

Sensitivity of abyssal water masses to overflow parameterizations

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Abstract

Antarctic Bottom Water (AABW) and North Atlantic Deep Water (NADW) control the abyssal limb of the global overturning circulation and play a major role in oceanic heat uptake and carbon storage. However, current general circulation models are unable to resolve the observed AABW and NADW formation and transport processes. One key process, that of overflows, motivates the application of overflow parameterizations. A sensitivity study of both AABW and NADW properties to three current parameterizations is presented using an ocean-sea ice model within a realistic-topography sector of the Atlantic Ocean.

Overflow parameterizations that affect only tracer equations are compared to a fully dynamical Lagrangian point particle method. An overflow parameterization involving partial convective mixing of tracers is most efficient at transporting dense NADW water downslope. Such a parameterization leads to a maximum mean increase in density in the north of 0.027 kg m^{-3} and a decrease in age of 525 years (53%). The relative change in density and age in the south is less than 30% of that in the north for all overflow parameterizations. The reduced response in the south may result from the differing overflow characteristics of AABW compared to NADW. Alternative approaches may be necessary to improve AABW representation in global climate models.

Keywords: AABW, NADW, global climate models, sector model, overflow schemes

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1. Introduction

Antarctic Bottom Water (AABW) and North Atlantic Deep Water (NADW) form important components of the global Meridional Overturning Circulation (MOC), large scale ocean stratification and distribution of oceanic heat, carbon and nutrients (Talley et al., 2003; Hughes and Griffiths, 2006; Johnson, 2008; Kuhlbrodt et al., 2007; Purkey and Johnson, 2010; Ríos et al., 2012). Properties of the deep and bottom waters throughout the global ocean are defined initially by the formation of dense shelf waters or, in part, through open ocean convection processes such as in the Labrador Sea (Zhang et al., 2011). Here we focus on the subsequent overflow processes of the shelf waters whereby the dense water flow from the continental shelf and descends down the continental slope. In the case of NADW, shelf waters are transported through the Faroe Bank Channel and Denmark Strait. Conversely, AABW flows off the Antarctic continental shelf from numerous source regions dispersed across the shelf (Baines and Condie, 1998). Due to limitations on computational resources, present generation General Circulation Models (GCMs) are unable to attain the high horizontal and vertical resolutions required to resolve overflow processes (Legg et al., 2009), thereby compromising characteristics of the resulting water masses.

Recently, several studies have indicated that abyssal water masses are key players in global climate change. For example, the recently observed contraction of AABW (Purkey and Johnson, 2012; Katsumata and Masuda, 2013), warming and freshening within the AABW and NADW density ranges (Hall et al., 1997; Levitus et al., 2005; Steinfeldt et al., 2007; Purkey and Johnson, 2010; Frajka-Williams et al., 2011; Purkey and Johnson, 2012; Couldrey et al., 2013; Sloyan et al., 2013; Zenk and Visbeck, 2013) and increase in total carbon and decrease in oxygen (Garcia et al., 1998; Sloyan et al., 2013) influences the global ocean circulation and property budgets. These results motivate us to improve simulations of AABW and NADW formation processes, in particular, overflows.

Representation of overflows in z -coordinate models (the most common vertical coordinate used in GCMs) is particularly difficult due to step-like topography (Beckmann and Döscher, 1997; Roberts and Wood, 1997; Winton et al., 1998; Ezer and Mellor, 2004; Legg et al., 2006).

29 Water that flows down a slope undergoes vertical convective mixing at each of these steps
30 (refer to Figure 1a). This convection overly mixes and dilutes the overflowing waters before
31 it reaches the bottom leading to deep water that is too warm and fresh (Winton et al., 1998;
32 Downes et al., 2011) and bottom water that is overly warm and salty (Downes et al., 2011).
33 Hence, overflow parameterizations have been developed to move the dense shelf water into
34 the deep ocean, aiming to increase the density and decrease the age of AABW and NADW
35 waters as well as increase the magnitude of the AABW and NADW overturning cells. The
36 performance of these parameterizations in current GCMs, however, poorly represents the
37 overflows and deep water properties, particularly in the Southern Ocean (Condie, 1995;
38 Griffies et al., 2000; Legg et al., 2009; Downes et al., 2011; Weijer et al., 2012; Heuzé et al.,
39 2013). Further, the limited testing of overflow parameterizations in the Southern Ocean
40 and within models with realistic bathymetry, motivates the need to develop an increased
41 understanding of overflow parameterizations. This paper tests the sensitivity of AABW and
42 NADW properties and transport to three distinct overflow parameterizations, along with
43 variations to their controlling parameters.

44 The overflow parameterizations tested here include the downslope transport scheme of
45 Campin and Goosse (1999) (hereafter CG1999), the sigma bottom boundary layer scheme
46 of Beckmann and Döscher (1997) and Döscher and Beckmann (2000) (hereafter SIGMA),
47 and the embedded Lagrangian point-particle method of Bates et al. (2012a) and Bates et al.
48 (2012b) (hereafter BLOBS). Note that we do not consider the overflow parameterization
49 for the Parallel Ocean Program (POP) (Danabasoglu et al., 2010) as it was designed for
50 NADW overflows where the flow is constrained by well defined sills or straights. Through
51 that method, AABW source regions are confined to single regions in the Weddell and Ross
52 Seas. We consider this approach unsuitable for the dispersed nature of AABW sources
53 (e.g. van Sebille et al., 2013; Baines and Condie, 1998) and biases were indeed found in the
54 representation of AABW using this method (Weijer et al., 2012); however, reasons for these
55 biases were not provided.

56 We perform the sensitivity analysis within a realistic bathymetry sector of the Atlantic
57 ocean that incorporates both the NADW source regions and the Weddell Sea, which is an

58 important source region for AABW (Deacon, 1937; Orsi et al., 1999; Naveira Garabato et al.,
59 2002). Previous sector models of the Atlantic (e.g., Ezer and Mellor, 1994) do not include the
60 South Atlantic. While the sector model described here is not a fully realistic representation
61 of the Atlantic, it is computationally fast, allowing multiple simulations to be run whilst
62 providing the major circulation processes commonly present in GCMs.

63 Our sensitivity analysis examines how the overflow schemes control AABW and NADW
64 properties in GCMs and indicates the suitability of each parameterization to the respective
65 overflow regions. An outline of the overflow parameterizations being tested and their defining
66 characteristics is given in Section 2 with a review of the previous studies evaluating them.
67 Section 3 provides the method for the set-up of the novel sector model incorporating the
68 key processes of GCMs, followed by the defining parameter space to be tested for each
69 scheme. Results assessing the overall performance of the sector model, a comparison of the
70 response of AABW and NADW to each overflow scheme and the sensitivity of each scheme
71 to parameter variations is given in Section 4. Final concluding remarks are provided in
72 Section 5.

73 **2. Parameterizations**

74 *2.1. Campin and Goosse (1999) (CG1999)*

75 The CG1999 scheme is designed to move dense water downslope with minimal mixing
76 by directly transferring tracer properties between cells. The scheme is activated when a grid
77 cell at the bottom of a water column is adjacent to a less dense cell in a deeper water column.
78 The tracer properties of the first cell are then transported downslope to the bottom of the
79 adjacent water column or its neutrally buoyant level. A return flow is applied to conserve
80 mass in a rigid lid case (refer to figure 1 of Campin and Goosse (1999)).

81 The downslope flux of properties is dependent on the topographic slope, S , and the
82 density difference, $\Delta\rho$, between the shallow ocean cell and the horizontally adjacent less
83 dense cell giving the volume flux on the slope, F , defined as

$$F = \frac{g\gamma}{\rho_0} \Delta\rho\Delta A, \quad (1)$$

84 where g is the gravitational acceleration, ρ_0 is a reference density taken here to be 1035 kg
 85 m^{-3} , ΔA is the cell area through which the transport is being considered and $\gamma = \frac{\delta S}{\mu}$ where
 86 δ is the fraction of the grid cell participating in the overflow and μ is the dissipation rate due
 87 to friction (Griffies, 2012). Transport may only occur between horizontally adjacent water
 88 columns.

An alternative method where no return flow is provided (Figure 1b) may be applied where the change in tracer of the deep ocean cell is defined by the downslope flux and the difference in concentration of the tracer of the shallow cell and the deep cell (Griffies, 2012) such that

$$\partial_t(V\rho C)_{kdw}^{do} = \rho F(C_{kup}^{so} - C_{kdw}^{do}), \quad (2)$$

89 where C is the concentration of the tracer in the shallow ocean (so) and deep ocean (do),
 90 $V = \Delta z\Delta y\Delta x$ is the volume of the dense water cell, kup indicates the vertical level of the
 91 shallow ocean cell and kdw the vertical level of the deep ocean cell (Figure 1a). Such a
 92 downward flux acts without the convective mixing (represented in Figure 1a) that occurs
 93 over the topographic steps. This variant of CG1999 is only possible for models with a free
 94 surface, in which there is no constant volume restriction on water columns (Bates et al.,
 95 2012a), allowing the model to adjust accordingly to the change in density and thickness of
 96 the water column (indicated in Figure 1b).

97 We choose the no-return flow method as the default scheme of CG1999 since this case
 98 allows for an increased exchange of dense water down the slope when analysed in an idealised
 99 slope configuration with no surface forcing (Bates et al., 2012b). However, it is advantageous
 100 to further test the return flow case as Campin and Goosse (1999) and Goosse et al. (2001)
 101 both indicate an increased downward flow of dense water for the case when a return flow is
 102 implemented.

103 CG1999 is recognised to have some limitations, specifically, it only identifies water
 104 columns in directly adjacent cells from the shallow water column in its search for favourable

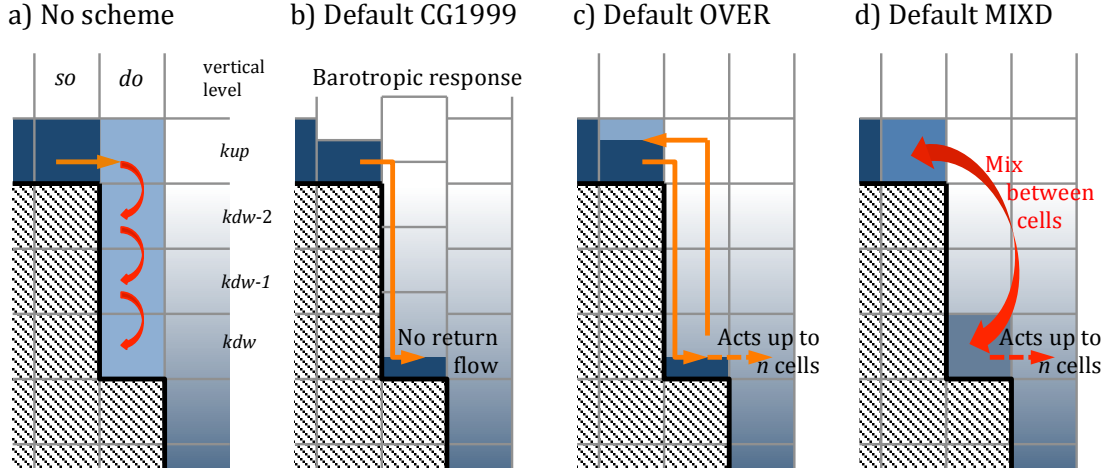


Figure 1: (a) A representation of the convection of dense water as it flows over the topographic step, (b) a representation of the no-return flow case of CG1999 where the volume flux leads to a change in water column thickness, (c) a representation of the overexchange (OVER), exchanging properties between the shallow and deep ocean grid cells and acting up to n cells and (d) a representation of mixdownslope (MIXD) where the shallow and deep cells mix towards their mean through a partial convective mixing scheme. Symbols so and do indicate the shallow and deep ocean columns respectively with the notation of the vertical levels provided in (a). The shade of blue within a cell indicates the density of water (darker = more dense).

105 downslope flow. Dense water travelling across regions of equal depth are therefore not af-
 106 fected by the scheme. Griffies (2012) recognised that such a restricted search could limit the
 107 downslope flow. Hence, the schemes of overexchange and mixdownslope (hereafter referred
 108 to as OVER and MIXD respectively) were developed to allow multiple grid cells away from
 109 the shallow dense column to be searched for favourable downslope flow.

110 2.1.1. Overexchange (OVER)

OVER is similar to the return flow case of CG1999 except that it allows for the exchange of tracer properties of the dense shallow water cell with the neutrally buoyant or bottom deep ocean cell without the exchange of properties of the intermediate cells (Figure 1c). Such an exchange is given by Equation (2) and (Griffies, 2012):

$$\partial_t(V\rho C)_{kup}^{so} = \rho F(C_{kdw}^{do} - C_{kup}^{so}), \quad (3)$$

111 The exchange of tracer properties may then occur in up to n adjacent cells (CG1999 is
 112 equivalent to $n = 1$) with the shallow cell properties being transferred along each of the
 113 n bottom cells. It is also possible to apply a weighting to the farthest cells to allow for
 114 an enhanced downslope flow. No rigorous assessment of this scheme has been previously
 115 undertaken and our results will indicate the importance of allowing for more grid cells to be
 116 included in the parameterizations when searching for favourable downslope conditions.

117 2.1.2. *Mixdownslope (MIXD)*

MIXD is similar to OVER as it allows for n grid cells to be applied in the search for
 downslope flows, however, in this case tracers are transferred through partial convective
 mixing whereby the dense shallow ocean cell partially mixes with the deep ocean cell (Griffies,
 2012) (Figure 1d). MIXD does not apply a complete mixing (mixed concentration is C_{mix})
 between the shallow cell concentration $C(s)$ and deep cell concentration $C(d)$, rather it
 applies a time tendency that mixes the concentrations towards the average (Griffies, 2012):

$$\text{tendency}(s) = \frac{M(s)\delta}{\Delta t} \left(\frac{C_{mix} - C(s)}{A} \right), \quad (4)$$

$$\text{tendency}(d) = \frac{M(d)\delta_d}{\Delta t} \left(\frac{C_{mix} - C(d)}{A} \right), \quad (5)$$

118 where the shallow and deep cell mass are $M(s)$ and $M(d)$ respectively, A is the horizontal
 119 area of the cells, δ is the fraction of the shallow ocean cell participating in the downslope
 120 transport (and a key defining parameter to vary within the scheme) and δ_d is determined
 121 as a function of S and $\Delta\rho$. As with OVER, MIXD also allows for weighting of the farthest
 122 n cells. Although not rigorously tested in the literature, this scheme is used in the GFDL
 123 ESM2M earth system model documented by Dunne et al. (2012) as well as the Australian
 124 Community Climate and Earth System Simulator (ACCESS) (Bi et al., 2013; Marsland
 125 et al., 2013). Additionally, impacts from MIXD were seen to be non-trivial in the North
 126 Atlantic in an analysis by Palter et al. (2014) of the buoyancy budget in GFDL ESM2M
 127 under control and idealised climate change situations.

128 *2.2. Sigma Boundary Layer (SIGMA)*

129 The parameterization of Beckmann and Döscher (1997) and Döscher and Beckmann
 130 (2000) applies a sigma coordinate layer in the bottom cells of a z -coordinate model. The
 131 sigma layer is not affected by the convective mixing of the stepped topography and allows
 132 for diffusion and advection to occur in this layer in addition to the diffusion and advection
 133 within the z -coordinate (Figure 2).

The diffusive flux between two adjacent cells of the SIGMA scheme is given by Beckmann and Döscher (1997)

$$F_\sigma = -A\nabla_\sigma T, \quad (6)$$

where

$$A = \begin{cases} A_{max} & \text{if } \nabla_\sigma \rho \cdot \nabla H < 0 \\ A_{min} & \text{if } \nabla_\sigma \rho \cdot \nabla H \geq 0, \end{cases} \quad (7)$$

134 ∇_σ is the horizontal gradient operator between sigma layer cells, A is the diffusivity and
 135 is maximum (A_{max}) for cases when downslope flow is favourable and minimum otherwise
 136 (A_{min}), H is the bottom depth, and T the tracer being considered.

