ensemble of structures, as they may occur in an encounter complex [223].

This approach is greatly enhanced by lanthanide ions, due to larger PCSs and the available choice of different lanthanides, including very good diamagnetic references. In the case of the complex between the E. coli DNA polymerase III subunits ε$_{186}$ and θ, lanthanide ions in the metal binding site of ε$_{186}$ induce significant PCSs in θ allowed determination of the ε$_{186}$:θ rigid-body docking [109]. The study showed that ambiguities in the docking arrangement arising from the symmetry of the Δχ tensor of a single metal ion are lifted by the availability of PCSs from two different lanthanides (Dy$^{3+}$ and Er$^{3+}$ in the case of the ε$_{186}$:θ).

The approach was first extended to non-metalloproteins by attaching a double-arm LBP [124] to one of the proteins in a protein-protein complex. The target protein was the p62 PB1 domain. The domain produces a front-to-back homo-oligomer, which was reduced to a dimer by suitable mutations. Combined with chemical shift perturbations, PCSs measured with four different lanthanide ions determined the structure of the 20 kDa dimer [126].

In the same year (2010), a milestone study of the 65 kDa complex of adrenoxin reductase (AdR) with adrenoxin illustrated the potential of the CLaNP-5 tag (12) for determining the structure of protein-protein complexes without resonance assignments of the tagged protein [224]. PCSs were generated in adrenoxin by Tm-CLaNP-5 tags attached at two different sites of AdR. Combined with PREs from a Gd-CLaNP-5 tag, chemical shift perturbations, and optimisation of the orientation of the Δχ tensors in an iterative fashion, the final rigid-body docking solutions computed with XPLOR-NIH showed RMSD values of no more than 3.2 Å and were in agreement with the crystal structure of the complex. The study involved significant biochemical effort, as good labelling efficiencies were found for only two
out of four tag attachment sites and an extensive mutation study was needed to identify the cysteine residues in wild-type AdR that had to be mutated prior to tag attachment. Notably, PCSs were observed over distances of up to 56 Å. Therefore, the structure could be determined despite the paramagnetic iron-sulfur cluster in AdR, which prevented observation of NMR signals near the protein-protein interface.

To solve the ambiguity of docking solutions arising from the symmetry of Δχ tensors, it was shown that the location and orientation of a Δχ tensor is readily varied by changing the length of the peptide linker in the fusion with a double-arm LBP [225]. The strategy was demonstrated with the complex between FKBP12-rapamycin and the mTOR FRB domain. Five different linker lengths were tested to identify two constructs that yielded different PCSs of good magnitude without perturbing the protein structure.

PCSs from single-arm lanthanide tags are more difficult to interpret if the tag is flexible. If a homology model of the 3D structure of the protein-protein complex is available, however, a single tag attached at a single site with a single paramagnetic lanthanide can yield conclusive experimental verification of the complex. This was demonstrated for the complex between the dengue virus NS2B-NS3 protease and aprotinin (BPTI), where an effective Δχ tensor established with inclusion of PCSs from residues near the site of interest proved sufficiently accurate to demonstrate that NS2B assumes the closed conformation throughout, including segments for which the crystal structure did not show electron density [69]. This study extended earlier work, where the C1 (19a) and C2 (19b) tags had been used with different lanthanides at three different sites to show that the protease also assumes the closed conformation in complex with a low-molecular weight inhibitor and, without inhibitor, after cleavage of the artificial peptide linker between NS2B and NS3 [161, 226].

7.4. Lanthanide-generated PCSs for studies of dynamic proteins and protein-protein complexes

If a molecule moves relative to the Δχ tensor of a paramagnetic metal ion, this will change the PCSs observed (unless the nuclear spins move along a PCS isosurface, which is unlikely for larger polypeptide segments). Therefore, PCSs from paramagnetic lanthanide tags attached to a structurally conserved part of the protein offer a unique tool to assess inter-domain movements. In general, large-amplitude motions will reduce the magnitude of PCSs, as the spaces visited by the nuclear spins are likely characterized by PCSs of different sign.
7.4.1. PCSs of random coil peptides

The reduction of PCS magnitude due to mobility is particularly apparent along a random coil polypeptide chain. An example is a study of the 166 kDa complex between the E. coli DNA Pol III subunits α, ε, and θ. The ε:θ complex is structurally well defined, but it binds to α via a flexibly disordered polypeptide chain at the C-terminal end of ε. PCSs from a Er3+, Tb3+ or Dy3+ ion bound to the natural metal binding site in ε decrease to very minor effects with increasing distance from the globular domain of ε over about 15 residues of the flexible polypeptide segment [227]. Almost complete suppression of PCSs after about 15 residues of flexible polypeptide segment was also observed in the case of the long unstructured loop formed by the C-terminal domain of E. coli single-stranded DNA binding protein (SSB) [228].

