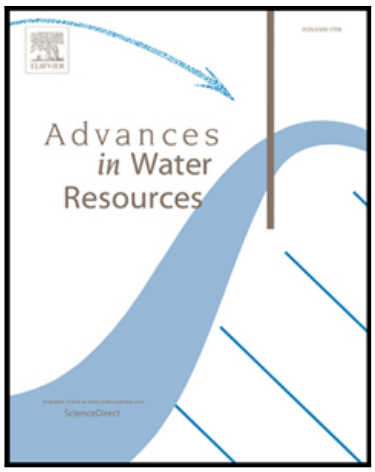

Pore-scale modeling of capillary trapping in water-wet porous media: A new cooperative pore-body filling model

L.C. Ruspini, R. Farokhpoor, P.E. Øren

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Highlights

- A new model for cooperative pore body filling displacement is proposed.
- Capillary trapping is strongly influenced by the interaction between different displacement mechanisms.
- Image-based pore networks from micro-CT scans are used in order to study capillary trapping in water-wet rocks.
- A good agreement between experimental and simulated results is found using the proposed model.

Pore-scale modeling of capillary trapping in water-wet porous media: A new cooperative pore-body filling model

L.C. Ruspini[a,1], R. Farokhpoor[a], P.E. Øren[b]

[a] *Thermo Fisher Scientific*
[b] *Australian National University*

Abstract

We present a pore-network model study of capillary trapping in water-wet porous media. The amount and distribution of trapped non-wetting phase is determined by the competition between two trapping mechanisms - snap-off and cooperative pore-body filling. We develop a new model to describe the pore-body filling mechanism in geologically realistic pore-networks. The model accounts for the geometrical characteristics of the pore, the spatial location of the connecting throats and the local fluid topology at the time of the displacement. We validate the model by comparing computed capillary trapping curves with published data for four different water-wet rocks. Computations are performed on pore-networks extracted from micro-CT images and process-based reconstructions of the actual rocks used in the experiments. Compared with commonly used stochastic models, the new model describes more accurately the experimental measurements, especially for well connected porous systems where trapping is controlled by subtleties of the pore structure. The new model successfully predicts relative permeabilities and residual saturation for Bentheimer sandstone using *in-situ* measured contact angles as input to the simulations. The simulated trapped cluster size distributions are compared with predictions from percolation theory.

Keywords: porous media, two-phase flow, capillary trapping, residual saturation, pore-network simulation, cooperative pore-body filling

[1] email: leonardo.ruspini@fei.com

1. Introduction

Multiphase flow in geological porous media is of great theoretical and practical interest in many fields of technology. Important industrial applications include geological sequestration of carbon dioxide (CO_2), remediation of non-aqueous phase liquid (NAPL) contaminants in soil and the extraction of hydrocarbons from petroleum bearing reservoirs. At the macroscopic scale, the complex physics of multiphase flow are usually described using mass balance equations for the fluids and invoking Darcy-type formulations for constitutive relationships such as relative permeability and capillary pressure Bear (1988); Lake (1989). These relationships are a manifestation of the underlying pore-scale processes and depend on the micro-structure of the porous medium and the physical characteristics of the solid and the fluids that occupy the pore space Øren & Bakke (2003); Andrew et al. (2014a). There is therefore significant interest in pore-scale investigations aimed at computing physically-based effective properties that can be used to inform larger scale continuum models.

Capillary trapping of residual non-wetting phase (*nwp*) is of great importance to the efficiency of hydrocarbon recovery processes and is a key mechanism in long-term CO_2 geo-sequestration. In hydrocarbon recovery and in remediation processes, a minimal residual *nwp* saturation is optimal while in storage, the aim is to maximize the magnitude of trapped CO_2. Capillary trapping is also an important contributor to hysteresis in relative permeability and capillary pressure relationships Spiteri et al. (2008); Joekar-Niasar et al. (2013). The overall amount of trapped *nwp* is governed by flowrate, wettability, pore structure and the topology of the non-wetting phase Jerauld & Salter (1990); Blunt & Scher (1995); Øren et al. (1998); Herring et al. (2013).