The advective term is not assessed in this analysis as Döscher and Beckmann (2000) found it to have little impact in 1.5° horizontal resolution models. Instead, the advection term is partly accounted for via velocity dependent diffusion A_u (Griffies, 2012):

$$A_u = \begin{cases} |u|\delta x & \text{if } \nabla \rho \cdot \nabla H < 0 \text{ and } u \cdot \nabla H > 0 \\ A_{min} & \text{otherwise,} \end{cases} \quad (8)$$

137 where $|u|$ is the resolved sigma layer zonal velocity (we have only shown the zonal component
 138 for simplicity).

139 SIGMA has previously been found to produce an improved spreading of dense waters
 140 down an idealised linear slope (Beckmann and Döscher, 1997) and increased transport of
 141 dense water within a realistic bathymetry model of the North Atlantic at 1.5° horizontal
 142 resolution (Döscher and Beckmann, 2000). Bates et al. (2012b) similarly reports that the

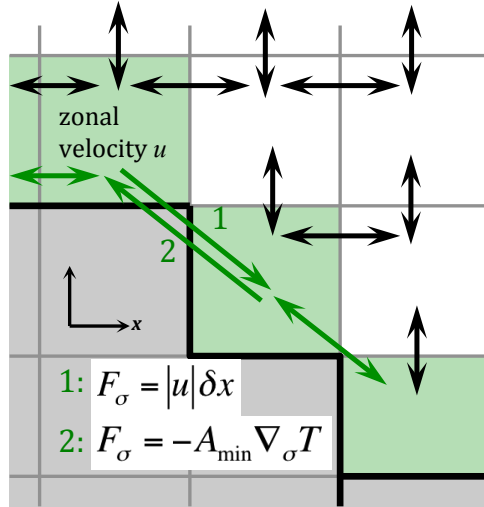


Figure 2: A representation of the velocity dependant SIGMA scheme (Equation 8) based on Griffies (2012) where the bottom sigma layer is represented by the green boxes and diffusion occurs between these grid cells (green arrows) in addition to the diffusion of the z -coordinate (black arrows).

143 SIGMA scheme is able to improve both the depth of penetration and slope velocities of a
 144 down flowing plume but the lack of rotational effects can also lead to a weakening of the
 145 circulation. No previous studies have tested the schemes performance in a Southern Ocean
 146 configuration.

147 2.3. Lagrangian point particles (BLOBS)

148 We test the new BLOBS parameterization developed by Bates et al. (2012a) (Figure
 149 3). This scheme implements a system of Lagrangian point particles that interact with the
 150 Eulerian model, exchanging mass and momentum. The Lagrangian point particles may be
 151 defined as either passive or dynamic. Passive particles are created by taking a portion of the
 152 properties of the Eulerian model, transporting it downslope and returning the properties to
 153 the Eulerian model without further interaction. This case is not considered in our sensitivity
 154 analysis, as Bates et al. (2012a) found that the difference between the passive overflow scheme
 155 and the original Campin and Goosse (1999) scheme is of the order of machine error. Further,
 156 free Lagrangian particles (that is particles that move freely through the open ocean away
 157 from bottom boundaries) will not be included due to their non-hydrostatic nature potentially

158 leading to large vertical velocities and instabilities. In this study, only bottom grid cell
159 Lagrangian particles are considered as these are the particles that affect the formation rate
160 and properties of AABW and NADW.

161 Bottom particles are created when the difference in density between the dense shallow
162 and less dense deep ocean cell is greater than the defined threshold $\Delta\rho$. The Lagrangian
163 particles then transport mass and momentum, while interacting with the bottom grid cells
164 of the Eulerian model, until they are destroyed and their properties returned to the Eulerian
165 model (Figure 3).

166 The simplicity of the point particles definition allows a more complete set of dynamics,
167 and hence a more complete representation of overflow processes, to be applied to the La-
168 grangian framework (Bates et al., 2012a). For example, BLOBS includes non-hydrostatic
169 momentum and an entrainment parameterizations based on Price and Baringer (1994). In
170 idealised model set-ups (the DOME by Legg et al. (2006) and bowl by Winton et al. (1998)),
171 the dynamic bottom BLOBS scheme enhances downslope transport and circulation response
172 due to more realistic dynamics than previous overflow schemes (Bates et al., 2012b). Note
173 however, a recently discovered coding error reduces the increase in circulation of the bowl
174 case given in Bates et al. (2012b) (Appendix A). The computational overhead of BLOBS is
175 proportional to the number of active Lagrangian particles, with the bowl test case leading
176 to a 16-117% increase in computational time and insignificant increase in the DOME case
177 (Bates, 2011). However, BLOBS is yet to be tested outside an idealized model configuration.

178 **3. Model and Methods**

179 We define a model domain that allows a range of sensitivity tests to be performed for
180 each of the overflow parameterizations. A computationally fast domain is required due to
181 the large number of model runs that need to be performed. We also need a model that
182 represents all the key characteristics of current GCMs and the factors that affect AABW
183 and NADW formation. Hence, a 1° horizontal resolution sector model of the Atlantic, the
184 primary formation regions of AABW and NADW, is developed.

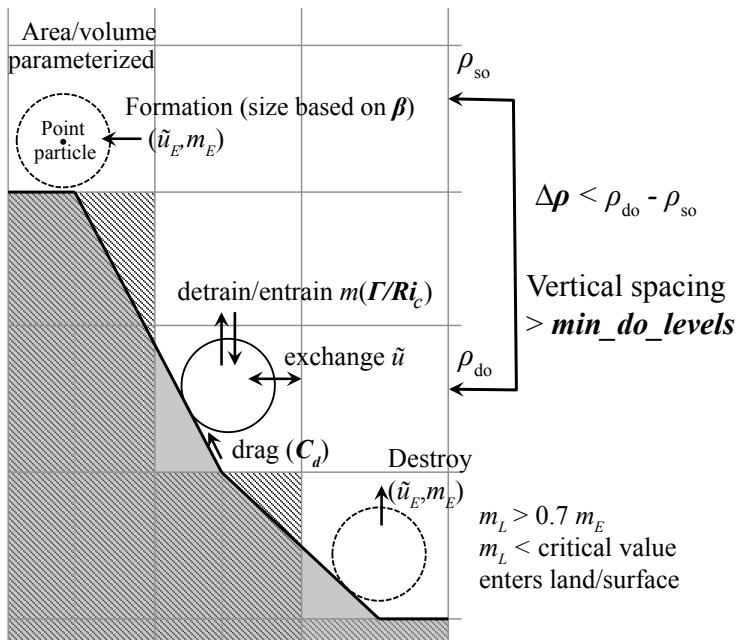


Figure 3: A representation of the dynamic bottom BLOBS scheme (based on Bates et al. (2012a)). Dashed circles indicate Lagrangian particle formation and destruction while a solid circle is an active particle with mass and momentum in the Lagrangian system given by m_L and \tilde{u}_L and in the Eulerian system by m_E and \tilde{u}_E . Methods for particle destruction are given in the bottom right with conditions for formation above. Hatched grid cells are land points while shaded regions indicate the effective bathymetry seen by the Lagrangian particles (Bates et al., 2012a). Parameters here are; bottom drag (C_d), the detrainment parameter (Γ), the critical Richardson number (Ri_c), $\beta = \frac{\delta}{\mu}$, and the minimum vertical spacing to allow Lagrangian particle formation (min_do_levels). Each parameter is defined in more detail in Section 3.3.3

185 3.1. Sector Domain

186 The Atlantic sector is created by scaling topography derived from the NOAA/GFDL
 187 $1/4^\circ$ model global bathymetry (Delworth et al., 2012) and the Weddell Sea coast of the
 188 ETOPO2 version 2 globally gridded 2 minute ocean and land topography, referred herein as
 189 ETOPO2 (U.S. Department of Commerce, National Oceanic and Atmospheric Administra-
 190 tion, National Geophysical Data Center, 2001). The ETOPO2 data is only used where the
 191 GFDL bathymetry has idealised straight edge boundaries along the Weddell Sea coast; at
 192 all other locations we choose the GFDL bathymetry due to its proven applicability within
 193 the model's framework. The ETOPO2 data replaces the GFDL bathymetry between the

194 sector latitudes of 78.47°S to 70.74°S and longitudes of 3.375°E to 30.123°E (corresponding
195 to global longitudes of 72°W to 35°W) and smoothing is applied at the ETOPO2 and GFDL
196 boundary to ensure no sharp edges are created.

197 Two piecewise-linear boundaries set the longitudinal limits of the domain (red lines in
198 Figure 4a). The topography within the boundary region is deformed at each latitude via
199 a linear mapping to a fixed 60° wide section and interpolated to a 1/4° Mercator grid
200 (Figure 4b). The boundaries are chosen to follow land masses and so create closed wall
201 boundaries everywhere except Drake Passage. Periodic boundary conditions are applied at
202 Drake Passage to simulate the Antarctic Circumpolar Current (ACC); the land boundary is
203 defined so that the two Antarctic eastern and western edges, and the Africa-South America
204 boundary match (Figure 4c). Due to this 60° wide boundary restriction and the increased
205 computational efficiency of a reduced domain, our configuration is advantageous over an
206 approach that does not deform the bathymetry and uses a land fill to remove the ocean
207 outside the boundary region. Also, land filling does not permit a smooth transition of the
208 topography for the periodic ACC flow and requires more land points to be taken into account
209 in the model computations.

210 Following the deformation and smoothing, all inland lakes and the Mediterranean Sea are
211 filled in, land is added to the eastern and western boundaries to ensure no re-entrant regions
212 outside Drake Passage and some minor smoothing of the Antarctic and North Atlantic
213 continental slopes is performed (Figure 4b). With the model set-up initially at $\frac{1}{4}^\circ$ resolution,
214 the topography is then interpolated to create the 1° resolution domain used in this study.
215 1° is chosen over $\frac{1}{4}^\circ$ due to the need for computational speed; higher resolution simulations
216 are ongoing.

217 While the deformation may influence the shape of important regions of deep and bottom
218 water pathways (e.g. the mid-Atlantic ridge), the bathymetry retains the primary features
219 that control both AABW and NADW flow. Despite the shift of the mid-Atlantic ridge, the
220 AABW (and NADW) follows the expected path, moving along the western continental rise
221 south (north) of the equator and flowing against the mid-Atlantic ridge north (south) of the
222 equator.

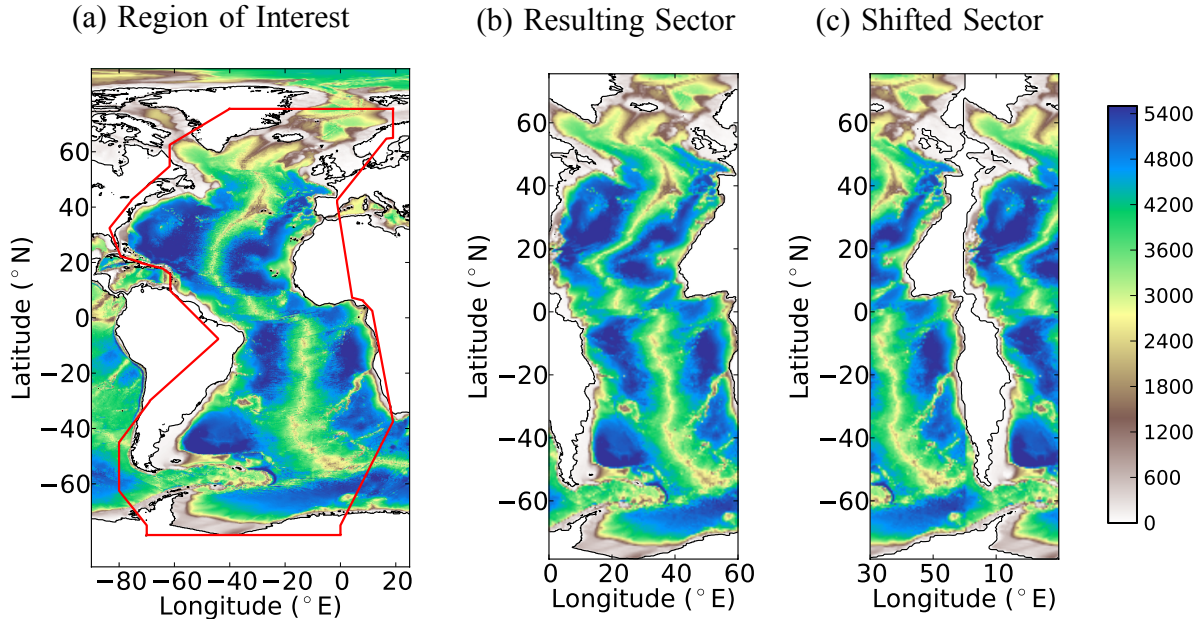


Figure 4: (a) The defined boundaries for the domain of the sector, with the GFDL bathymetry shown only in this case. The region within the boundary is deformed to fit a 60° wide sector resulting in (b) with smoothing across the boundary for the periodic ACC indicated by the smooth transition in the shifted sector in (c).

223 3.2. Model Properties

224 The Modular Ocean Model version 5 (MOM5, Griffies (2012)) is chosen to represent
 225 the ocean. The model employs a z^* vertical co-ordinate with partial cells and gradually
 226 increasing vertical grid spacing from 10 m at the surface to 200 m at depth, providing a
 227 total of 65 vertical levels to 5.5 km deep. Horizontal resolution of 1° is used employing
 228 the Gent and McWilliams (1990) eddy parameterization and the Fox-Kemper et al. (2008)
 229 parameterization of submesoscale eddies. The KPP surface boundary layer scheme of Large
 230 et al. (1994) is used, along with the interior gravity wave induced mixing scheme of Simmons
 231 et al. (2004) and the coastal tide mixing scheme of Lee et al. (2006). The background
 232 diffusivity is defined as $1 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ and the background viscosity as $5 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$.
 233 Horizontal frictional dissipation is achieved through the biharmonic Smagorinsky viscosity
 234 scheme (Griffies and Hallberg, 2000), however a Laplacian operator is employed in the lower
 235 five points of the model to maintain the stability of the model on small partial cells near

236 the shelves.

237 The nonlinear equation of state of Jackett et al. (2006) is applied, as the physical processes
238 involved in the overflows include nonlinear effects such as cabbelling and thermobaricity
239 (McDougall, 1987; Gordon et al., 1993; Foldvik et al., 2004; Urakawa and Hasumi, 2012).
240 The ocean model is coupled to the GFDL Sea Ice Simulator (SIS) (Winton, 2000), which
241 is run on the same Mercator grid as the ocean model. A non-linear equation for the frazil
242 ice formation is applied as we find that the linear form significantly decreases (by order
243 0.05 kg m^{-3}) the shelf water densities on the Antarctic shelf (Appendix B), an undesirable
244 effect as it decreases the flow of water down the slope. The Coordinated Ocean-ice Reference
245 Experiments (CORE) Normal Year Forcing (Large and Yeager, 2009) atmospheric state is
246 coupled to the ocean and ice model. The CORE product is deformed in the same manner as
247 the bathymetry after first being interpolated to a $\frac{1}{4}^\circ$ resolution for the deformation process,
248 and then to 1° . Applying the same deformation procedure allows for continuity between the
249 devised ocean and land and the atmosphere.