A recent study attached the DOTA-M8 ytterbium tag to two different intrinsically disordered proteins, residues 454-526 of the protein “fused in sarcoma” and residues 1-101 of the lymphoid enhancer-binding factor 1. Attached to cysteine residues engineered into the polypeptide chains, PCSs were observed between 5 and 25 residues from the tag attachment site, greatly improving spectral resolution and enabling unique resonance assignments. Remarkably, the PREs were sufficiently small to allow observation of the backbone amide resonances of the tagged cysteine residues [229].

These results are in overall agreement with expectations for a model that represents the polypeptide chain as a Gaussian chain of statistical chain segments [230], where a statistical chain segment corresponds to the polypeptide segment for which the relative orientation of the first and last amino acid residue is uncorrelated. After at most two statistical chain segments, this model would predict that amino acid residues sample spaces with opposite signs of PCS values. The length of the statistical chain segment in random-coil peptides corresponds to about nine amino acid residues [231].

7.4.2. Inter-domain PCSs in multiple-domain proteins

Likewise, inter-domain motions decrease the magnitude of PCSs. An early example was the N60D mutant of the two-domain protein calmodulin [232]. While Tm3+ and Tb3+ ions bound to the N-terminal domain generated significant PCSs in the N-terminal domain, the PCSs and paramagnetically induced 1H-15N RDCs in the C-terminal domain were much smaller, and could be interpreted by an ensemble of three different relative domain orientations but not by a single one. The data subsequently formed the basis for maximum-
occurrence calculations that assess the maximum contribution of a conformation in the ensemble [233-236]. In an alternative approach, the data were used to probe the conformational space of calmodulin by molecular dynamics and replica-averaged metadynamics simulations [237].

The N60D mutant of calmodulin was used further to study inter-domain mobility in a complex with a peptide derived from the voltage-gated calcium channel Ca_{1.2} (IQ), for which three different inter-domain orientations had been observed in the crystal. PCSs and RDCs of backbone amide protons generated by four different lanthanide ions (with two additional lanthanides used for cross-validation) were measured. Beyond inclusion of all three crystal conformations, a best ensemble fit of the data required four additional conformations derived from MD simulations [238].

With an increasing number of protein coordinates deposited in the protein data bank (PDB), there are also an increasing number of crystal structures of proteins in different conformations. PCSs present highly informative data on whether the conformations in solution match those in the crystal environment, and whether conformational changes occur in solution. One example is the dengue virus NS2B/NS3 protease, where crystal structures show very different conformations for NS2B, whereas PCSs measured in solution support only the closed conformation [69, 161, 226]. Another example is the E. coli aspartate/glutamate binding protein, where PCSs in the presence of glutamate agree with the crystal structure, whereas PCSs in the absence of glutamate indicate a more open conformation with a flexible hinge between the two domains [239]. The approach has also been used to decide whether T4 lysozyme without bound substrate or inhibitor assumes an open or closed conformation in solution [240]. The study showed that, based on data comprising paramagnetically induced \(^1\)H-\(^1\)N RDCs and PCSs from Tb\(^{3+}\) and Tm\(^{3+}\), an improved fit could be obtained by assuming an equilibrium between two different protein conformations, whereas inclusion of a third conformation no longer improved the fit. In the case of the glucose-galactose binding protein, MD simulations were used to generate transitions between open and closed conformations to explain PCSs and \(^1\)H-\(^1\)N RDCs generated with a Dy\(^{3+}\) tag (10, Fig. 11) [241]. Again, the paramagnetic data could be explained by an equilibrium between two protein conformations.

Another recent study investigated the conformation of the cytochrome P450 CYP101A1 in the presence and absence of substrate (camphor) and the redox partner putidaredoxin [242]. Using the double-arm lanthanide tag CLaNP-7 (14) loaded with Yb\(^{3+}\) and attached at a single site, PCSs of backbone amides showed a better fit to a crystal structure in the closed conformation when substrate was present and to an open conformation
in the absence of substrate. In the complex with both substrate and putidaredoxin, the PCSs observed for a P450 sample selectively labelled with $^{15}$N-leucine were conserved, indicating the closed conformation in contrast to previous X-ray crystallographic and EPR results. Notably, the outstanding sensitivity of PCS measurements was critical to perform this study, as this 45 kDa enzyme was only stable for a few hours in the absence of substrate.