It is generally accepted that the amount of capillary trapping for a given rock depends on the capillary number Ca which describes the balance between viscous and capillary forces. Ca has several definitions depending on the intended application Chatzis & Morrow (1984); Hilfer & Øren (1996); Hilfer et al. (2015), but it has traditionally been defined in terms of a pore-scale force balance

$$Ca = \frac{v_i \mu_i}{\sigma} \tag{1}$$

where v_i is the invading phase velocity, μ_i is the invading phase viscosity and σ is the interfacial tension. For imbibition processes, the amount of trapped *nwp* is constant at small Ca values, but decreases sharply if the capillary number exceeds some critical value. This is due to a transition from capillary dominated to viscous dominated flow and has been demonstrated extensively both experimentally Chatzis & Morrow (1984); Morrow et al. (1988); Georgiadis et al. (2013); Armstrong et al. (2014); Khishvand et al. (2016a) and numerically Hughes & Blunt (2000); Nguyen et al. (2006); Koroteev et al. (2013); Ramstad et al. (2014). For water-wet siliciclastic rocks such as Berea, Bentheimer and Fontainebleau the critical value has been observed to be $Ca \geq 10^{-5}$ Taber (1969); Youssef et al. (2015); Khishvand et al. (2016a). This value is at least one order of magnitude larger than that encountered in most reservoir scale processes such as waterflooding and in CO_2 storage situations where the natural flow of brine may only be a few meters per year Krevor et al. (2015).

The residual *nwp* saturation depends strongly on wettability (i.e. the contact angle between the *nwp* and the solid surface). The effects of wettability on waterflood residual oil have been studied extensively in the petroleum industry. Jadhunandan and Morrow Jadhunandan & Morrow (1995) performed an extensive core-flooding study of the effects of wettability on waterflood oil recovery. They found that after injecting 20 pore volumes of brine, maximum oil recovery was achieved for weakly water-wet conditions. This has also been observed in pore-network model studies Øren & Bakke (2003); Valvatne & Blunt (2004) using a pore-level scenario for wettability alteration proposed by Kovscek et al. Kovscek & Radke (1993). In the context of CO_2 sequestration, it is generally expected that the CO_2-brine-rock system will be water-wet. This is heavily supported by core-flooding experiments Suekane et al. (2008, 2009); Pentland et al. (2011); Krevor et al. (2012); Akbarabadi & Piri (2013, 2015); Zuo & Benson (2014); Niu et al. (2015); Palamara et al. (2015), image-based characterization of the residual non-wetting phase and *in-situ* contact angle measurements using X-ray computed tomography (micro-CT) imaging techniques Armstrong et al. (2012); Andrew et al. (2014a). In addition, trapped cluster sizes have been found to obey an approximate power law distribution Favetto et al. (2010); Iglauer et al. (2011); Andrew et al. (2014b) with an exponent broadly consistent with percolation theory Geistlinger & Mohammadian (2015), confirming water-wet conditions.

The amount of trapping depends on the initial non-wetting phase saturation. For water-wet media, it is generally observed that the residual *nwp* saturation increases as the initial saturation increases Land (1968); Suzanne et al. (2003b); Pentland et al. (2010a); Niu et al. (2015). However, there is significant variation among different rocks Al-Mansoori et al. (2010). The constitutive relation between initial and residual *nwp* saturations is commonly referred to as IR (initial-residual) curve. Several empirical trapping models have been developed to describe the IR relation. The most widely used model is that of Land Land (1968). It was developed to predict the IR characteristics of water-wet sandstones. The trapped *nwp* saturation S_{nwr} is given as

$$S_{nwr} = \frac{S_{nwi}}{1 + CS_{nwi}} \tag{2}$$

where S_{nwi} is the initial *nwp* saturation and C is the Land trapping coefficient. C is usually computed from experimental or numerical S_{nwi} and S_{nwr} values. A review of commonly used trapping models is given in Joekar-Niasar et al. (2013).

Topological and geometrical properties of the pore structure have a clear effect on the overall amount of trapping. For example, the residual gas saturation in water-wet Fontainebleau sandstone varies from $S_{gr} \simeq 0.33$ to $S_{gr} \simeq 0.9$ as porosity decreases from 0.28 to 0.05 Bourbie & Zinzner (1985); Suzanne et al. (2003b). Chatzis et al. Chatzis et al. (1983) investigated capillary trapping in 2D and 3D porous materials and found that the distribution and magnitude of trapped *nwp* depends strongly on the pore-throat aspect ratio. Similar findings were reported by Al-Raoush and Wilson Al-Raoush & Wilson (2005) using micro-CT imaging to analyze the distribution of residual *nwp* in a glass bead pack. The pore structure strongly affects capillary trapping because the pore-scale mechanisms underlying trapping critically depend on topological and geometrical aspects of the pore structure.