250 The model is initiated from the January Levitus (1994) climatology in the World Ocean
251 Atlas (WOA 2009) with the temperature and salinity fields deformed in the same manner
252 as the global bathymetry. Sea surface salinity is restored to monthly climatologies that
253 have similarly been deformed. The model is then spun-up for 2660 years to a control state
254 where sufficient AABW and NADW is produced to allow a suitable sensitivity analysis of
255 the overflow parameterizations.

256 *3.3. Parameter Space*

257 The control run (CTR), excludes any overflow scheme and reaches equilibrium (defined
258 by $<10\%$ change in zonal mean age per 200 years, averaged over the entire domain) at 2660
259 years. Each of the separate overflow schemes are applied individually starting from year 2660
260 and run for 200 years. The parameters chosen for each run (defined below) are varied about
261 recommended default values to explore a suitably large parameter space that encompasses
262 the range of responses possible from the schemes.

263 3.3.1. CG1999, MIXD and OVER

264 A summary of the parameter choices for testing CG1999, MIXD and OVER is given in
265 Table 1. The key tuneable parameter of CG1999 is $\gamma = \frac{\delta S}{\mu}$ (Equation (1)); however, since
266 slope S is not an external parameter, we define $\beta = \frac{\delta}{\mu}$ as the primary parameter to be varied
267 in the sensitivity analysis.

268 Campin and Goosse (1999) recommend values of $\delta = \frac{1}{3}$ and $\mu = 10^{-4} \text{ s}^{-1}$, hence $\beta_0 =$
269 $\frac{1}{3} \times 10^4 \text{ s}$ is used as the default value. To obtain a suitable spectrum of parameters, δ is
270 varied within the bounds of the parameter ($\delta = 0.1$ and $2/3$) and μ is varied by an order
271 of magnitude in either direction ($\mu = 10^{-3} \text{ s}^{-1}$, 10^{-5} s^{-1}). These parameters give β values
272 of $0.3\beta_0$, $2\beta_0$, $0.1\beta_0$ and $10\beta_0$ respectively. Both return flow and no return flow cases are
273 considered.

274 OVER has the same defining β parameter as CG1999, but now with the additional pa-
275 rameter determining the number of grid cells (n) used in the search for the neutral buoyancy
276 level. Due to the similarity between OVER and CG1999, fewer values of β are tested.

277 In MIXD, the defining parameters vary from CG1999 and OVER due to the partial
278 mixing of tracers of this method. The defining parameters of MIXD are δ_s (the fraction of
279 the shallow ocean cell participating in the downslope flow) and n . Again, due to similarity
280 of this scheme to both CG1999 and OVER, only limited parameter choices are considered.
281 Applying a weighting term (*weight*) for farther cells is also considered for OVER and MIXD
282 where an increased fraction of tracer is transported to furthest n cells, rather than an
283 equivalent fraction across each of the n cells. For the MIXD case, a final option where the
284 scheme is set at the default parameters but a mask is applied removing the scheme from the
285 northern half of the sector is tested. This run, referred to as *mask*, allows us to attribute
286 changes to northern or southern overflow processes.

287 3.3.2. SIGMA

288 The SIGMA parameter variations are given in Table 2. The default case is chosen as the
289 case where a velocity dependent diffusion is applied (Equation 8). The defining parameter
290 for such a case is the sigma diffusivity ratio $\kappa_\sigma^{ratio} = A_{min}/A_{max}$ (or $\kappa_\sigma^{ratio} = A_{min}/|u|\delta x$ for

Run	β (s) or δ_s	return flow(CG1999) or weighted(MIX,OVER)	n
CG1999 (default)	$\beta = \beta_0$	false	1
CG1999 ($0.1\beta_0$)	$\beta = 0.1\beta_0$	false	1
CG1999 ($0.3\beta_0$)	$\beta = 0.3\beta_0$	false	1
CG1999 ($2\beta_0$)	$\beta = 2\beta_0$	false	1
CG1999 ($10\beta_0$)	$\beta = 10\beta_0$	false	1
CG1999 (<i>rf</i>)	$\beta = \beta_0$	true	1
OVER (default)	$\beta = \beta_0$	false	1
OVER ($0.3\beta_0$)	$\beta = 0.3\beta_0$	false	1
OVER ($10\beta_0$)	$\beta = 10\beta_0$	false	1
OVER ($n = 2$)	$\beta = \beta_0$	false	2
OVER ($n = 6$)	$\beta = \beta_0$	false	6
OVER (<i>weight</i>)	$\beta = \beta_0$	true	6
MIX (default)	$\delta_s = 0.333$	false	1
MIX ($\delta_s = \frac{2}{3}$)	$\delta_s = 0.666$	false	1
MIX ($\delta_s = 1.0$)	$\delta_s = 1.0$	false	1
MIX ($n = 2$)	$\delta_s = 0.333$	false	2
MIX ($n = 4$)	$\delta_s = 0.333$	false	6
MIX (<i>weight</i>)	$\delta_s = 0.333$	true	6
MIX (<i>mask = south only</i>)	$\delta_s = 0.333$	false	1

Table 1: Parameter domain of CG1999, MIXD and OVER for varying β , δ_s , and n , with options for weighted runs and implementing return flow. Refer to the text for further details.

Run	κ_σ (m ² s ⁻¹)	κ_σ^{ratio}	velocity dependent diffusivity
SIGMA (default)	N/A	10⁻⁶	true
SIGMA ($\kappa_\sigma^{ratio} = 10^{-4}$)	N/A	10 ⁻⁴	true
SIGMA ($\kappa_\sigma^{ratio} = 10^{-8}$)	N/A	10 ⁻⁸	true
SIGMA ($\kappa_\sigma = const$)	10 ³	10 ⁻⁶	false

Table 2: Parameter domain of SIGMA for varying κ_σ and κ_σ^{ratio} and the option of implementing constant diffusivity. Refer to the text for further details.

291 the velocity dependent case) with A_{max} and A_{min} defined in Equation (7). The recommended
292 default value of κ_σ^{ratio} (1×10^{-6} , the default within MOM5) is applied with variations by two
293 orders of magnitude (1×10^{-4} and 1×10^{-8}). A final variation through the application of
294 a constant diffusivity $\kappa_\sigma = A_{max}$ (Griffies, 2012) is investigated with the magnitude chosen
295 based on the scheme’s preset value of 1×10^3 m² s⁻¹.

296 3.3.3. BLOBS

297 The parameter variations for BLOBS are summarised in Table 3 and their application
298 within the Lagrangian system is represented in Figure 3. Numerical parameters such as the
299 relative error of the Runge-Kutta and time step are ignored as they do not affect the physical
300 parameters. The parameters to be tested are β , the dimensionless bottom drag coefficient
301 C_d , the detrainment parameter Γ and the critical Richardson number Ri_c defining the degree
302 of entrainment.

303 We define the number of particles formed by setting the minimum density difference
304 between shallow and deep ocean cells that permits the creation of a Lagrangian particle,
305 $\Delta\rho$, to 0.013 kg m⁻³ and the minimum slope on which a Lagrangian particle is formed,
306 min_do_levels , to 5 (see Figure 3). This choice is a pragmatic value, taking into account
307 the computational cost of BLOBS and defining shelf densities in the CTR case. With the
308 default values chosen, we test the influence of increased and decreased particle formation
309 rates through increasing/decreasing $\Delta\rho$ and min_do_levels (the *more/less* cases in Table 3)

310 Bates et al. (2012b) tested variations of the detrainment parameter (Γ), determining
311 that the degree of detrainment was less sensitive to change when Γ was decreased below
312 5×10^{-8} kg m⁻² s⁻¹; we perform similar tests in a realistic ocean configuration. Hence,

Run	β (s)	C_d	Γ (kg m ⁻² s ⁻¹)	Ri_c	min_do	$\Delta\rho$
BLOBS (default)	β_{0b}	3×10^{-3}	5×10^{-8}	0.8	5	0.013
BLOBS ($4\beta_{0b}$)	$4\beta_{0b}$	3×10^{-3}	5×10^{-8}	0.8	5	0.013
BLOBS ($0.5\beta_{0b}$)	$0.5\beta_{0b}$	3×10^{-3}	5×10^{-8}	0.8	5	0.013
BLOBS ($C_d = 3 \times 10^{-2}$)	β_{0b}	3×10^{-2}	5×10^{-8}	0.8	5	0.013
BLOBS ($C_d = 3 \times 10^{-4}$)	β_{0b}	3×10^{-4}	5×10^{-8}	0.8	5	0.013
BLOBS ($Ri_c = 0.4$)	β_{0b}	3×10^{-3}	5×10^{-8}	0.4	5	0.013
BLOBS ($Ri_c = 1.2$)	β_{0b}	3×10^{-3}	5×10^{-8}	1.2	5	0.013
BLOBS ($\Gamma = 5 \times 10^{-7}$)	β_{0b}	3×10^{-3}	5×10^{-7}	0.8	5	0.013
BLOBS ($\Gamma = 5 \times 10^{-9}$)	β_{0b}	3×10^{-3}	5×10^{-9}	0.8	5	0.013
BLOBS (<i>more</i>)	β_{0b}	3×10^{-3}	5×10^{-8}	0.8	2	0.010
BLOBS (<i>less</i>)	β_{0b}	3×10^{-3}	5×10^{-8}	0.8	8	0.016

Table 3: Parameter domain of BLOBS where β , C_d , Ri_c and Γ are the varied parameters along with the number of active particles formed through *min_do_levels* (shortened to *min_do* above to conserve space) and $\Delta\rho$. For details refer to the text.

313 a default of 5×10^{-8} kg m⁻² s⁻¹ is chosen with variations to 5×10^{-7} kg m⁻² s⁻¹ and
314 5×10^{-9} kg m⁻² s⁻¹. The critical Richardson number defining the degree of entrainment
315 is tested about the suggested default value of 0.8 (Bates et al., 2012b), increasing and
316 decreasing it to 1.2 and 0.4 respectively.

317 The parameter β is applied in BLOBS as the scheme relies on a similar processes to
318 CG1999 in determining the initial formation of a Lagrangian particle. Hence, β is used to
319 calculate, for example, the initial size of the particle relative to the grid cell volume. The
320 default β for BLOBS is defined as β_{0b} and chosen to be 0.16666. Variations increasing and
321 decreasing β to $\frac{1}{2}\beta_{0b}$ and $4\beta_{0b}$ are tested.

322 Bates et al. (2012b) determined that increasing the bottom drag decreases the downslope
323 speed and increases the depth that the particles penetrates in an idealised slope configura-
324 tion. We choose the default bottom drag based on that suggested by Bates et al. (2012b)
325 ($C_d = 3 \times 10^{-3}$) and test the model’s sensitivity to an order of magnitude increase and
326 decrease about this value.

327 The default value of the minimum mass of the Lagrangian particles before they are
328 destroyed (1×10^3 kg) will not be considered in the sensitivity study as smaller values can
329 lead to roundoff errors and numerical errors (Griffies, 2012). Similarly, the default value of

330 the maximum portion of a grid cell that a Lagrangian particle may occupy (0.7) will be held
331 constant, as Bates (2011) found that a larger value results in the bottom cells constraining
332 the particle mass.

333 *3.3.4. Model runs*

334 The yearly temperature, salinity, density, age and transport are assessed to diagnose
335 the effect of varying overflow schemes and parameters on the overturning and deep ocean
336 properties. Here, age is defined as the time since the water has been in contact with the sur-
337 face. Note, there is no model diagnostics for the mass transport of the Lagrangian particles,
338 therefore their contribution is not included in calculations of the overturning streamfunction.
339 However, the particles influence on the Eulerian model may still be partly discerned through
340 the changes they induce compared to CTR.

341 Many of the results are simplified to a time mean of the last 20 years to provide an
342 indication of the overflow scheme's overall performance. Two regions are used to diagnose
343 the overflow scheme's impact in the northern and southern Atlantic regions; the north
344 region is the zonally and meridionally averaged region from 32.4°-62.4°N and represents
345 a 30° area south of the Denmark Strait, and the south region is zonally and meridionally
346 averaged within 44.7°-74.7°S and represents the region 30° north of the Antarctic slope
347 edge. These regions are chosen for the analysis as it allows both north and south responses
348 to be quantified separately and hence the sensitivity of each scheme to AABW and NADW
349 overflows. We choose the north/south regions to encompass the areas extending from the
350 northern/southern edge of the overflows. This area is large enough that the influence the
351 schemes have on the downstream deep and bottom water properties can be clearly assessed.

352 **4. Results**

353 *4.1. Model Performance*

354 Due to the novel nature of the sector model, a brief model evaluation of the control
355 state is presented. At 2660 years, the ACC transport is approximately 50 Sv, appearing
356 to have reached equilibrium (not shown). This transport is less than half the observed

357 value (137 ± 7 Sv; Meredith et al., 2011). At $\frac{1}{4}^\circ$ resolution the Drake Passage transport is
358 84 Sv, indicating resolution affects the transport here. Further, factors influencing the ACC
359 outside the Atlantic (e.g. ≈ 15 Sv transport provided by Indonesian Through-flow to ACC
360 (Sprintall et al., 2009)) are not included in the sector model.

361 The decadal mean NADW transport at 30°N (defined as the maximum in the upper
362 overturning cell in potential density space referenced to 2000 m, $\sigma_2 > 36.6 \text{ kg m}^{-3}$) and the
363 AABW transport at 30°S (defined as the maximum in the lower overturning cell in potential
364 density space, $\sigma_2 > 36.6 \text{ kg m}^{-3}$) are found to be 3.6 Sv and 2.2 Sv respectively (Figure
365 5). There is a strong pole-to-pole upper overturning cell, indicated by the red streamlines
366 outcropping in the Southern Ocean. The low NADW transport and maximum cell transport
367 of 7 Sv (compared to max Atlantic Meridional Overturning Circulation (AMOC) of e.g. 18 Sv
368 at 26.5°N from RAPID observations; Johns et al., 2011), is likely due to the incomplete
369 representation of factors that contribute to the NADW, such as the closed wall boundary in
370 the north and the closed Mediterranean overflow. The latter, however, is partially accounted
371 for with surface salinity restoring and so we expect the influence of the closed Mediterranean
372 to be less than 1 Sv (Rahmstorf, 1998; Chan and Motoi, 2003; Ivanovic et al., 2014).

373 The CORE NYF surface forcing may also influence the AABW and NADW transports
374 (Gerdes et al., 2006) along with open ocean convection processes (Zhang et al., 2011). With
375 only the Weddell Sea source region included in the sector, a weaker AABW transport is
376 expected as we have included only one sixth of the Antarctic coastline. Finally, the lack
377 of an overflow scheme in CTR we would expect descending deep and bottom waters to be
378 overly influenced by the convective mixing on the topographic steps (e.g., Beckmann and
379 Döscher, 1997; Winton et al., 1998; Legg et al., 2006). Despite the relatively weak NADW
380 and AABW transports, we obtain a representation of NADW- and AABW-like overflows
381 and water masses that show similar interactions (not necessarily of the same magnitude)
382 and properties to those expected. We argue that such transport is sufficient to provide an
383 evaluation of the sensitivity of the overturning circulation to the overflow parameterizations.