It is common to derive crystal structures of protein-ligand complexes from crystals of apo-protein that are soaked with ligand molecules after crystallisation. This raises the possibility that crystal packing forces prevent the conformational changes that ligand molecules may induce in solution. In many instances, however, protein-ligand complexes resist crystallisation. For example, crystal structures of open and closed states have been reported of MurD, which is a three-domain 47 kDa protein required for bacterial peptidoglycan (murain) biosynthesis, but the protein could not be crystallized together with ATP or stable analogues thereof. PCSs measured with Yb-CLaNP-5 showed that the binding of ATP-Mg$^{2+}$ generates a semi-closed state that transitions into the fully closed state after binding of the UDP-$N$-acetylmuramoyl-l-alanine substrate and ATP hydrolysis [243].

7.4.3. PCS studies of dynamic protein-protein complexes

In principle, the long-range nature of PCSs generated by lanthanide tags also opens unique opportunities to study weak and dynamic protein-protein complexes, as the tags can be positioned sufficiently far from the interface to avoid steric interferences. Due to their distance dependence, however, intermolecular PCSs can be quite small and the RDCs resulting from paramagnetic alignment of the molecule in the magnetic field may be more sensitive reporters of dynamic protein-protein interactions. For example, the 23 kDa complex between yeast cytochrome $c$ and bovine adrenodoxin is transient and structurally heterogeneous, as indicated by unexpectedly small RDCs observed in adrenodoxin, when a Yb-CLaNP-5 tag was attached to cytochrome $c$ [244]. In this example, the tag was too far from the adrenodoxin molecule to provide intermolecular PCSs of sufficient magnitude to be interpreted in terms of a structural ensemble.

In the case of the cytochrome P450cam-putidaredoxin complex, CLaNP-7 (14) loaded with Yb$^{3+}$ or Tm$^{3+}$ on two sites of P450cam and one site of putidaredoxin produced PCSs and RDCs that resulted in a structural model of the complex. In this case, evidence for a heterogeneous encounter state came primarily from PREs measured with Gd-CLaNP-7, which were larger than expected [245].
An interesting example of a dynamic protein-protein complex has recently been provided by the synaptotagmin-1 C2B domain bound to the SNARE complex (total molecular weight 51 kDa) [246]. Using the C2-Dy$^{3+}$ tag attached at two different sites of the SNARE complex yielded sizeable PCSs in the SNARE complex, but the PCSs observed for the C2B domain were much smaller than expected, which was explained by a dynamic binding mode between the two proteins, arising from predominant interactions through charged rather than hydrophobic amino acid side chains. In this system only two out of ten different tagging sites tested delivered suitable PCSs.

7.4.4. Relaxation dispersion and CEST experiments on protein signals shifted by PCSs

A more difficult challenge is the use of paramagnetic metal ions to assist the analysis of conformational changes by relaxation dispersion experiments. Relaxation dispersion experiments are uniquely suited to revealing the existence of small populations of conformations with lifetimes on the micro- to millisecond time scale. It has been shown that paramagnetic lanthanide ions in the Ca$^{2+}$ binding site of the N-terminal domain of troponin C generate relaxation dispersion curves unobservable with Ca$^{2+}$ or La$^{3+}$ [247]. This effect was attributed primarily to motions in the lanthanide-binding site.

Similarly, substitution of the diamagnetic Zn$^{2+}$ ion in the N-terminal domain of the two-domain protein PA0128 by a paramagnetic Co$^{2+}$ ion produced relaxation dispersion curves for the C-terminal domain that were not observable in diamagnetic samples [198]. In this case, the effect was attributed to translational movements of the C-terminal relative to the N-terminal domain.