Pore-network modeling is one of the most widely used numerical tool for studying capillary dominated two-phase flow at the pore-scale Fatt (1956a,b,c); Bryant & Blunt (1992); Øren et al. (1998); Patzek (2001); Øren & Bakke (2003); Valvatne & Blunt (2004); Ryazanov et al. (2010). The predictive capabilities of network models have improved significantly with the ability to reproduce essential geometrical and topological features of the pore space

using networks extracted from micro-CT images Lindquist & Venkatarangan (1999); Lindquist et al. (2000); Silin & Patzek (2006); Dong & Blunt (2009) or process-based reconstructions Bakke & Øren (1997); Øren & Bakke (2002, 2003). Pentland et al. Pentland et al. (2010b) successfully computed capillary trapping for an n-decane/brine system in water-wet Berea and Clashach sandstones using pore-networks extracted from micro-CT images. In order to match residual saturations, the advancing contact angle θ_a had to be tuned and was randomly distributed in the range 27^o-87^o. This is high for a strongly water-wet system. Raeini et al. Raeini et al. (2015) found that pore-network simulations with $\theta_a = 47^o$ significantly over-estimated trapping in water-wet sandpacks while direct finite volume simulations better matched the experimental data. Bondino et al. Bondino et al. (2013) reported that contact angles had to be adjusted to unrealistically high values in order to match experimentally measured residual saturations in water-wet systems. Similar findings were reported by Valvatne and Blunt Valvatne & Blunt (2004).

The failure of pore-network models to predict residual saturations for water-wet systems is typically attributed to the simplified geometry, the presence of viscous forces, or to overestimation of snap-off events Valvatne & Blunt (2004). However, predictive capabilities of pore-network models do not only depend on the ability to reproduce wettability effects and to capture essential geometrical and topological features of the pore space. They also depend on a precise characterization of the pore-scale displacement and trapping mechanisms. Pore-scale mechanisms for imbibition were first observed in two-dimensional micro-model experiments and described in the pioneering works of Lenormand et al. Lenormand et al. (1983); Lenormand & Zarcone (1984). There are three basic types of displacements: piston-like, snap-off and cooperative pore-body filling. Recently, these mechanisms have been observed in rocks using high speed synchrotron-based micro-CT Berg et al. (2013); Armstong & Berg (2013); Andrew et al. (2015).

Piston-like (PL) advance refers to the displacement of non-wetting phase from a throat by an invading interface initially located in an adjoining wetting phase filled pore-body. The invading wetting phase preferentially fills the narrowest regions of the pore space. Piston-like displacement in throats is favored while wetting phase advance is impeded by the larger pore-bodies. Piston-like advance is not a bond-breaking mechanism (i.e. local *nwp* disconnection) and it does not result in trapping of the non-wetting phase.

Snap-off (SO) refers to the invasion of a non-wetting phase filled throat by arc menisci (AM) or wetting layers initially present in corners, crevices and rough surfaces of the pore space. For small injection velocities, wetting layers will swell and thicken ahead of the bulk wetting phase invasion in pores and throats. At a critical capillary pressure, the AMs fuse and the center of the throat spontaneously fills with wetting phase Roof (1970). Snap-off is a bond-breaking mechanism that can lead to *nwp* trapping.

Cooperative pore-body filling (PBF) refers to cases where wetting phase displaces non-wetting phase from a pore-body when one or more of the connecting throats are filled with non-wetting phase. Using the terminology of Lenormand Lenormand et al. (1983), the displacement events are labeled I_n where n is the number of connecting throats filled with non-wetting phase. The I_1 is not a bond-breaking mechanism. In contrast, for $n > 1$, the I_n displacements are bond-breaking mechanisms that can lead to *nwp* trapping.

At the pore-scale, the amount and distribution of trapped *nwp* are determined by the competition between the two bond-breaking mechanisms, SO and PBF. The mechanism that actually dominates depends on pore-structure, contact angle and the topology of the non-wetting phase Øren et al. (1998); Valvatne & Blunt (2004); Herring et al. (2013). Snap-off can lead to significant trapping while PBF encourages a flat, frontal advance of the wetting phase with little trapping, at least for uniform porous media such as the micro-model experiments described by Lenormand Lenormand et al. (1983).

Fluid topology, phase connectivity and capillary entry pressures govern the order in which the wetting phase invades pores and throats Øren et al. (1998). The PL and SO mechanisms are well characterized and capillary entry pressures can be calculated from local geometrical and wetting characteristics Blunt & Scher (1995); Øren et al. (1998). In contrast, PBF depends on fluid topology and there is no exact expression for the capillary entry pressure for different I_n configurations. Typically, stochastic expressions are used to compute these entry pressures Blunt (1997); Øren et al. (1998). Clearly, this is a simplification that can limit the predictive capabilities of pore-network models, especially for rocks where PBF is an important trapping mechanism.

This paper presents a new model for the calculation of capillary entry pressures for cooperative pore-body filling. The model accounts for wetting properties, geometrical characteristics of the pore-body and the spatial locations of the connecting *nwp* filled throats. The new PBF model is implemented in a pore-network simulator described earlier Øren et al. (1998). We compute capillary trapping curves for different water-wet rocks and compare the results with experimental data. The simulated trapped cluster size distributions are compared with predictions from percolation theory.