384

385 The model density and tracer fields (Figures 5c and 6) are similar to those found in the

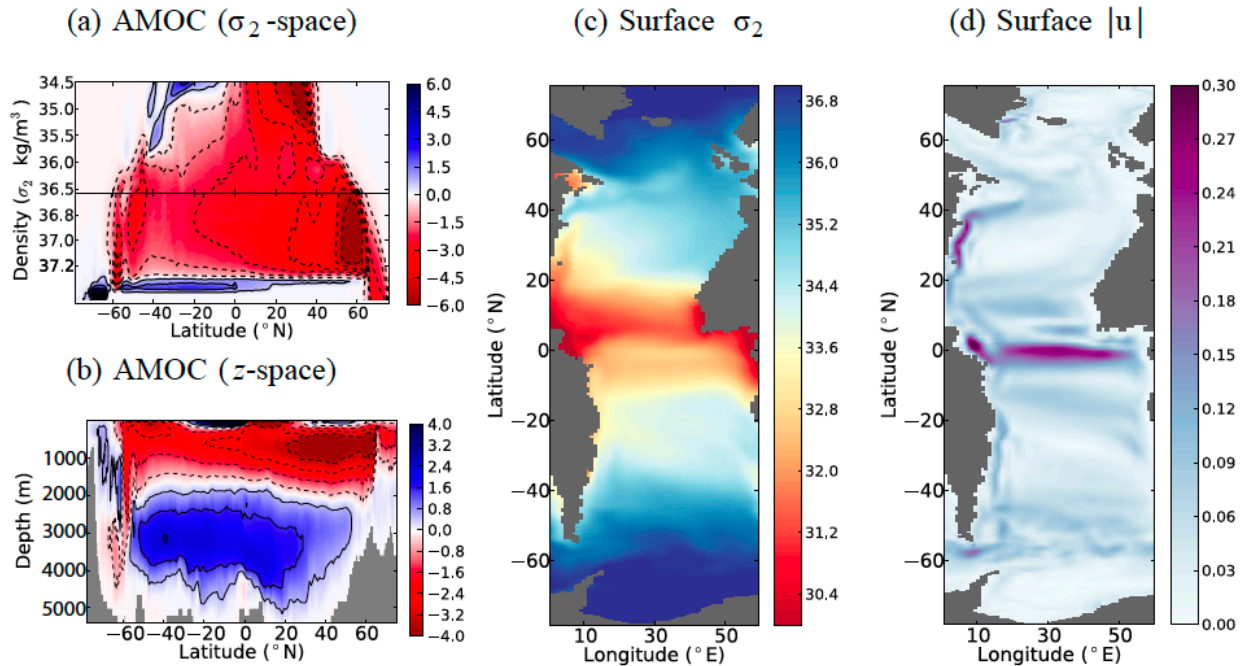


Figure 5: 10 yr mean state from 2660-2670 years for 1° resolution sector model with (a) Meridional Overturning (S_v) in density space and (b) z -space where contours are at unit intervals from 0.5 and -0.5 (with negative indicating clockwise overturning), (c) Surface density in σ_2 (kg m^{-3}) and (d) absolute mean surface velocity (m s^{-1}).

386 global climate model configurations using the MOM4p1 ocean component (Dunne et al.,
 387 2012; Danabasoglu et al., 2014), however there is a cool and fresh bias compared to observa-
 388 tions. Despite the transformed sector shape, many of the major surface circulation pathways
 389 (e.g. equatorial currents and western boundary currents) are reproduced (Figure 5d). The
 390 range of processes available in this sector is a step forward compared to idealised bathymetry
 391 sectors (e.g., Hogg et al., 2013; Munday et al., 2013) where much of the dynamics and forcing
 392 are also idealised and so are unable to incorporate all the key factors of a GCM.

393 4.2. Parameterizations Comparison

394 The five different default parameterization schemes of CG1999, OVER, MIXD, SIGMA
 395 and BLOBS are initially compared to each other and to CTR in the north and south analysis
 396 regions. With only a 200 year model period, further changes are expected if the simulations
 397 continued, however computational constraints do not permit equilibration. Due to the ap-

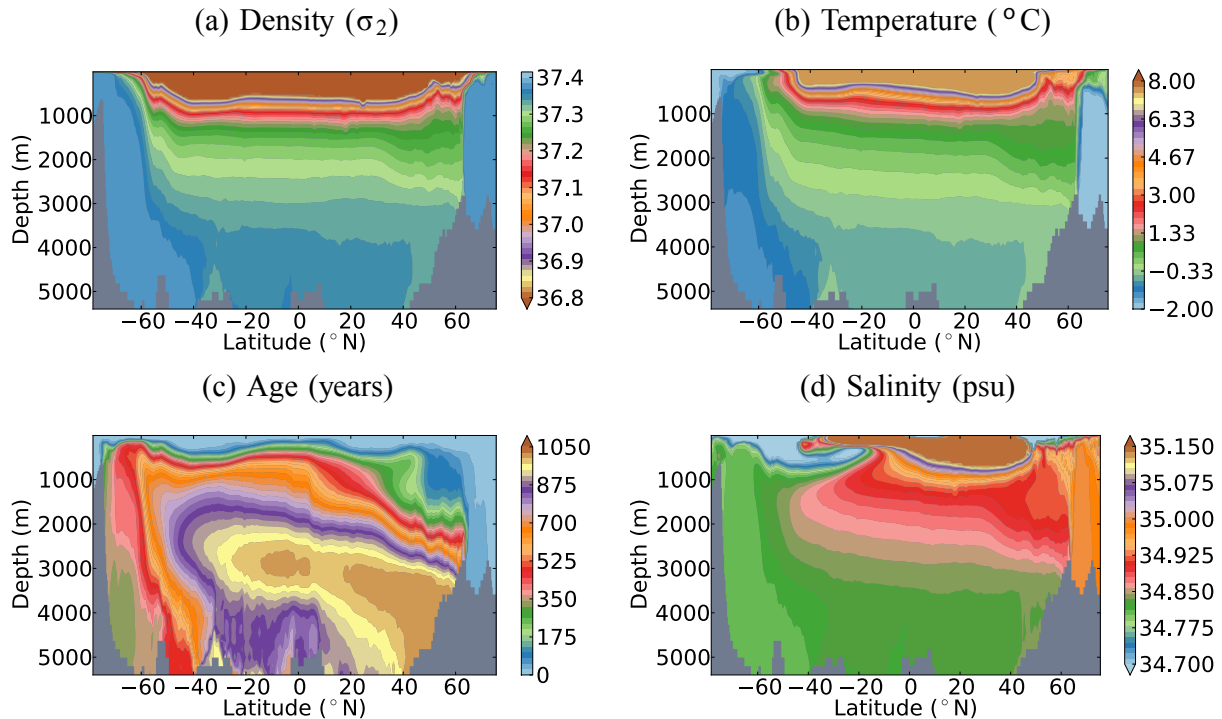


Figure 6: 10 yr mean state from 2660-2670 years for the 1° resolution sector model with zonally averaged fields of (a) potential density in σ_2 (kg m^{-3}), (b) temperature ($^\circ\text{C}$), (c) age (years) and (d) salinity (psu).

398 proximately constant trends in the last 100 years (Figure 7), the model change compared to
 399 CTR and relative sensitivity produced by each scheme is well represented within this period.
 400 In fact, it is clear after only 50 years that MIXD dominate in the north and south, leading
 401 to an increase in density and decrease in age. Hence a time mean of the last 20 years is a
 402 suitable measurement of the sensitivity of each overflow scheme.

403 Profiles of area-averaged temperature, salinity, density and age differences from CTR
 404 for the years 180-200 are found for the north and south regions (Figure 8). The greatest
 405 response in both the north and south is produced by MIXD. In the north, MIXD leads to
 406 saltier and warmer waters descending below 2000 m and 2500 m respectively. With the
 407 density response dominated by salinity, the tracer changes produce a maximum increase
 408 in density below the surface of 0.02 kg m^{-3} at 2500 m and a decrease in age of 400 years
 409 (42%) at 3200 m. Note, the change in age is greater than the period of the model run (200

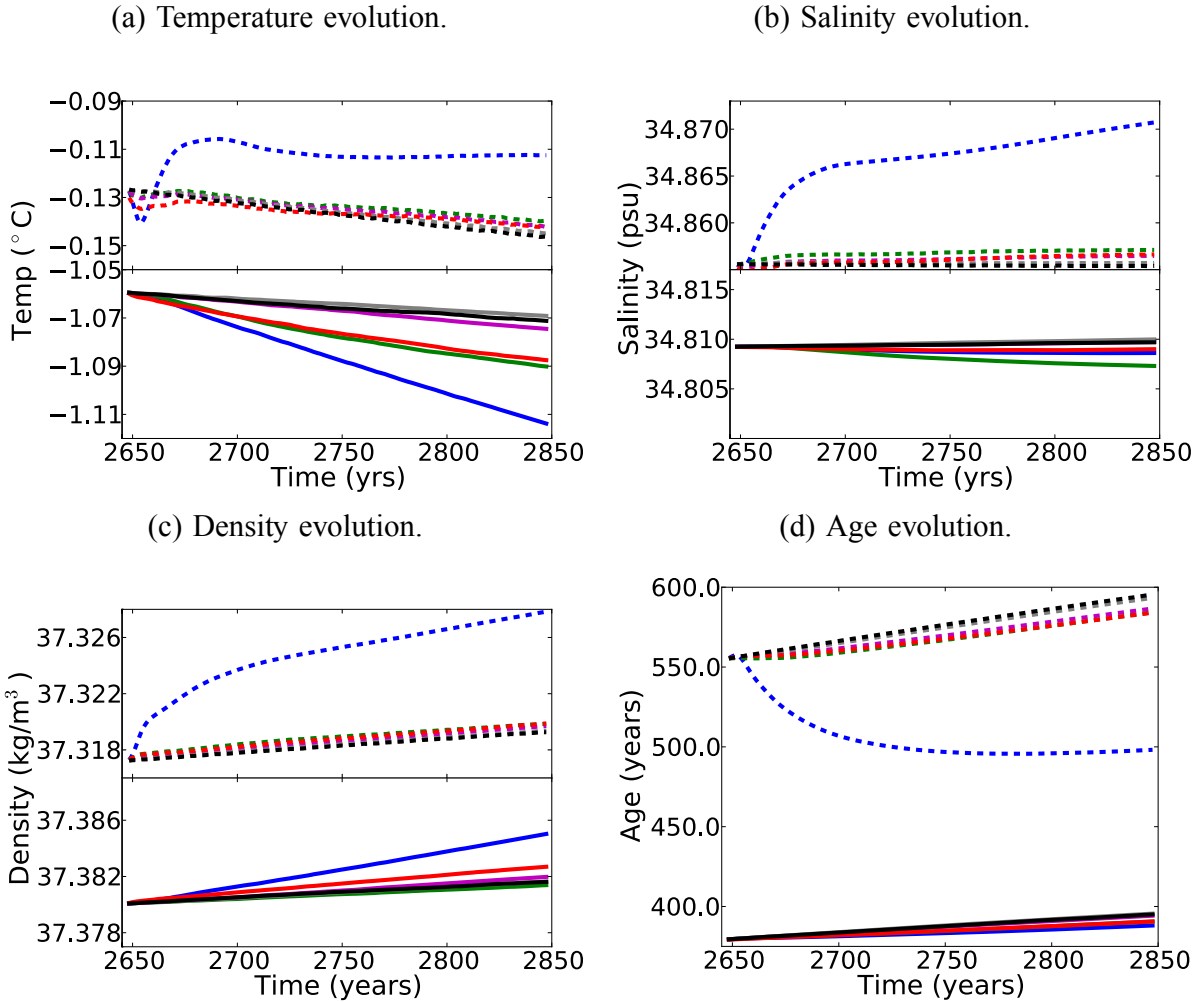


Figure 7: Evolution of (a) temperature ($^{\circ}\text{C}$), (b) salinity (psu), (c) density in σ_2 (kg m^{-3}) and (d) age (years) for the default setup of each scheme over the 200 years the overflow schemes are applied (coloured lines) compared to CTR (black) where no overflow scheme is applied. Quantities are calculated as the average of the bottom two grid cells below 2 km in the region 30° south of the Denmark Strait (dashed lines) and the region 30° north of the Antarctic slope edge (solid lines). Note the discontinuity in the vertical axes of (a), (b) and (c), and the CG1999 is often overlaid by the CTR case.

410 years) due to changes in circulation that alter the regions of differently defined age water
 411 masses. In the south, the changes are much smaller. While cooler and slightly fresher waters

412 descend the south in MIXD leading to an increase in density and decrease in age over the
413 water column, the magnitudes (0.003 kg m^{-3} and 20 years respectively) are just 30% the
414 vertically integrated absolute change in density and 10% of the age changes produced in the
415 north.

416 The effect of CG1999, OVER, SIGMA and BLOBS on tracer properties is negligible
417 ($<3\%$ change in age and $<0.2\%$ in density) in the south (solid lines in Figure 8)). Measurable
418 changes are found in the north region (dashed lines), where age decreases by a maximum of
419 40 years (5%) at 2750 m for these schemes and changes in temperature and salinity lead to
420 an increase in density below the surface by a maximum of 0.005 kg m^{-3} at 1750 m.

421 The difference in the MOC from the CTR (Figure 9) for the last 20 years for CG1999,
422 OVER, SIGMA or BLOBS (Figure 9a, 9b, 9c and 9d respectively) shows minimal change
423 in the AABW anti-clockwise cell. However, OVER, SIGMA and BLOBS each increase the
424 density of the clockwise NADW cell (the negative red band in Figure 9) without signifi-
425 cantly altering (to an error of 1%) the maximum streamfunction and hence our diagnostic of
426 NADW transport. BLOBS provide a larger change in circulation in the north than CG1999,
427 supporting the updated results of Bates et al. (2012b) that take into account code error (Ap-
428 pendix A). We stress that the BLOBS Lagrangian particle contribution to the overturning
429 is not included in the calculated streamfunctions producing some uncertainty in the specific
430 values of the streamfunction. The particles exclusion from the transport term also leads to
431 the spike observed in Figure 9d at 20°N where a large number of particles are accumulat-
432 ing and being destroyed, returning their momentum and mass properties to the Eulerian
433 model. The overall influence and order of magnitude of the BLOBS scheme on the Eulerian
434 model may still be interpreted from the streamfunctions as particle lifetimes are often less
435 than one year and results shown are at 200 years. A similar approach for the barotropic
436 streamfunction was applied in Bates et al. (2012b).