Unfortunately, attempts to enhance relaxation dispersion effects by paramagnetic lanthanide tags have so far been thwarted by difficulties distinguishing motions of the protein from those of the tag [151, 152, 198]. Alternatively, however, chemical exchange saturation transfer (CEST) experiments can be used to measure chemical shifts and PCSs of low-populated states. This has recently been demonstrated for the Abp1p SH3 domain tagged with 4MMPyMTA (33). In the presence of 3% Ark1p peptide, $^{15}$N PCSs of five residues measured with Tb$^{3+}$ were shown to agree between the excited state of apo-Abp1p SH3 domain and its complex with peptide [175]. In the same work, a mutant of the HYPA/FPB11 FF domain was ligated with the same Tb$^{3+}$ tag. This domain is in exchange with a small population of unfolded protein, which was confirmed by the small magnitude of the PCSs observed for seven backbone amides in $^{15}$N CEST experiments.
7.4.5. PCSs for 3D structure determination of short-lived enzyme intermediates

Two-dimensional HSQC spectra can be measured very quickly, allowing correspondingly rapid collection of structural restraints from PCSs. This has recently been exploited to determine the conformation of a short-lived enzyme intermediate. A cysteine mutant of *S. aureus* sortase A was used to attach the tags 38 or 35 and measure PCSs of backbone amides by \(^{15}\)N-HSQC spectra of samples right after addition of substrate peptide. Different PCSs were observed for a number of loop segments in the resulting transient thioester intermediate to those in the free enzyme. The PCSs generated by Dy\(^{3+}\), Tb\(^{3+}\) and Tm\(^{3+}\) were used to calculate the structure of the enzyme in the intermediate, assuming that the structure of segments with conserved PCSs did not change from that of the free enzyme [177].

7.5. Protein-small molecule interactions

7.5.1. Studies with lanthanide tags on the protein

There is much scope for using PCSs to study the binding site, orientation and structure of ligand molecules binding to proteins, in particular as paramagnetic effects can be elicited by tags that are quite remote from the ligand binding site. PCSs generated by lanthanide ions are particularly suitable, as the paramagnetic shifts are almost exclusively due to pseudocontact shifts, although it has been shown that contact shifts can be taken into account for paramagnetic effects that are generated by transition metal ions such as Fe\(^{2+}\), Co\(^{2+}\) or Ni\(^{2+}\) located in the vicinity of the ligand [248].

In general, proteins have been tagged with lanthanides at one or several sites. Some studies also explored the alternative approach of attaching lanthanide tags to ligands (see also Section 5.3.1).

The first published example where PCSs from lanthanides were used to define the exact binding mode of a ligand was a study of the affinity and binding mode of thymidine in the active site of the *E. coli* DNA polymerase III subunit ε\(_{186}\). This protein is a proof-reading exonuclease that forms a tight complex with the subunit θ [249]. The metal ions in the active site were replaced by Tb\(^{3+}\), Dy\(^{3+}\) or Er\(^{3+}\). PCSs were measured in one-dimensional NMR spectra of the thymidine ligand. With a dissociation constant of about 7 mM, the ligand binds only weakly and is in fast exchange between the bound and free states; the NMR signals of the ligand are therefore averaged between the two states, reducing the magnitude of the PCSs in proportion to the fraction bound. Even with a 550-fold excess of ligand, PCSs were still measurable because the distance between lanthanide and ligand binding site was short. Straightforward 1D \(^1\)H- and \(^{13}\)C-NMR spectra were sufficient to measure the PCSs induced by
Tb$^{3+}$, Dy$^{3+}$ and Er$^{3+}$. Combined with the $\Delta$ tensors determined from the $^{15}$N-HSQC spectrum of the protein, the PCSs determined the binding affinity and orientation of the thymidine ligand with respect to the $\varepsilon_{186}$ subunit, which proved to be closely related to the binding mode observed for thymidine monophosphate by X-ray crystallography.

Another early study analysed the weak binding of lactose to galactin-3 using paramagnetic restraints from an LBP fused to the protein [250]. The measurements used a 5:1 ratio of ligand to protein, which was found to be the optimal compromise between signal-to-noise ratio and the size of PCSs and RDCs in the ligand, measured in [$^{13}$C-$^1$H]-HSQC spectra with Dy$^{3+}$ as the paramagnetic ion. These data alone produced a structure having an RMSD of 4.3 Å for the ligand atoms relative to the crystal structure, which decreased to 1.9 Å with the inclusion of a single intermolecular NOE in the calculation.

Using a LBP fused to the N-terminus of the growth factor receptor-bound protein 2 (Grb2) SH2 domain and anchored to the protein at a second point via a disulfide bond, the binding modes of two ligands of different affinity were determined by PCSs from four different paramagnetic lanthanide ions [125]. Deuterated protein was used to observe the ligand signals in 1D $^1$H-NMR experiments. The ligand conformers and positions determined from the PCS data displayed RMSD values between 1.9 and 3 Å, indicating that PCS data from a single lanthanide site can leave substantial structural uncertainties in flexible ligand molecules. It was noted that loading the LBP tag on the protein with Gd$^{3+}$ delivered a sensitive way of screening a library of ligands for binding by using PREs.