2. Previous PBF models

Capillary entry pressure for pore-body filling is limited by the largest radius of curvature required to invade a pore-body. For a pore-body with coordination number z, there are $z-1$ possible displacements, referred to as I_1 to I_{z-1}. If only one of the connecting throats is filled with non-wetting phase, the I_1 displacement is similar to a piston-like displacement and the capillary entry pressure can be calculated from an energy balance using the Mayer, Stowe and Princen (MSP) theory Mayer & Stowe (1965); Princen (1969). However, when two or more of the adjacent throats are occupied by the non-wetting phase, the radius of curvature depends on the spatial locations of the *nwp* filled throats Lenormand et al. (1983). Blunt Blunt (1997) presented a stochastic model for the radius of curvature based on the number n of adjacent *nwp* filled throats, represented as

$$R_n = \frac{1}{\cos\theta_a}\left(r_p + \sum_{i=1}^{n} A_i x_i\right) \tag{3}$$

where x_i are random numbers between 0-1, A_i are empirical parameters ($\{0,$ 2.5, 5, 20, 100$\}$ μm), θ_a is the advancing contact angle and r_p is the pore-body radius. This model is referred to as Blunt$_1$ in the following.

Øren et al. Øren et al. (1998) presented a variation of Eq. (3) by modifying the A_i parameters to also depend on the radii of the *nwp* filled throats

$$R_n = \frac{1}{\cos\theta_a}\left(r_p + \sum_{i=1}^{n} a_i r_i x_i\right) \tag{4}$$

where the values of a_i are given by $\{0.0,$ 0.5, 1, 2, 5, 10$\}$ and r_i are the radii of the *nwp* filled throats. We refer to this model as Oren$_1$. The entry

capillary pressure is given by $Pc_n = 2\sigma/R_n$. Additional variations on the initial stochastic model can be found in the literature Patzek (2001).

To account for the possibility of negative capillary entry pressures for $\theta_a < 90^o$, Blunt Blunt (1998) proposed to define the entry capillary pressure as

$$Pc_n = \frac{2\sigma\cos(\theta)}{r_p} - \sigma\sum_{i=1}^{n} A_i x_i \tag{5}$$

where the coefficient $A_i = 1500\ \frac{1}{m}$. This model is referred to as Blunt_2. Valvatne Valvatne (2004) presented a variation of the Blunt_2 model by relating the parameter A_i to the permeability k of the pore-network

$$Pc_n = \frac{2\sigma\cos(\theta)}{r_p} - \sigma\frac{0.03}{\sqrt{k}} \tag{6}$$

This last model is referred to as Valvatne_1. No analysis of the differences between these models has been presented in the literature. As part of this work, we present a systematic comparison of the effects that the different stochastic models have on capillary trapping in water-wet rocks.

3. New PBF model

In this section we derive a new model for calculating capillary entry pressures for cooperative pore-body filling. In contrast to the stochastic PBF models described earlier, the new model accounts for the local fluid topology and the geometrical characteristics of the throats actually involved in the displacement. The model is based on the following geometrical assumptions: (i) the center-line of the throats connected to a pore-body meet in the center of the pore-body, (ii) the limiting radius of curvature is governed by the pair of *nwp* filled throats with the largest angular spacing, and (iii) the radius of curvature is calculated in the plane defined by the center-line of the two throats and the pore-body center. In the next section, we demonstrate the key steps involved in the calculations of PBF entry pressures assuming a symmetric pore-throat system, i.e. constant throat size and constant contact angle. The analysis is then extended to the general case, i.e. different throat sizes and different contact angles.

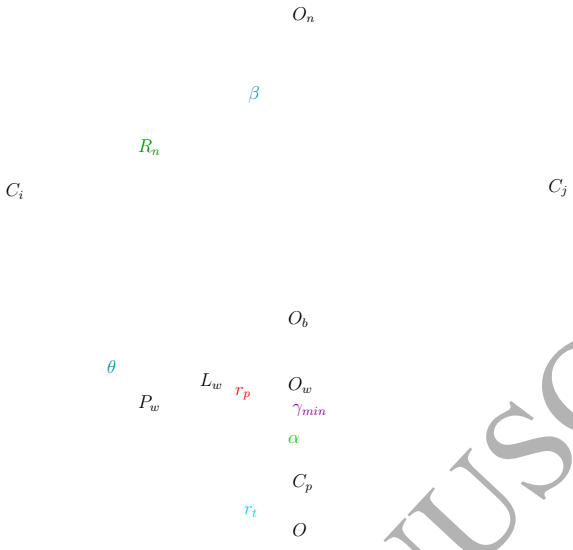

Figure 1: Geometrical description of a symmetric pore-throat system.