437 MIXD (Figure 9e) provides the greatest change in the north, increasing the density of
438 the NADW cell throughout the model domain. However, the movement of water to greater
439 densities distributes the NADW over a greater depth range, reducing the peak of the anti-
440 clockwise cell so that the defined NADW transport decreases by 0.2 Sv (5%). MIXD also

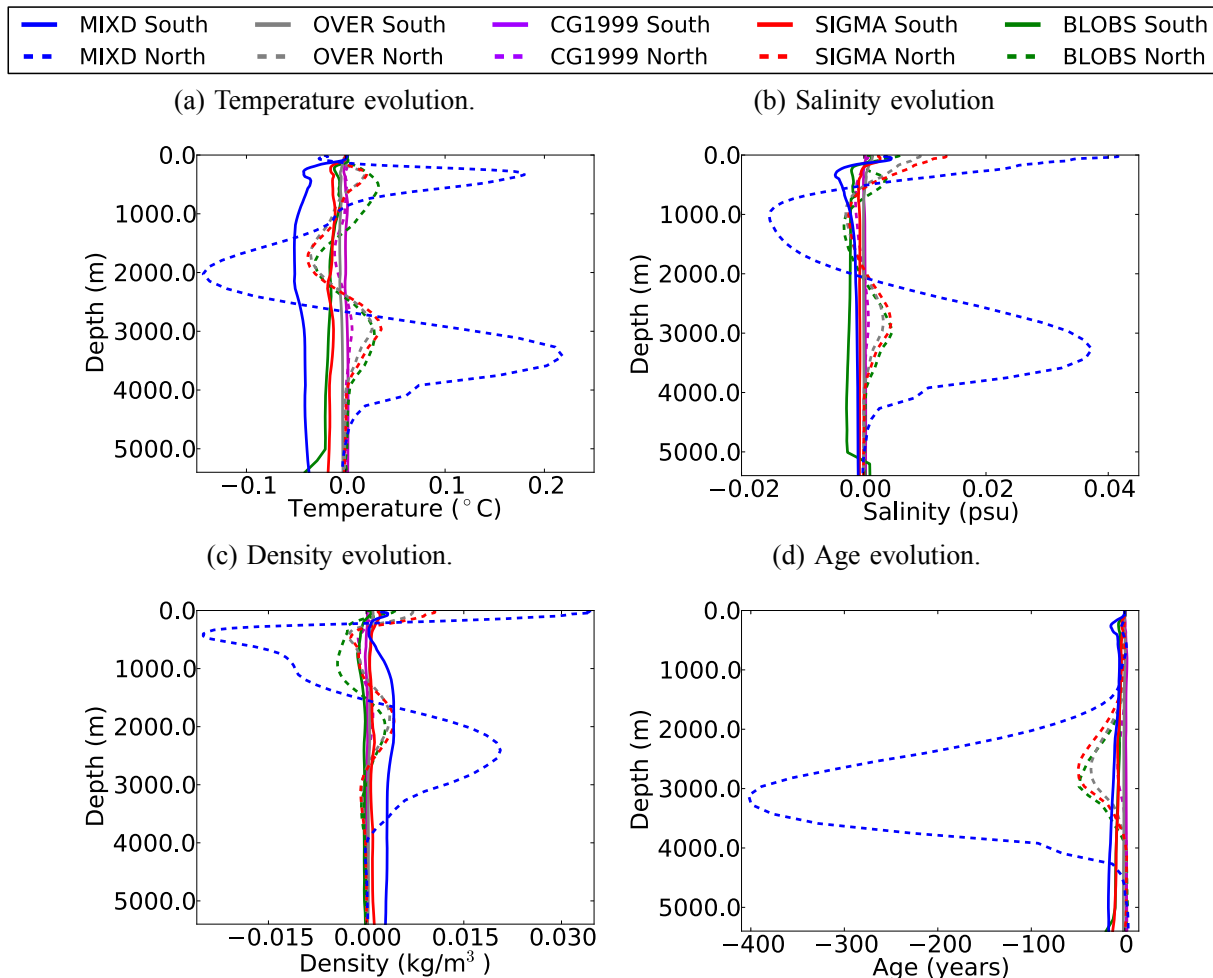


Figure 8: Mean difference from CTR in (a) temperature ($^{\circ}\text{C}$), (b) salinity (psu), (c) density (kg m^{-3}) and (d) age (years) averaged over the region 32.4°N - 62.4°N (dashed lines) and 44.7°S - 74.7°S (solid lines) versus depth for each of the different parameterizations. The difference is defined as the time average of the last 20 years in the overflow scheme runs minus the equivalent of the CTR. Note, that profiles of CG1999, OVER and SIGMA overlie in the south.

441 produces a slight increase in density of the AABW cell southward of 20°N . In this case
 442 the increase occurs over the region where the peak transport of the cell occurs, thereby
 443 increasing AABW transport by 0.2 Sv (9%).

444 The minimal change produced by CG1999 may be expected based on the results of
 445 Goosse et al. (2001). They found only a relatively weak response of AABW to the return
 446 flow CG1999 case with the application of realistic surface forcing (the more complete AABW

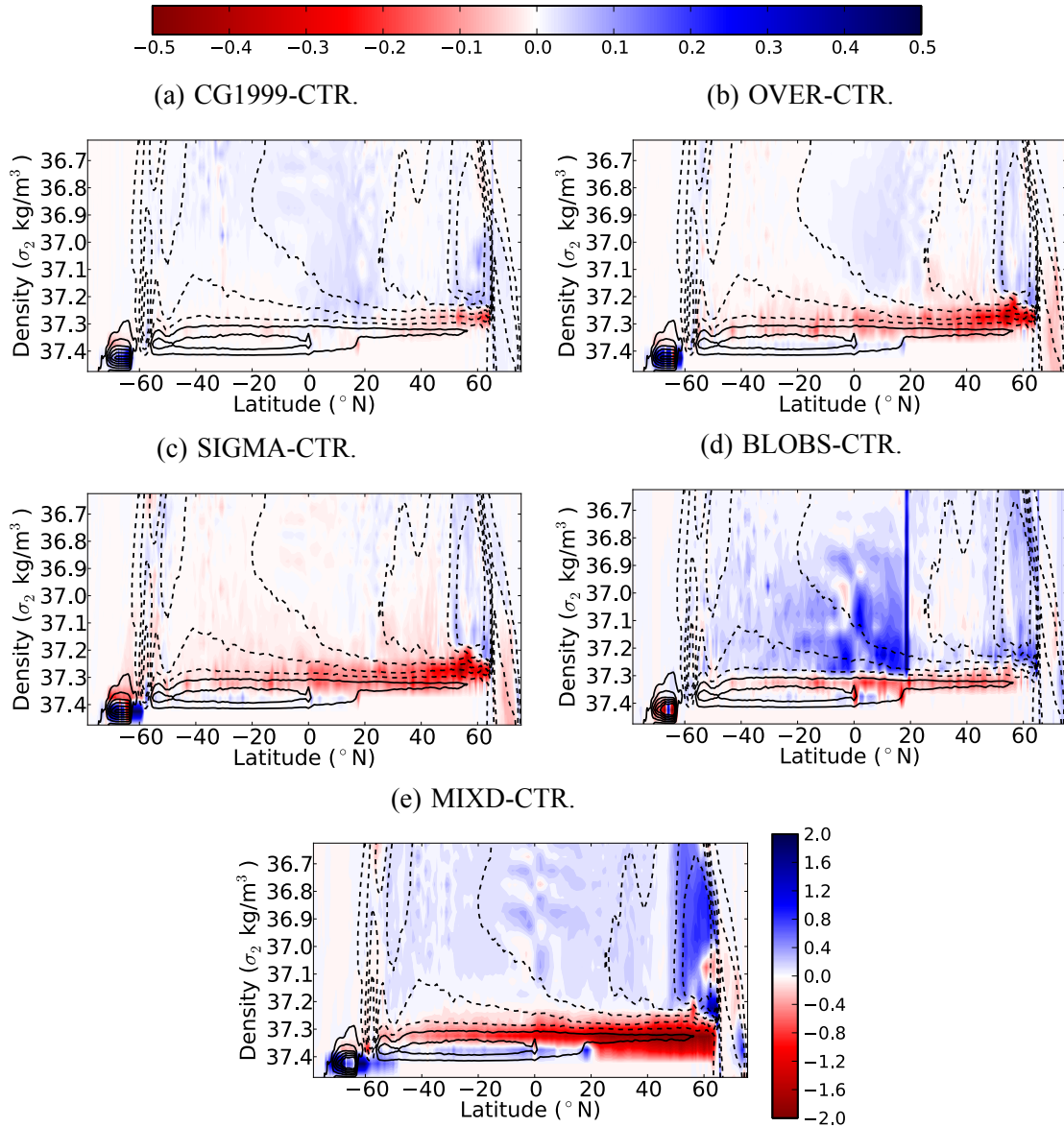


Figure 9: Difference in meridional overturning (Sv) from CTR in potential density space referenced to 2000 m (σ_2) for the cases (a) CG1999, (b) OVER, (c) SIGMA, (d) BLOBS and (e) MIXD for years 180-200 in the default parameter runs. The contours represent the mean overturning of CTR in this period with solid contours indicating anti-clockwise overturning and dashed clockwise at unit intervals starting at 0.5 and -0.5 respectively with a positive (blue) change indicating an increase in anti-clockwise flow while negative (red) is an increase in clockwise flow. Note the different colour bar for panel (e).

447 representation with such surface forcing compared to the idealised Campin and Goosse
 448 (1999) case, lowers the impact of the scheme). Further, in the default CG1999 case, the direct

449 transport of tracers downslope without a return flow leads to a change in the water mass
450 transformation opposite to that from advection (not shown). This anti-correlation may also
451 partly account for the result of Bates et al. (2012b) who found that, while CG1999 increased
452 the depth of the downslope plume in an idealised test case, it decreased the downslope speed
453 of the plume. An equivalent anti-correlation of the parameterization's downslope flow and
454 the Eulerian advection term is found for BLOBS. The movement of Lagrangian particles
455 replaces a portion of the Eulerian flow leading to a near zero change in tracers and density in
456 the south. A reduction in the vertical diffusion component through applying MIXD is also
457 observed. However, the partial convective mixing of MIXD does not counteract the vertical
458 diffusion to the same degree as the BLOBS does to advection.

459 The different response of the model to MIXD and the resulting increased sensitivity of
460 AABW and NADW indicates the partial convective mixing is the most efficient of the three
461 processes based on CG1999 at transporting dense water down slope. This result corroborates
462 the non-trivial impact of MIXD found the North Atlantic by Palter et al. (2014). Hence,
463 due to the similarity of the CG1999, OVER and MIXD schemes and the minimal response
464 produced by CG1999 and OVER for all the parameter choices given in Table 1, only results
465 of the MIXD sensitivity analysis to changes in parameters will be presented along with
466 SIGMA and BLOBS.

467 Some analysis of other regions of deep water formation was also undertaken. For example,
468 within the Labrador Sea, the BLOBS leads to a decrease in transport of Labrador Sea Water
469 (based on the transport within density layers at the expected Labrador Sea Water depths)
470 out of the Labrador Sea (7% of CTR). MIXD is found to increase transport into the region
471 (43% greater than CTR) and also decreases the transport out (59% of CTR). However, the
472 production of Lagrangian particles and the application of MIXD within the Labrador Sea
473 itself makes any correlation between the Nordic Sea overflows and the Labrador Sea currents
474 and convection (Zhang et al., 2011) impossible to distinguish. Since we are interested in the
475 overall NADW and AABW properties, further work into such deep water formation regions
476 as the Labrador Sea is beyond the scope of this paper.

4.3. MIXD Parameter Sensitivity

We now investigate the sensitivity of AABW and NADW to MIXD with the various parameter choices given in Table 1. The greatest change caused from applying MIXD, compared to CTR, occurs when more grid cells are applied to the downslope flow (n ; blue line; Figure 10) and further again when the most distant points are weighted for enhanced downslope flow ($weight$; green line; Figure 10). Both cases lead to denser (by a maximum of 0.015 kg m^{-3} compared to default MIXD and 0.027 kg m^{-3} compared to CTR) and younger (by 125 years; 15% compared to default MIXD and 525 years; 63% compared to CTR) waters penetrating deeper in the north, with minimal change occurring at the surface for each parameter variation. These results are consistent with expectations, as increasing n increases the number of instances where MIXD is activated, while $weight$ enhances the transport to greatest depths.

Increasing the fraction of the grid cell participating in the overflow (δ ; Equation 2.1.2) also increases the density and decreases age in the north compared to the default MIXD (also expected, as increasing δ allows a greater volume of water to participate in the overflow) but with minimal response in the south. The greatest response in the south occurs again for $weight$, increasing density and decreasing age by 0.0075 kg m^{-3} and 60 years (15%) respectively compared to default MIXD. There is little sensitivity to the salinity in the south (<10% change compared to the north), however cooler waters are produced in the south by the parameter changes.

For the change in MOC from CTR for each parameter change in MIXD (Table 1), only the *mask* case (Figure 11a) shows negligible change (<0.05 Sv) of the NADW cell from the default MIXD (Figure 9d). We remind the reader that the *mask* case only applies the MIXD scheme south of the equator. The *mask* case does, however, indicate that the NADW and AABW cell changes are uncorrelated in this case with similar change produced in the anti-clockwise AABW cell when compared to the default MIXD case. Also, there are approximately equivalent changes in the deep south region for the *mask* case and the default MIXD (Figure 10), hence the effects of each parameter change on the defined south region may be considered approximately independent of the changes in the NADW flow.

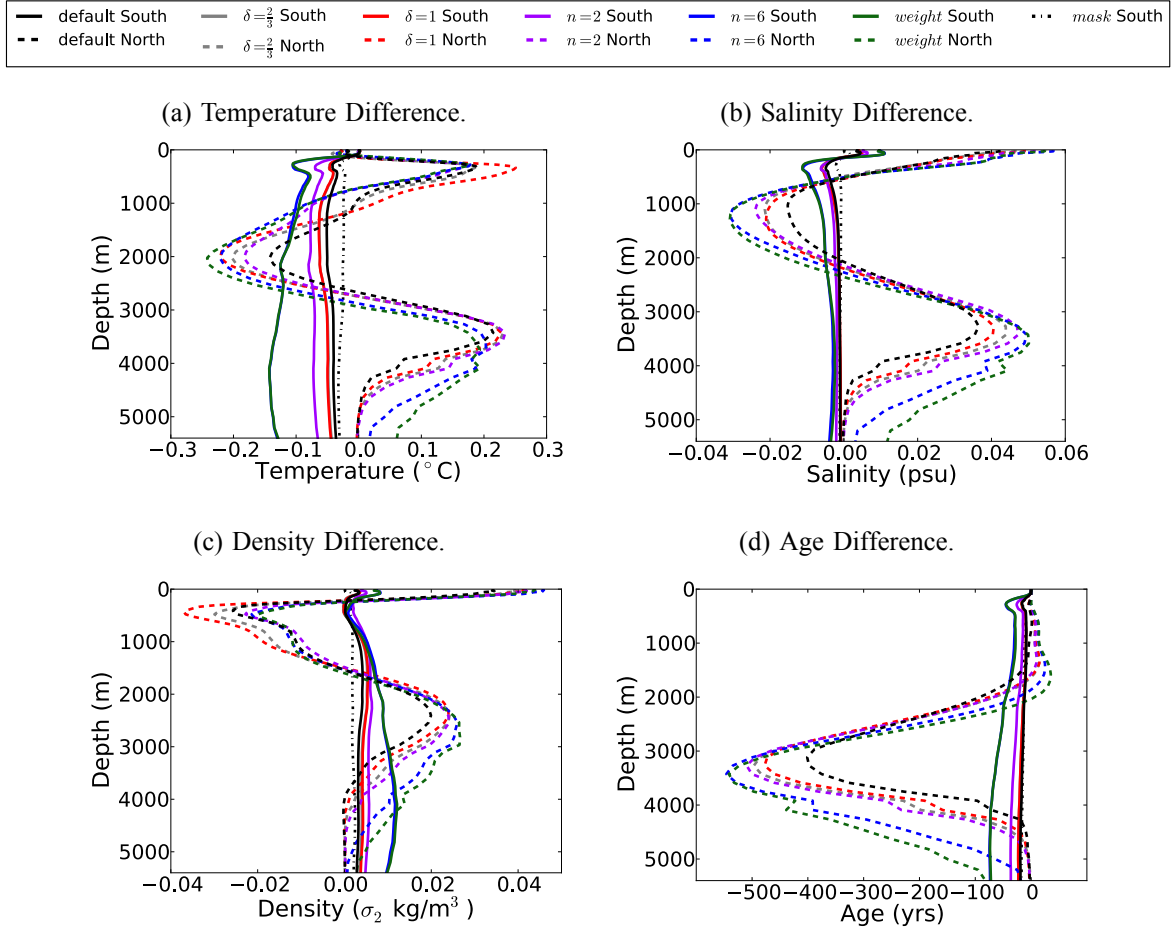


Figure 10: MIXD difference from CTR in (a) temperature ($^{\circ}\text{C}$), (b) salinity (psu), (c) density (kg m^{-3}) and (d) age (years) averaged over the region 32.4°N - 62.4°N (dashed lines) and 44.7°S - 74.7°S (solid lines) versus depth for each of the different parameter changes of MIXD. The difference is defined as the time average of the last 20 years in the overflow scheme runs minus the equivalent of the CTR.