If the binding mode of a ligand has been determined by intermolecular NOEs, PCSs from a single tagging site provide valuable restraints for cross-validation. In this way, the binding mode of $^{13}$C/$^{15}$N labelled dGMP to the R3H domain of human S$\mu$bp-2, as well as the protein conformation itself, were confirmed by PCSs using the C1 tag (19a) loaded with Tb$^{3+}$ or Yb$^{3+}$ [251].

The value of PCSs generated from tags positioned at three different sites of the target protein was explored with the complex of human FKB12, tagged with Yb$^{3+}$-CLaNp-5 (12), with a weakly binding small molecule [67]. A 1.3-fold excess of ligand was sufficient to allow selective detection of the ligand signals in 1D $^1$H-NMR spectra, with the help of a $T_2$ relaxation filter to suppress the protein signals. At this ligand excess, only 2% of the ligand molecules were in the bound state and the PCSs observed in the ligand were less than 10 Hz. An RMSD of 2.8 Å was obtained between ligand coordinates determined from PCSs and ligand coordinates determined from intermolecular NOEs, but it was noted that the NOE structure matched the PCS data less well than the PCS-based docking model. It was noted that
PCSs from more than three tagging sites may be required for unambiguous identification of a ligand binding site, unless additional information from sources other than PCSs is available. (A single PCS restricts the position of a nuclear spin to a PCS isosurface. A second PCS from a different tagging site locates the spin on the line formed by the intersection between two PCS isosurfaces. With the PCS isosurface from a third tagging site, this line intersects with the third isosurface at only two points. Usually, only one of these two points is compatible with independent chemical information such as van der Waals contacts. Otherwise, the ambiguity can be resolved by the PCS from a fourth tagging site.)

NMR studies of protein-ligand complexes are greatly facilitated if the ligand is in fast exchange between the bound and free state, which facilitates the observation of the ligand resonances, as the ligand can be added in excess and the properties of the bound ligand derived from the average NMR spectrum. Observing the NMR spectrum of a non-exchanging ligand is much harder, as the bound-state ligand signals must be identified in a 1:1 complex with the protein. This problem has recently been addressed by using a ligand containing a tert-butyl group, which produces an exceptionally narrow and intense signal for which NOEs can readily be observed. This approach has been demonstrated with the dengue virus NS2B/NS3 protease in complex with a tert-butyl-group-containing inhibitor that forms a covalent bond to the active-site serine residue [252]. From cross-peaks observed in 2D NOESY spectra, PCSs could readily be measured not only for the tert-butyl group, but also for its NOE partners, for protease samples labelled at three different sites with C2 tags (19b) loaded with Tb\(^{3+}\) or Tm\(^{3+}\). Using the \(\Delta\chi\) tensors determined from PCSs of backbone amides of the protein, the PCSs measured for the bound ligand defined localisation spaces on the protein surface, which indicated where the tert-butyl group and each of its NOE partners are located. Finally, modelling software was used to determine structural details of those parts of the ligand for which no PCSs could be measured.

7.5.2. Studies with lanthanide or cobalt tag on the ligand

Three different examples of ligand-protein studies using lanthanide-tagged ligands instead of tagged proteins have recently been reported. The interactions studied were of lactose with galectin-3 [82], fucose with a viral coat protein [131], and sevoflurane with calmodulin [132]. All three examples, described in more detail in Section 5.3.1, explored weak intermolecular interactions, where residual tag flexibility compromises the value of PCSs for gaining detailed structural information about specific intermolecular interactions. Furthermore, it is difficult to attach lanthanides at more than a single site of a small ligand,
leaving ambiguities in PCS interpretation even if ligand and tag are perfectly immobilized on the target protein.

An interesting hybrid strategy is to generate PCSs in a ligand by attaching a metal tag to another ligand that binds tightly to the target protein, resulting in a secondary site screening approach. This was demonstrated with the N-terminal coiled coil of HIV-1 gp41 as the target, a 39-residue α-helical peptide labelled with an EDTA-Co²⁺ complex at an N-terminal cysteine residue as the tag, and 3-p-fluorobenzylbenzoic acid as the ligand binding to the target with low affinity [253]. Although PCSs were observable for only six ligand protons, and their values were small (< 10 Hz), Δχ-tensor fits allowed discrimination between different ligand poses.