3.1. Symmetric pore-throat system

Fig. 1 shows a schematic of a symmetric pore-throat system. The radius of curvature can be expressed as

$$R_n = f\left(\alpha, \theta, r_t, r_p\right) \tag{7}$$

where α is the angle between the throats, θ is the contact angle, r_t is the throat radius (equal for both) and r_p is the pore radius. α is calculated from the position of the pore and throat centers using the cosine rule

$$\cos(\alpha) = \frac{\overrightarrow{C_pC_i} \cdot \overrightarrow{C_pC_j}}{\left|\left|\overrightarrow{C_pC_i}\right|\right| \left|\left|\overrightarrow{C_pC_j}\right|\right|} \tag{8}$$

where C_p, C_i, C_j are the center points of the pore and the two throats, respectively. In addition, the angles γ_{min}, γ_{max} and β are defined as

$$\gamma_{min} \quad = \quad \alpha - 2\arcsin(\frac{r_t}{r_p}) \tag{9}$$

$$\gamma_{max} = \alpha + 2\arcsin(\frac{r_t}{r_p}) \quad (10)$$

$$\beta = \frac{\pi}{2} - \theta - \frac{\alpha}{2} \quad (11)$$

An important assumption of the model is the position where the interface becomes unstable. The two limiting cases are: the *non-invasive* limit in which the interface becomes unstable once it enters into the throat region (point P_w in Fig. 1); and the completely *invasive* limit in which the interface becomes unstable when it touches the upper limit of the throat wall (point L_w in Fig. 1). The angle γ defines the position where the interface becomes unstable and is given by

$$\gamma = \epsilon\ \gamma_{min} + (1-\epsilon)\ \gamma_{max} \quad (12)$$

where ϵ is a model parameter ranging from 0.0 to 1.0.

As shown in Fig. 1, there are two points where the meniscus intersects the pore-throat border. It is readily shown that

$$OO_n = OO_b + O_bO_n = OC_p + C_pO_w + O_wO_n \quad (13)$$

$$OO_b = \frac{R_n\sin(\beta)}{\tan(\frac{\alpha}{2})}; O_bO_n = R_n\cos(\beta); OC_p = \frac{r_t}{\sin(\frac{\alpha}{2})}; C_pO_w = r_p\cos(\frac{\gamma}{2}) \quad (14)$$

$$O_wO_n^2 = R_n^2 - \left(r_p\sin(\frac{\gamma}{2})\right)^2 \quad (15)$$

and the radius of curvature R_n can be calculated by solving the following quadratic equation

$$\left[\left(\cos(\beta) + \frac{\sin(\beta)}{\tan(\frac{\alpha}{2})}\right)^2 - 1\right] R_n^2 + \left[-2\left(\cos(\beta) + \frac{\sin(\beta)}{\tan(\frac{\alpha}{2})}\right)\left(\frac{r_t}{\sin(\frac{\alpha}{2})} + r_p\cos(\frac{\gamma}{2})\right)\right] R_n \ ... \\ ... + \left[\left(\frac{r_t}{\sin(\frac{\alpha}{2})} + r_p\cos(\frac{\gamma}{2})\right)^2 + \left(r_p\sin(\frac{\gamma}{2})\right)^2\right] = 0 \quad (16)$$

From Eq. (16) it is possible to calculate the limiting radius of curvature and then obtain the entry capillary pressure by using

$$Pc_n = 2\frac{\sigma}{R_n} \quad (17)$$

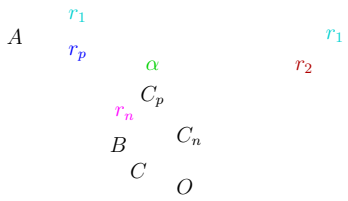

Figure 2: Geometrical description of a non-symmetric two throats system and its associated symmetric system. The blue line represents the interface position for the new PBF model.