506 All other parameter changes lead to the NADW becoming denser at the lower edge of
 507 the clockwise cell (Figure 11) compared to the default MIXD (Figure 9d). Increasing n
 508 and applying *weight* again maximise the NADW cell MOC response and leads to a slight
 509 enhancement in the anti-clockwise AABW cell, though overall the AABW cell is less sensitive
 510 to the parameter changes.

511 The net transport shows an overall marginal increase in the maximum of the AABW cell
 512 at 30°S by up to 14%, while the increase in density of the NADW cells leads to an overall

Run	AABW – CTR (Sv)	NADW – CTR (Sv)
CG1999 (default)	0.004 (↑ 0.2%)	-0.004 (↓ 0.1%)
OVER (default)	0.01 (↑ 0.5%)	0.01 (↑ 0.3%)
MIXD (default)	0.21 (↑ 10%)	-0.12 (↓ 3%)
MIXD (<i>mask</i>)	0.16 (↑ 7%)	-0.01 (↓ 0.3%)
MIXD ($\delta = \frac{2}{3}$)	0.21 (↑ 10%)	-0.15 (↓ 4%)
MIXD ($\delta = 0.1$)	0.25 (↑ 11%)	-0.20 (↓ 6%)
MIXD ($n = 2$)	0.30 (↑ 14%)	-0.11 (↓ 3%)
MIXD ($n = 6$)	0.30 (↑ 14%)	-0.11 (↓ 3%)
MIXD (<i>weight</i>)	0.22 (↑ 10%)	-0.11 (↓ 3%)

Table 4: Difference from CTR of AABW and NADW transport (defined as the maximum and minimum transport for $\sigma_2 > 36.6 \text{ kg m}^{-3}$ at 30°S and 30°N respectively) for each MIXD parameter sensitivity runs as well the default CG1999 and OVER for comparison. Note the different scale of the horizontal axes to Figure 8.

513 decrease in the maximum NADW transport (Table 4). The transport of CG1999 and OVER
514 is also included in Table 4 for comparison, however, due to the fundamental similarity of the
515 schemes and the minimal change of CG1999 and OVER, we only present the comprehensive
516 results for MIXD.

517 4.4. SIGMA Parameter Sensitivity

518 Insignificant changes ($< 1\%$) from the default SIGMA are found in the tracer properties
519 (Figure 12) and MOC (Figure 13a and 13b compared to Figure 9c) for variations in κ_σ^{ratio} .
520 This lack of sensitivity to κ_σ^{ratio} indicates that an increase or decrease of the flow that does
521 not enhance the dense downslope transport has little influence on the actual downslope
522 transport of the dense waters. Applying a constant diffusivity is found to produce the
523 largest change in tracers (blue line; Figure 12) and MOC (Figure 13c) compared to the
524 default, effectively decreasing the scheme’s impact (by approximately 50%) on density, age
525 and the NADW cell. This result agrees with Tang and Roberts (2005) who investigated
526 SIGMA in the North Atlantic and found the inclusion of an advective component (in our
527 case the velocity dependent diffusion) increased the dense downslope flow. In contrast,
528 Döscher and Beckmann (2000) found minimal change with the inclusion of an advective
529 term; however, they use a diffusion coefficient of $10^4 \text{ m}^2 \text{ s}^{-1}$ in the constant diffusion case,

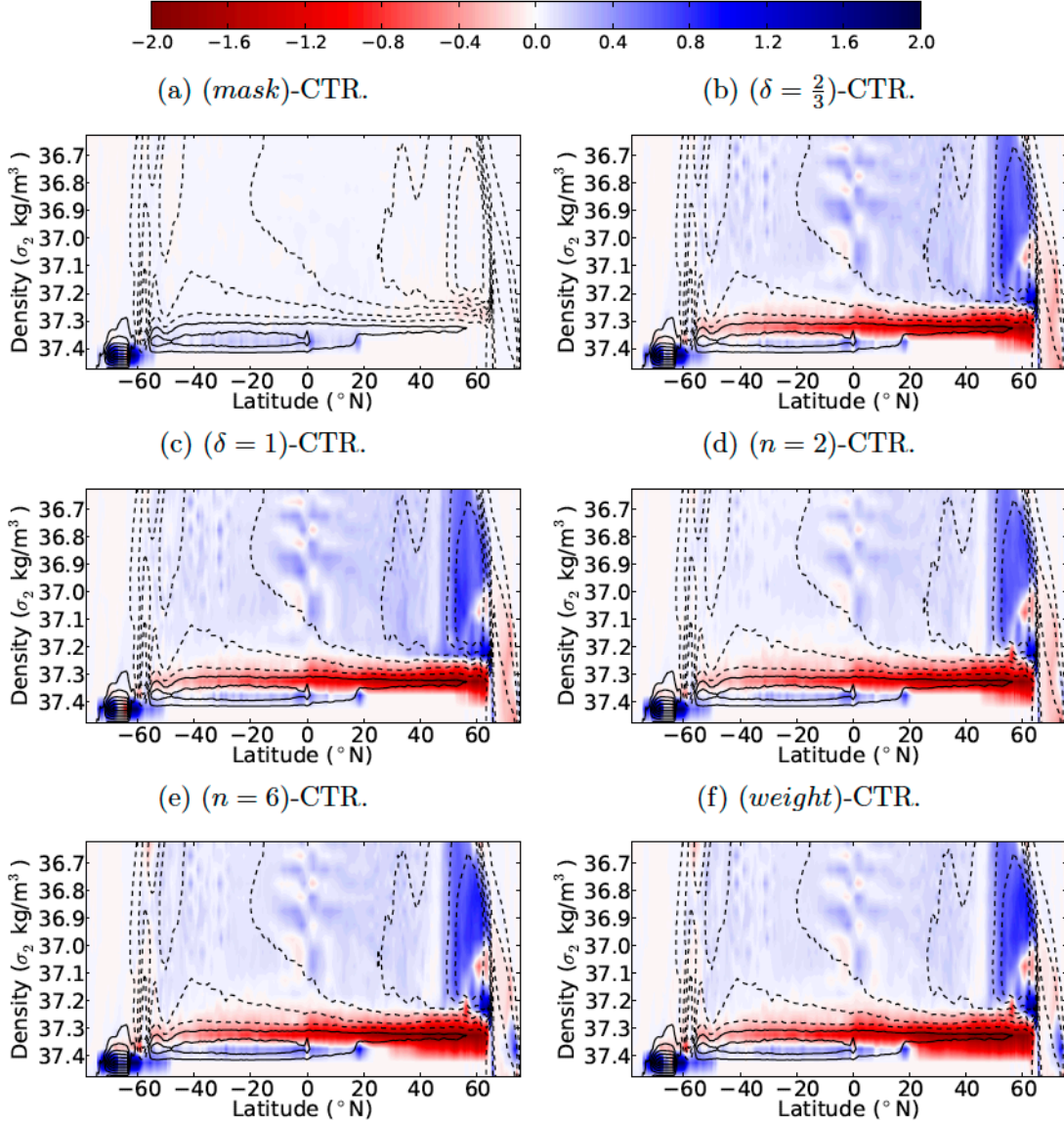


Figure 11: Difference in meridional overturning (Sv) of MIXD from the CTR in potential density space referenced to 2000 m (σ_2) for the cases (a) *mask*, (b) $\delta = \frac{2}{3}$, (c) $\delta = 1$, (d) $n = 2$, (e) $n = 6$ and (f) *weight* taken as a time mean from years 180-200 in the parameter runs. The contours represent the mean overturning of CTR in this period with solid contours indicating anti-clockwise overturning and dashed clockwise at unit intervals starting at 0.5 and -0.5 respectively.

530 while Tang and Roberts (2005) used $10^3 \text{ m}^2 \text{ s}^{-1}$.

531 Döscher and Beckmann (2000) also indicate SIGMA produces a deepening of the upper
 532 NADW cell, increasing the depth of the MOC 0 Sv streamfunction below the NADW cell

Run	AABW – CTR (Sv)	NADW – CTR (Sv)
SIGMA (default)	0.01 (↑ 0.5%)	0.02 (↑ 1%)
SIGMA ($\kappa_\sigma^{ratio} = 10^{-4}$)	0.01 (↑ 0.5%)	0.02 (↑ 1%)
SIGMA ($\kappa_\sigma^{ratio} = 10^{-8}$)	0.01 (↑ 0.5%)	0.02 (↑ 1%)
SIGMA ($\kappa_\sigma = const$)	0.01 (↑ 0.5%)	0.01 (↑ 0.3%)

Table 5: Difference from CTR of AABW and NADW transport (defined as the maximum/minimum transport for $\sigma_2 > 36.6 \text{ kg m}^{-3}$ at 30°S and 30°N respectively) for each SIGMA parameter sensitivity runs.

533 from 1800 m to 2700 m. Our results do not replicate this result, again potentially due to the
534 different diffusion coefficients, with no noticeable change (less than 50 m) in the depth of
535 the MOC zero streamfunction compared to CTR (Figure 5b). Overall, insignificant ($\leq 1\%$)
536 change occurs for the AABW and NADW transport (Table 5). One main disadvantage of
537 SIGMA is that the scheme is limited to the bottom grid cells. Such a limit means dense water
538 descending to a neutral buoyancy depth, rather than the ocean bottom, are not represented
539 and may be reducing the scheme’s overall response.

540 4.5. BLOBS Parameter Sensitivity

541 The BLOBS scheme is computationally expensive compared to the other schemes, re-
542 quiring $4.8\times$ the runtime of CTR for the default BLOBS case. The *less* case is the least
543 computationally expensive of the BLOBS sensitivity runs ($2.5\times$ the runtime of CTR), due
544 to the runtime dependence on the number of active Lagrangian particle (Bates, 2011). This
545 computational expense is higher than expected (Bates, 2011), however recent code alter-
546 ations (Appendix A) and the application of BLOBS in a realistic bathymetry may have
547 influenced the runtime as well as the large number of active particles (order 10^5).

548 Parameter variations increasing/decreasing detrainment or entrainment produce minimal
549 change to AABW and NADW properties and circulation (results overlap or are close to
550 the default case of Figure 14). This low sensitivity is a consequence of the detrainment
551 influencing the Lagrangian particles mass by only 0.0001% and entrainment by 0.1%. Due
552 to the similarity of these results to the default BLOBS case, they are not included in the
553 following figures and discussion.

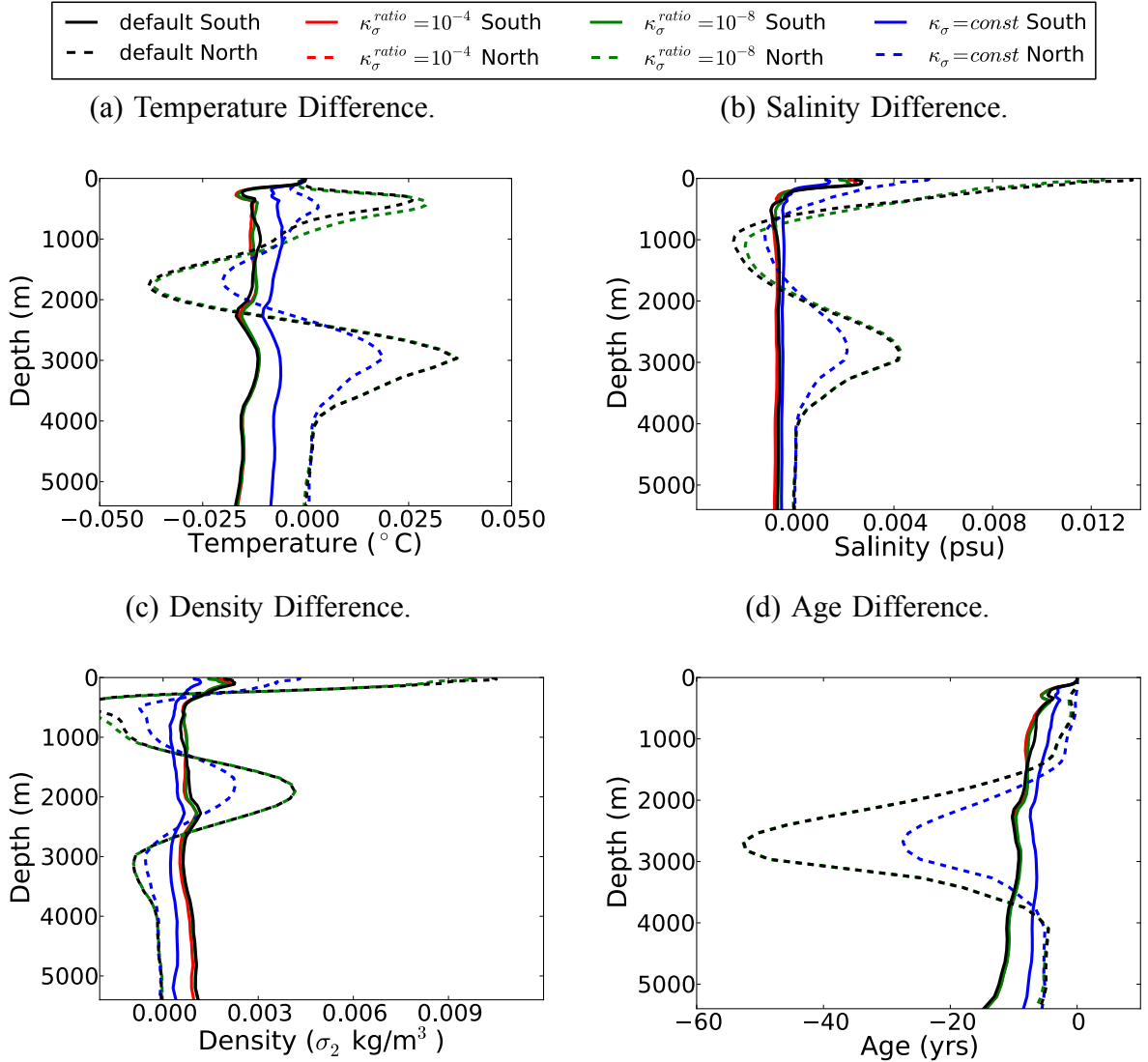


Figure 12: SIGMA difference from the CTR in (a) temperature ($^{\circ}\text{C}$), (b) salinity (psu), (c) density (kg m^{-3}) and (d) age (years) averaged over the region 32.4°N - 62.4°N (dashed lines) and 44.7°S - 74.7°S (solid lines) versus depth for each of the different parameter changes of SIGMA. The difference is defined as the time average of the last 20 years in the overflow scheme runs minus the equivalent of the CTR. Note the different scale of the horizontal axes to Figure 8 and 10 in order to highlight the structure of the SIGMA scheme results.