8. Conclusion and prospects

With the coordinates of tens of thousands of proteins deposited in the protein data bank, the groundwork has been laid for many more investigations of protein conformational change, which ultimately is at the heart of the function of most proteins, ranging from small local changes in enzyme catalysis and ligand binding to large-amplitude conformational changes in signalling and motor proteins. By choosing the attachment sites of paramagnetic tags, it is possible to study such protein properties site-selectively without having to solve again the 3D structure of the entire protein, as required in X-ray crystallography or cryo-electron microscopy. In particular, owing to the long-range nature of paramagnetic effects, lanthanide tags lend themselves to site-specific studies where the tag must be sufficiently far from the site of interest not to interfere. To support site-specific NMR studies, it will be useful to develop improved methods for labelling the site of interest with NMR isotopes, e.g. by segmental isotopic labelling [254] or residue-specific labelling [255, 256].

In view of the general importance of NMR spectroscopy in drug development, the availability of protein crystal structures also provides fertile ground for further developments of lanthanide-tagging techniques with the aim of fragment-based drug design.

In closing, we note an additional application of paramagnetic lanthanide tags that is emerging in EPR spectroscopy, where distances between two gadolinium ions can be measured over ranges of 20 to 80 Å in frozen solutions [257]. The high sensitivity of EPR spectroscopy may allow such experiments in cells at physiological concentrations. For these applications, it is important that the Gd³⁺ ion does not leak from the tag and that the tag is
rigidly attached to the protein in order to generate narrow distance distributions. Further tag development thus has an importance that goes beyond its applications in NMR spectroscopy.

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**Glossary of abbreviations**

3MDPA: 3-mercaptodipicolinic acid

4MDPA: 4-mercaptodipicolinic acid

4MMMDPA: 4-mercaptomethylidipicolinic acid

4MMPyMTA: 2,2',2'',2''-(((4-(mercaptomethyl)pyridine-2,6-diyl)bis(methylene))bis(azanetriyl)tetraacetic acid

4MTDA: 4-mercapto-2,2':6',2''-terpyridine-6,6''-dicarboxylic acid

4PS-DPA: 4-(phenylsulfonfyl)dipicolinic acid

4PS-PyMTA: 4-phenylsulfonfyl-(pyridin-2,6-diyl)bismethylenenitrilo tetrakis(acetic acid)

4VPyMTA: 4-vinyl(pyridine-2,6-diyl)bismethylenenitrilotetakisacetic acid

ArgN: *E. coli* arginine repressor

BpyAla: (2,2'-bipyridin-5-yl)-L-alanine

BTTAA: 2-(4-(bis((1-tert-butyl)-1H-1,2,3-triazol-4-y1)methyl)amino)methyl)-1H-1,2,3-triazol-1-yl)acetic acid

CEST: chemical exchange saturation transfer

CLaNP: caged lanthanide NMR probe

CSA: chemical shift anisotropy

DFT: density functional theory

DOTA: 1,4,7,10-tetraazacyclododecane-1,4,7,10-tetraacetic acid

DPA: dipicolinic acid

DTPA: diethylenetriaminepentaacetic acid

DTNB: 5,5'-dithiobis-2-nitrobenzoic acid

EDTA: ethylenediaminetetraacetic acid

HQ-Ala: 2-amino-3-(8-hydroxyquinolin-3-yl)propanoic acid

HSQC: heteronuclear single quantum coherence
**IDA:** iminodiacetic acid

**LBP:** lanthanide binding peptide

**MTSL:** \(S-(1\text{-}oxyl\text{-}2,2,5,5\text{-}tetramethyl\text{-}2,5\text{-}dihydro\text{-}1H\text{-}pyrrol\text{-}3\text{-}yl})\text{methyl methanesulfonothioate}

**NOE:** nuclear Overhauser effect

**NTA:** nitrilotriacetic acid

**PCS:** pseudocontact shift

**PRE:** paramagnetic relaxation enhancement

**RACS:** residual anisotropic chemical shift

**RDC:** residual dipolar coupling

**RMSD:** root mean square deviation

**SAP:** square antiprism

**TAHA:** triaminohexaacetate

**TOCSY:** total correlated spectroscopy

**TSAP:** twisted square antiprism

**UTR:** unique tensor representation