3.2. Non-symmetric system: different throat sizes

If the throats have different radii, it is always possible to map the system onto an equivalent symmetric system. Fig. 2 shows the geometrical relations between a non-symmetric throat system and its equivalent symmetric system. The radius of curvature is the same in both systems. The smallest throat determines the interface position in the non-symmetric system and it is used as the throat radius in the equivalent symmetric system. The angle between the two throats α and the contact angle θ are the same in both systems. For the non-symmetric system shown in Fig. 2, we have

$$\alpha_1 + \alpha_2 = \alpha \tag{18}$$

$$\frac{\sin(\alpha_1)}{\sin(\alpha_2)} = \frac{r_1}{r_2} \tag{19}$$

$$\tan(\alpha_1) = \frac{\sin(\alpha)}{\left(\frac{r_2}{r_1} + \cos(\alpha)\right)} \tag{20}$$

where α_1 and α_2 are the angles defined between intersection of the throats axes and the segment OC_p. For both systems the distance AO is the same

and

$$AB^2 = r_p^2 - r_1^2 \quad (21)$$

$$AC = AB + \frac{r_1}{\tan(\alpha_1)} - \frac{r_1}{\tan(\alpha/2)} \quad (22)$$

Finally, the pore radius of the equivalent symmetric system is given by

$$r_p^* = \sqrt{AC^2 + r_1^2} \quad (23)$$

In summary, for a non-symmetric throat system it is always possible to derive an equivalent symmetric system having the same radius of curvature. The equivalent throat radius is given by the minimum of the two throat radii, the angle between the throats is the same and the equivalent pore size is given by Eq. (23). Once these new parameters are calculated, the radius of curvature can be determined from Eq. (16).

3.3. Non-symmetric system: different contact angles

An equivalent symmetric system can also be obtained for cases where the contact angles are different in the two throats. A geometrical representation of this case and its equivalent symmetric system is shown in Fig. 3. Similarly to the analysis presented above, the throat that defines the position of the interface is the one with the smallest contact angle. This is the contact angle used in the equivalent symmetric system. From Fig. 3, we have

$$AB = 2R \cos\left(\frac{\theta_{max} - \theta_{min}}{2}\right) \quad (24)$$

$$AC = AB \cos\left(\frac{\theta_{max} + \theta_{min}}{2}\right) \quad (25)$$

where the distance AC is the difference between the pore center in both systems. The equivalent pore radius is given by

$$LC_p = \sqrt{r_p^2 - r_t^2} \quad (26)$$

$$r_p^* = \sqrt{(LC_p + AC)^2 + r_t^2} \quad (27)$$

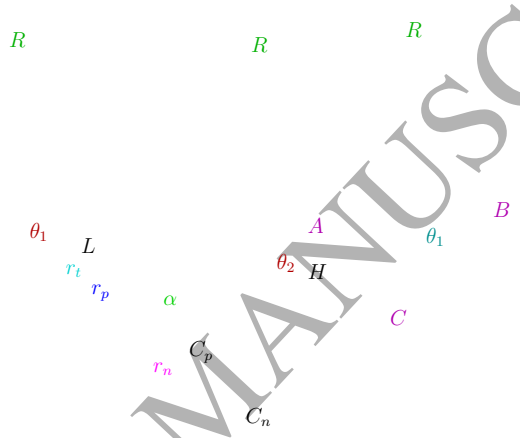

Figure 3: Geometrical description of a non-symmetric two throats system with different contact angles and its equivalent symmetric system.

It is important to note that the new equivalent pore size r_p^* depends on the interface radius R_n and cannot be determined analytically. It must be computed iteratively by solving Eq. (27) and Eq. (16). During this iterative process, it is necessary to check that the interface is still located inside the throats because for some numerical conditions it can be located at the throat/pore border.

The key difference between the new pore-body filling model described in this section and the stochastic models discussed above, is that the new model accounts for the spatial locations of the *nwp* filled throats actually involved in the displacement. This means that the radius of curvature depends on the local fluid topology which changes during the simulation. Entry pressures for PBF can therefore not be calculated prior to the simulations.

4. Materials and methods

We compare simulated capillary trapping curves with experimental data for four different water-wet rocks. Table 1 lists the fluids and rock properties of the experimental data sets. Pore space representations of the rocks are obtained from micro-CT imaging (sandpack and Bentheimer) and process-based reconstructions (Fontainebleau and Berea). A total of 12 pore space images are analyzed. Table 2 summarizes the properties of the images. Absolute permeabilities are calculated using a D3Q19 lattice Boltzmann solver Øren et al. (2007) with multiple relaxation times. Formation factors (FRF) are computed by solving the Laplace equation assuming insulating pore walls Øren & Bakke (2002).

We generated pore-network representations of the pore space images using e-Core[2]. Details about the algorithms used to extract topological and geometrical characteristics of the networks are given elsewhere Bakke & Øren (1997); Øren et al. (1998); Øren & Bakke (2003). Table 3 lists important geometrical and topological properties of the networks. The average aspect ratio $\overline{AR}$ is defined as

[2]Digital Rock Laboratory by Thermo Fisher Scientific (formerly FEI)

Table 1: Properties of samples and fluids used in experimental imbibition studies.