554 AABW shows minimal sensitivity to the BLOBS scheme despite the range of parameters
 555 explored. Increasing bottom drag produces the greatest change to density in the south
 556 (Figure 14), increasing density by a maximum of 0.0016 kg m^{-3} compared to CTR (6% the

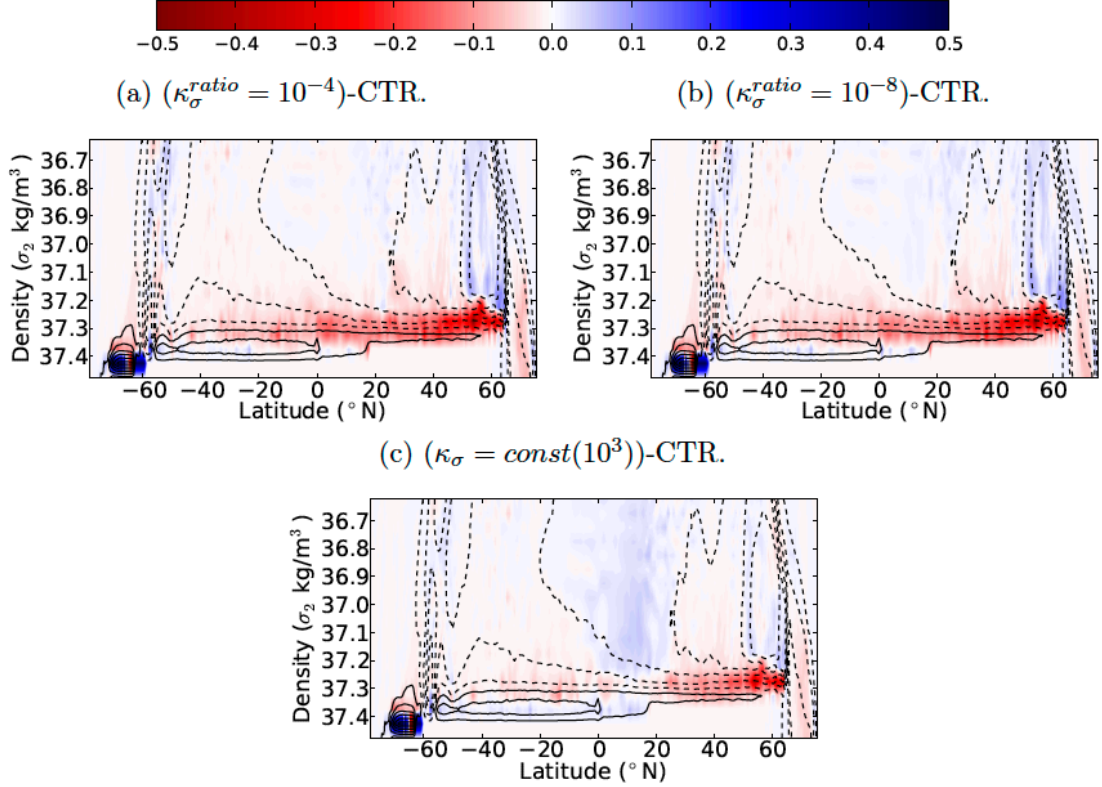


Figure 13: Difference in meridional overturning (Sv) of SIGMA from CTR in potential density space referenced to 2000 m (σ_2) for the cases (a) $\kappa_\sigma^{ratio} = 10^{-4}$, (b) $\kappa_\sigma^{ratio} = 10^{-8}$ and (c) $\kappa_\sigma = const$ taken as a time mean from years 180-200 in the parameter runs. The contours represent the mean overturning of the CTR case during the same time period with solid contours indicating anti-clockwise overturning and dashed clockwise at unit intervals starting at 0.5 and -0.5 respectively.

557 change produced from MIXD *weight*). Higher bottom drag acts to slow particles (Bates,
 558 2011) and flow non-geostrophically (Bates et al., 2012b). Such non-geostrophic flow allows
 559 particles to flow directly downslope and reach deeper depths providing the greatest increase
 560 in density below 2500 m. The maximum age decrease is 24 years compared to CTR (4%
 561 the change from MIXD *weight*) and occurs for the default and $4\beta_{0b}$. All other values show
 562 negligible change in the south compared to the default BLOBS (less than 0.0003 kg m^{-3}
 563 change in density and less than 20 years (3%) change in age). Minimal change is also observed
 564 in the lower cell of the overturning circulation (Figure 15) with the largest difference in
 565 AABW strength compared to CTR being less than 1% (Table 6).

566 In the north, increasing bottom drag (grey in Figure 14) leads to dense water descending
 567 to greater depth, with the maximum change from CTR (0.005 kg m^{-3}) at 2200 m. Decreasing
 568 the bottom drag to $C_d = 3 \times 10^{-4}$ (red in Figure 14) increases the speed of the Lagrangian
 569 particles (Bates et al., 2012b) but does not influence the particle trajectories (they continue
 570 to flow mainly geostrophically along the slope). The faster particles lead to cooler and
 571 fresher NADW compared to the default BLOBS with little change in density. Similar results
 572 to the default BLOBS occurs when fewer particles are formed (*less* case; magenta in Figure
 573 14). This indicates that the key overflow processes are captured when only considering
 574 steep slopes (>8 cells deep) and large density variations on the slope ($>0.016 \text{ kg m}^{-3}$).
 575 Increasing the number of particles formed (*more* case; green in Figure 14) however increases
 576 the transport of warm salty water to depth. The combined influence of the tracers decreases
 577 the density at the maximum by 0.0006 kg m^{-3} with a decrease in age of 15 years compared
 578 to the default BLOBS.

579 Increasing/decreasing the Lagrangian particles size (yellow/blue lines respectively in Fig-
 580 ure 14) increases/decreases the impact of the BLOBS scheme. The $4\beta_{0b}$ case produces for
 581 the greatest increase in density (maximum change below 1000 m of 0.0096 kg m^{-3}) and de-
 582 crease in age (maximum change 115 years) in the north of all the BLOBS parameter regimes
 583 considered. Such changes are 36% the density change and 22% the age change produced by
 584 MIXD *weight* in the north.

585 The change from CTR in the upper cell circulation (Figure 15) shows similar character-
 586 istics for all BLOBS cases, producing an increase in the circulation of the densest portion
 587 of the cell with a decrease in the streamfunction above. The $4\beta_{0b}$ case, as with the tracer
 588 properties, imparts the greatest impact, leading to a maximum change in the upper cell of
 589 0.7 Sv . As with MIXD however, the increase in the densest part of the NADW cell leads to
 590 a reduction in the calculated NADW maximum at 30°N (decreasing it by 1% for the $4\beta_{0b}$
 591 case; Table 6).

592 While our study focusses on water mass properties, some regard of the importance of
 593 reproducing the correct overflow pathways should be considered. BLOBS is the only scheme
 594 dynamically defining the descent path of AABW and NADW. All other schemes move dense

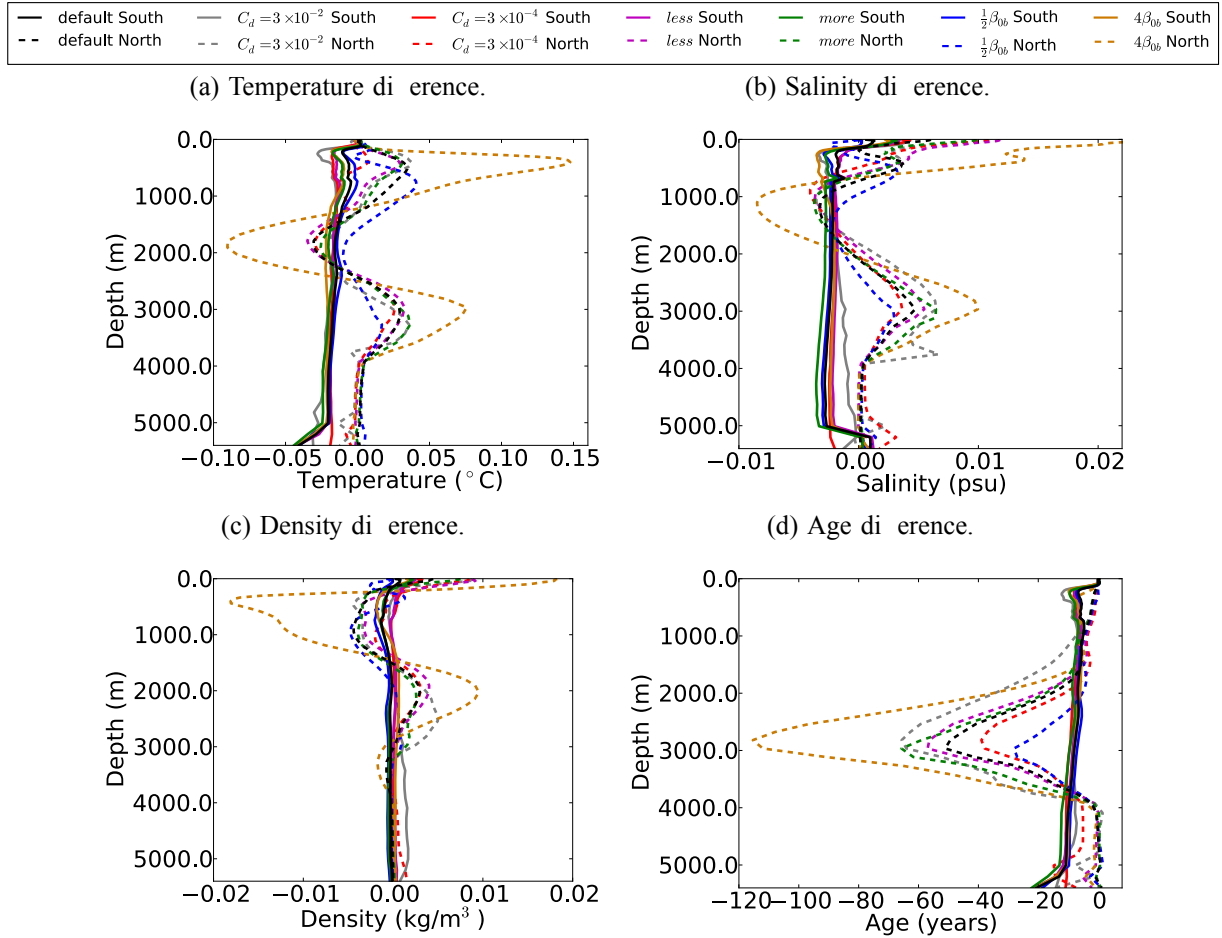


Figure 14: BLOBS difference from the CTR in (a) temperature ($^{\circ}\text{C}$), (b) salinity (psu), (c) density (kg m^{-3}) and (d) age (years) in the region 32.4°N - 62.4°N (dashed lines) and 44.7°S - 74.7°S (solid lines) versus depth for each of the different parameter changes of BLOBS. The difference is defined as the time average of the last 20 years in the overflow scheme runs minus the equivalent of the CTR. Note the different scale of the horizontal axes to Figure 8, 10 and 12 in order to highlight the structure of the BLOBS scheme results.

595 water unphysically straight downslope without consideration of Coriolis forces. That is,
 596 while BLOBS dynamically controls the descent of dense water, MIXD moves dense water
 597 directly downslope dispersing it throughout the deep ocean. Figure 16 illustrates this point
 598 where we see the change in temperature from CTR after 200 years on the bottom grid cells
 599 for BLOBS and MIXD. MIXD leads to cooler water dispersed across the Weddell Sea while
 600 BLOBS controls the flow of cold dense water along the overflow pathways. The way MIXD
 601 disperses dense water over a large area while BLOBS confines it to its dynamical pathway,

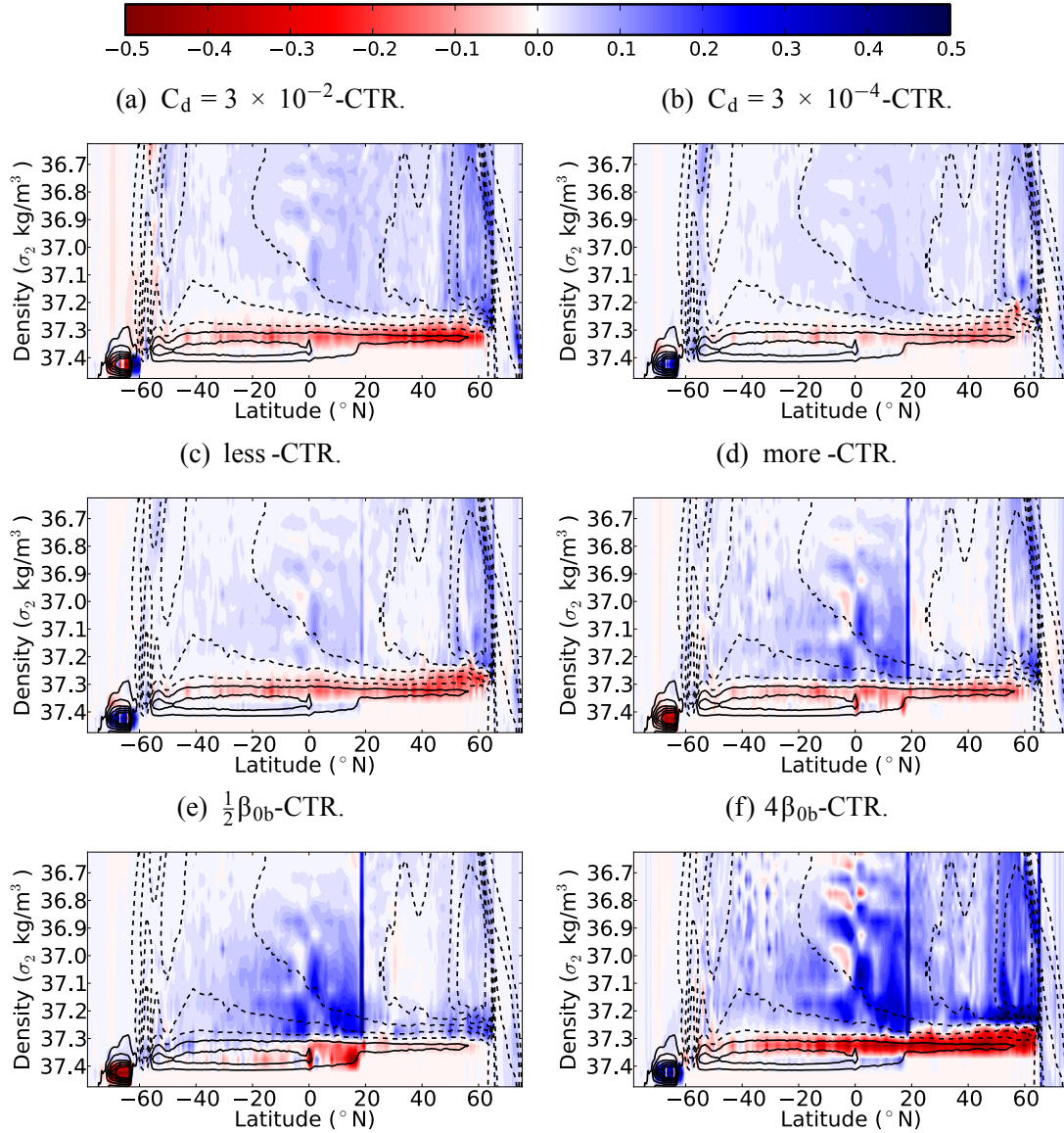


Figure 15: Difference in meridional overturning (Sv) of BLOBS from CTR in potential density space referenced to 2000 m (σ_2) for the cases (a) where $C_d = 3 \times 10^{-2}$, (b) $C_d = 3 \times 10^{-4}$, (c) *less*, (d) *more*, (e) $\frac{1}{2}\beta_{0b}$ and (f) $4\beta_{0b}$ taken as a time mean from years 180-200 in the parameter runs. The contours represent the mean overturning of the CTR case during the same time period with solid contours indicating anti-clockwise overturning and dashed clockwise at unit intervals starting at 0.5 and -0.5 respectively.

602 is likely one factor leading to MIXD producing the largest impact, while BLOBS is more
 603 suitably designed for influencing deep flows within straits and passages.

Run	AABW – CTR (Sv)	NADW – CTR (Sv)
BLOBS (default)	0.017 (\uparrow 0.8%)	-0.024 (\downarrow 0.7%)
BLOBS ($4\beta_{0b}$)	0.014 (\uparrow 0.6%)	-0.04 (\downarrow 1.1%)
BLOBS ($0.5\beta_{0b}$)	-0.006 (\downarrow 0.3%)	-0.03 (\downarrow 0.9%)
BLOBS ($C_d = 3 \times 10^{-2}$)	-0.027 (\downarrow 1.2%)	-0.017 (\downarrow 0.5%)
BLOBS ($C_d = 3 \times 10^{-4}$)	0.011 (\uparrow 0.5%)	-0.012 (\downarrow 0.3%)
BLOBS (<i>more</i>)	0.003 (\uparrow 0.1%)	-0.005 (\downarrow 0.1%)
BLOBS (<i>less</i>)	0.017 (\uparrow 0.8%)	-0.0004 (\downarrow 0.0%)

Table 6: Difference from CTR of AABW and NADW transport (defined as the maximum/minimum transport for $\sigma_2 > 36.6 \text{ kg m}^{-3}$ at 30°S and 30°N respectively) for each BLOBS parameter sensitivity runs.

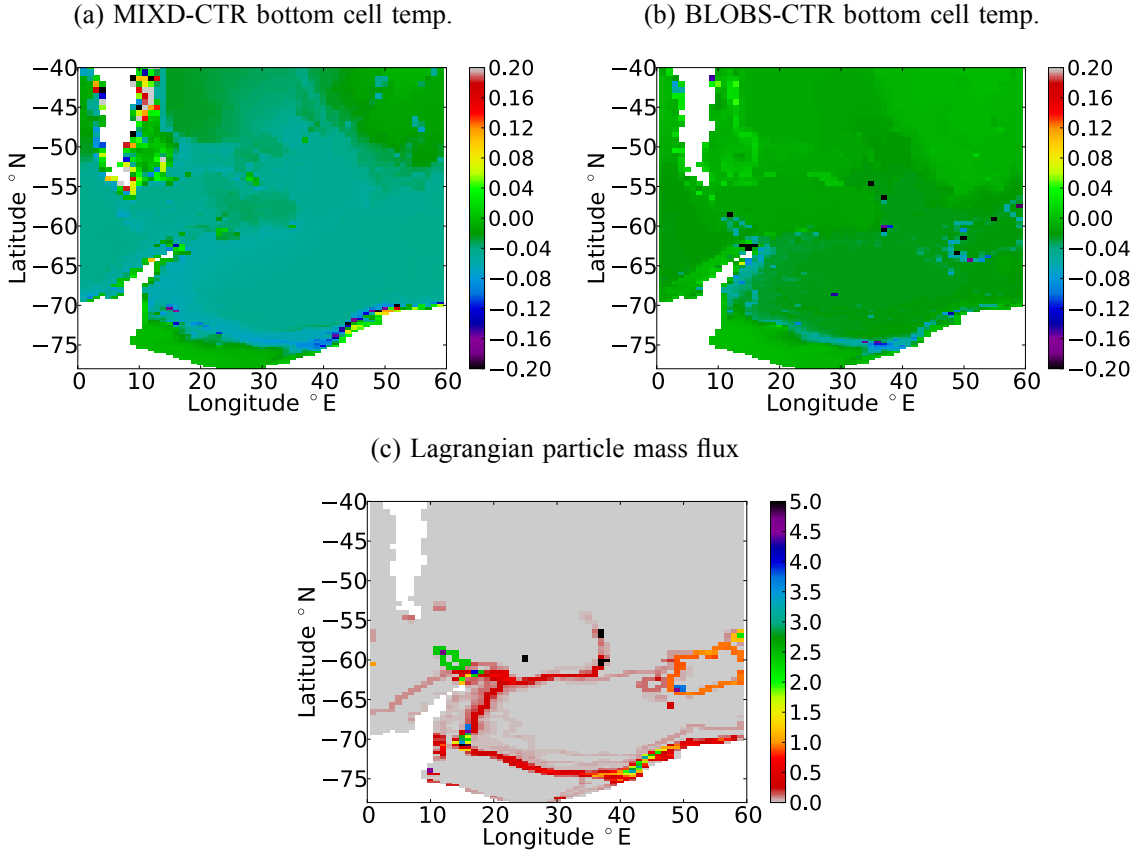


Figure 16: Difference from CTR in bottom grid cell temperature ($^\circ\text{C}$) at year 200 for (a) default MIXD and (b) default BLOBS case with (c) the Lagrangian particle mass flux ($1 \times 10^{14} \text{ kg/s}$) entering a grid cell for the default BLOBS case over year 200. Note that we only show the mass flux into the grid cell not also the mass flux out of a grid cell. This is done in order to make the Lagrangian particle paths clearer.

604 5. Conclusions

605 Many commonly used ocean climate models struggle to represent or parameterize the
606 observed AABW and NADW deep water properties. The application of overflow parameter-
607 izations seeks to improve the representation of these water masses. Many parameterizations
608 are successful at improving northern dense water flow, however those tested here are unable
609 to provide an equivalent sensitivity in the south.

610 MIXD (and in turn CG1999, OVER) and SIGMA overflow schemes only consider the
611 tracer equation in their adjustment. The fully dynamical scheme of BLOBS on the other
612 hand was designed to provide a more complete representation of overflow processes. The
613 large NADW response provided by MIXD indicates that adjustment through dynamical
614 factors such as the effects of the momentum of the water parcel, are not necessary for the
615 overflow parameterization to enhance northern downslope flow. The computational cost of
616 BLOBS compared to MIXD further makes BLOBS unviable for current GCM application,
617 while MIXD is already suitably implemented in some GCMs. However, while our study
618 assessed the sensitivity of AABW and NADW water mass properties, some consideration of
619 overflow pathways may be important, with accurate pathways only represented through the
620 dynamical BLOBS scheme.

621 The maximum response in the south (via the *weight* MIXD set-up) shows the compara-
622 ble sensitivity of AABW to NADW is always less than 1/3 when considering the vertically
623 integrated tracer and density changes. The reduced response from any parameterization in
624 the south implies that the characteristics of AABW overflows cannot be substantially im-
625 proved through the application of the existing overflow parameterizations investigated here.
626 This lack of sensitivity may result from the differing characteristics of the AABW overflows.
627 AABW overflows are more dispersed than NADW overflows and are likely less well resolved
628 across the shelf and slope. The dispersed nature of AABW also makes alternative schemes
629 not tested here, such as the POP overflow parameterization (Danabasoglu et al., 2010) po-
630 tentially difficult to implement for AABW. Alternative approaches need to be considered
631 (e.g. investigation into the shelf water properties or implementation of a dynamical pip-

632 ing scheme in BLOBS that reduces its influence on the Eulerian model), if progress into
633 improving AABW properties in z -coordinate GCMs is to be achieved.

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641 viewers for their efforts and thoughtful comments.

642 **Appendix A. BLOBS code in MOM5 distribution**

643 A slight omission in the code of the MOM5 distribution was discovered during recent
644 testing of the BLOBS. This error meant that ocean sea surface height (SSH) contributions
645 from the Lagrangian particle mass was not taken into account during the fast barotropic
646 time step of the ocean model and led to abnormally large SSH (up to ± 30 m). These
647 large SSH anomalies occurred in concentrated Lagrangian particle formation regions on the
648 shelf and produced a strong barotropic flow off the shelf. Such flow off the shelf led to an
649 unphysical increase in dense water transport and circulation. Updating the MOM5 code
650 to include the Lagrangian particles within the barotropic time step led to no significant
651 change in the presented dye concentration results of the DOME test case of Bates et al.
652 (2012b) since these results were presented after only 28 days of simulation. For the BOWL
653 test case, however, results after one year proved long enough for the SSH anomaly to build
654 and significantly alter the magnitude of the presented barotropic quasi-streamfunction. The
655 updated streamfunction and bottom temperature results for the BLOBS “ctrl” case of (Bates
656 et al., 2012b) (Figure A.17) shows an overall increase in the quasi-barotropic streamfunction,
657 however of order 220 Sv rather than 1200 Sv. This streamfunction illustrates a greater

658 increase in circulation compared to all other overflow parameterizations cases of (Bates
 659 et al., 2012b) except the no return flow (Campin and Goosse, 1999) case which produces a
 660 barotropic quasi-streamfunction of order 250 Sv.

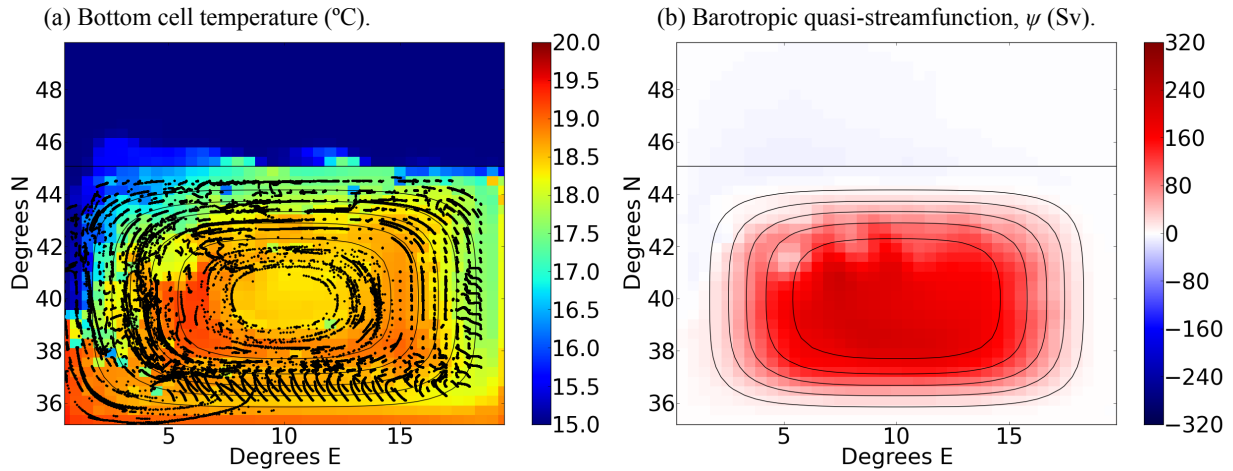


Figure A.17: (a) Bottom cell temperature (°C) and (b) barotropic quasi-streamfunction (Sv) of the “ctrl” bowl case of (Bates et al., 2012b) after one year, applying the updated MOM5 code. The black dots of (a) show the locations of the Lagrangian particles over the one year simulation.

661 Appendix B. Frazil Ice Parameterization

662 Both linear and non-linear equations may be used to define to frazil ice formation in
 663 MOM5. The linear equation computes the freezing temperature of sea water (T_f) as a linear
 664 function of salinity (S);

$$T_f = a_1 S, \quad (\text{B.1})$$

665 where a_1 is a constant (Griffies, 2012). The non-linear form instead determines T_f as a
 666 nonlinear function of salinity and gauge pressure (p);

$$T_f = \frac{a_0 + S(a_1 + \sqrt{S}(a_2 + \sqrt{S}a_3)) + p(a_4 + p(a_5 + Sa_6))}{b_0 + p(b_1 + pb_2) + S^{\frac{5}{2}}b_3}, \quad (\text{B.2})$$

667 where $a_0, a_1, a_2, a_3, a_4, a_5, a_6, b_0, b_1, b_2$ and b_3 are constants (Jackett et al., 2006). To test the
668 two forms of T_f , the model and set-up defined in Section 3.1 and 3.2 was used at $\frac{1}{4}^\circ$ resolution
669 and without the application of the Gent and McWilliams (1990) eddy parameterization. The
670 model is run for 280 yrs with the non-linear equation defining frazil formation applied. Two
671 runs are then performed for 15 yrs, one with the linear form (Equation B.1) and the other
672 continuing the non-linear form (Equation B.2). After 15 yrs, the non-linear forms leads to
673 a significant increase in ice mass compared to the linear case (Figure B.18d) and is most
674 pronounced in the southern hemisphere. The non-linear form also produces cooler and saltier
675 waters on the southern shelf, resulting in an overall increase in density on the Antarctic shelf
676 by up to 0.05 kg m^{-3} (Figure B.18).

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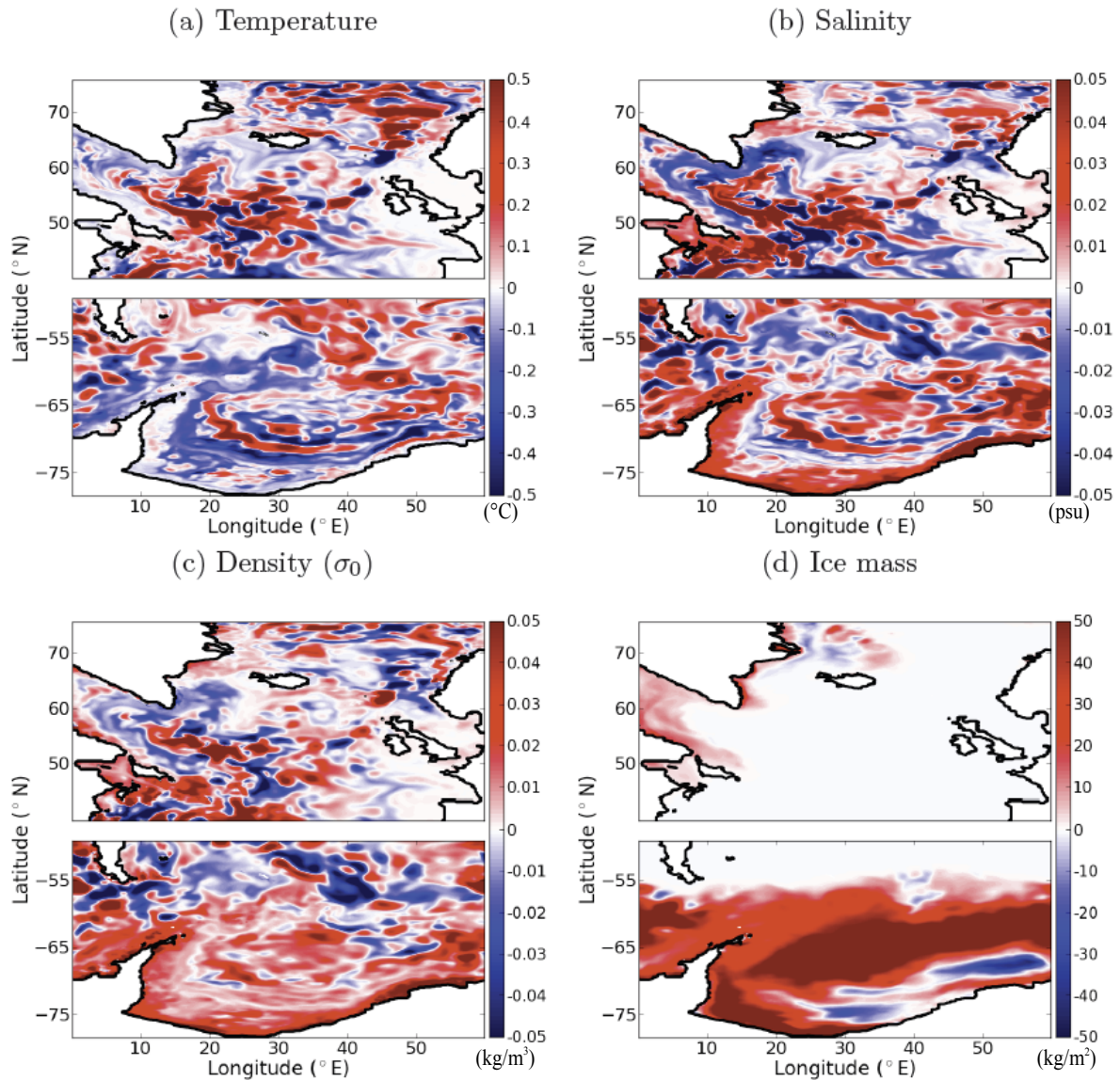


Figure B.18: Yearly mean difference in applying a non-linear to linear equation for defining the freezing temperature of seawater for frazil formation for (a) temperature ($^{\circ}\text{C}$), (b) salinity (psu), (c) potential density referenced to 0 m (σ_0 ; kg m^{-3}) and (d) ice mass (kg m^{-2}). Temperature, salinity and density are depth averaged on the shelf for values above 1300 m.

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