Reference	Samples	ϕ[%]	k[mD]	nwp/wp	ρ^1_{wp}	ρ^1_{nwp}	σ^2
Pentland et al.Pentland et al. (2010a)	Sandpack	37	32000	octane/brine	1042	709	50.81
SuzanneSuzanne et al. (2003b)	Fontainebleau	3-28	0.1-3000	air/water	770	2	24
Kumar et al.Kumar et al. (2009)	Fontainebleau	13.5	1800	butane/brine	-	-	40
Pentland et al.Pentland et al. (2011)	Berea	22	466	nDecane/brine	1025	700	-
Niu et al.Niu et al. (2015)	Berea	21	212	CO2/brine	1023	386	36-44
Akbarabadi et al.Akbarabadi & Piri (2013)	Berea	20	50	CO2/brine	1123	393	38.15
OakOak (1990)	Berea	-	1000	dodecane/brine	1001	802	53
Alizadeh et al.Alizadeh & Piri (2014)	Bentheimer	21.7	2660	soltrol/brine	1138	802	40.7
Raessi et al.Raeesi et al. (2013)	Bentheimer	23	1980	decane/brine	1000	691	58

[1] Density $[kg/m^3]$
[2] Interfacial Tension $[mN/m]$

Table 2: Pore space images and digital properties of rock samples used in the pore-scale simulations. Δ is the voxel length, size is the dimensions of the image (voxels) and PNM denotes the pore-network model.

Sample	$\Delta[\mu m]$	size	Porosity[%]	k[mD]	FRF	PNM k[mD]	PNM FRF
Sandpack	10	450^3	36.3	39055	5.05	37560	4.25
Bentheimer	2.03	800^3	21.4	3260	12.86	3116	12.7
Berea	1.5	1200^3	21.7	543.9	14.37	551.5	10.6
Fontainebleau_1	2.76	1000^3	24.9	5786	9.02	5545	7.25
Fontainebleau_2	2.76	1000^3	21.9	3837	11.69	3556	9.48
Fontainebleau_3	2.76	1000^3	19.9	2696	14.65	2465	11.7
Fontainebleau_4	2.76	1000^3	17.9	1954	18.63	1846	14.5
Fontainebleau_5	2.76	1000^3	14.9	1073	27.79	940.6	22.2
Fontainebleau_6	2.76	1000^3	12.9	632.4	40.48	557.6	31.7
Fontainebleau_7	2.76	1000^3	9.8	228.8	82.36	206.6	64.5
Fontainebleau_8	2.76	1000^3	7.8	88.91	175.7	69.6	139
Fontainebleau_9	2.76	1000^3	4.3	8.78	1105.4	1.38	1340

$$\overline{AR} = \frac{1}{N}\sum_{i=1}^{N}\frac{r_{p,i}}{\bar{r}_{t,i}} \tag{28}$$

where N is the total number of pores, $r_{p,i}$ is the size of the pore i and $\bar{r}_{t,i}$ is the average size of the throats connected to pore i. Computed permeabilities and formation factors of the pore-networks are compared with the image-based results in Table 2. The properties are in good agreement with both the grid calculations performed directly on the pore space images and the corresponding experimental results.

Pore-network models require contact angles as input to the simulations. Measurements of *in-situ* contact angles using micro-CT imaging techniques is

Table 3: Geometrical and topological properties of the pore-networks. $\bar{r}_p$ is the average pore size, $\bar{r}_t$ is the average throat size, $\overline{AR}$ is the average aspect ratio and $\bar{z}$ is the average coordination number.

Sample	Porosity[%]	Pores	Throats	$\bar{r}_p[\mu m]$	$\bar{r}_t[\mu m]$	$\overline{AR}$	$\bar{z}$
Sandpack	36.3	18824	52867	39.1	24.0	2.00	5.55
Bentheimer	21.4	5052	9380	14.4	9.66	2.12	3.80
Berea	21.7	86155	219923	7.35	3.98	2.71	5.06
Fontainebleau_1	24.9	23719	61108	22.6	13.0	2.44	5.14
Fontainebleau_2	21.9	25979	63155	21.1	12.1	2.52	4.84
Fontainebleau_3	19.9	27125	63649	20.0	11.5	2.54	4.61
Fontainebleau_4	17.9	27373	61945	19.0	11.0	2.58	4.46
Fontainebleau_5	14.9	27502	58581	17.8	10.3	2.58	4.16
Fontainebleau_6	12.9	26112	53389	17.2	9.91	2.61	3.99
Fontainebleau_7	9.9	23701	44734	16.0	9.26	2.58	3.66
Fontainebleau_8	7.8	20838	37025	15.4	8.79	2.61	3.41
Fontainebleau_9	4.3	15335	24096	11.6	7.09	2.73	3.02

a unique and promising method for measuring effective contact angles. The application of this method to a wide variety of rocks is of course limited by the ratio of the pore to voxel size. Unless this ratio is large, voxelation errors can lead to significant measurement uncertainties. *In-situ* contact angle measurements have recently been reported for Bentheimer and Berea sandstones Aghaei & Piri (2015); Khishvand et al. (2016a,b). The results of these measurements are summarized in Table 4.

Table 4: *In-situ* contact angle measurements for binary-equilibrated two-phase experiments in Berea and Bentheimer sandstone.

Reference	Sample	*nwp/wp*	θ_r [degrees]	θ_a [degrees]
Aghaei and PiriAghaei & Piri (2015)	Bentheimer	nDecane/brine	10-30	20-42
Aghaei and PiriAghaei & Piri (2015)	Berea	soltrol/brine	6-26	7-55
Khishvand et al. Khishvand et al. (2016a)	Bentheimer	nDecane/brine	17-32	20-50
Khishvand et al. Khishvand et al. (2016b)	Berea	decalin/brine	37-56	44-71
Khishvand et al. Khishvand et al. (2016b)	Berea	N_2/brine	28-44	35-58
Khishvand et al. Khishvand et al. (2016b)	Berea	N_2/decalin	28-48	37-56

The contact angle distributions for the two measurement series in Bentheimer sandstone are similar with a mean advancing contact angle $\theta_a \simeq 33^o$. For Berea sandstone, the mean value for the two oil-water systems is $\theta_a \simeq 31^o$ (soltrol-brine) and $\theta_a \simeq 57^o$ (decalin-brine). The contact angle distribution for the gas-oil and gas-water systems are similar with a mean $\theta_a \simeq 46^o$.

5. Results and Discussion

A pore-network simulator was developed following the model described in Øren et al. (1998). All the stochastic PBF models as well as the new model were included in the pore-network simulator. A detailed description of the simulator and the calculations of relative permeability and capillary pressure are given elsewhere Øren et al. (1998). We use $\epsilon = 0.5$, see Eq. (12), for all the simulations presented in this work. Appendix A shows that the exact value of ϵ has little effect on the amount of trapping.

We computed capillary trapping curves using both the new PBF model and the four stochastic models presented in Section 2. The observed differences between the models are analyzed. We compare the simulated results with the corresponding experimental data sets listed in Table 1. The input fluid properties are the same as those reported in the experiments. We assume strongly water-wet conditions for all primary drainage simulations, randomly assigning a receding contact angle θ_r in the range 0^o-10^o. Based on the measurements listed in Table 4, we use a random uniform distribution for θ_a between 30^o-35^o as the base case input when simulating imbibition. We perform a sensitivity analysis of the impact of the advancing contact angle on capillary trapping using contact angles in the range 15^o-20^o and 45^o-50^o.

5.1. Capillary trapping in sandpack LV60A

Pentland et al. Pentland et al. (2010a) measured residual oil saturation S_{or} as a function of initial oil saturation S_{oi} in a sandpack at ambient conditions. The sandpack was initially fully saturated with brine and then different volumes of oil (octane) were injected. Equilibrium initial conditions were established by letting the oil rise under buoyancy forces. The sandpack was then flooded with brine at low Ca to establish S_{or}. The sample was sliced into 10 sections and trapped saturations were measured using gas chromatography.

We extracted a pore-network from micro-CT images of the actual sandpack used in the experiments (LV60A). Properties of the images and the pore-network are given in Table 2. We established S_{oi} by simulating a primary drainage process. Oil is injected at the inlet face of the network and water escapes through the outlet on the opposite side. The simulation stops when the oil saturation reaches the target value, S_{oi}. Next, we simulate an

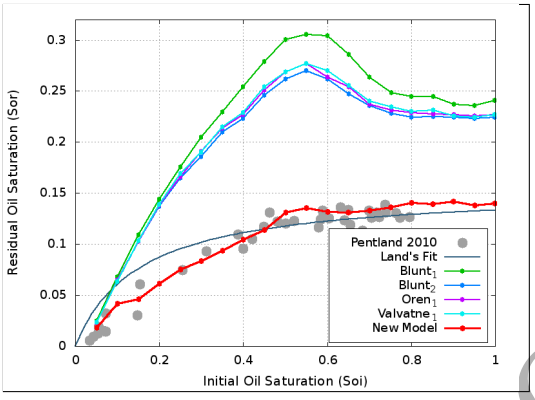

Figure 4: Capillary trapping in sandpack LV60. Comparison between experimental Pentland et al. (2010a), stochastic models (Blunt_1, Blunt_2, Oren_1 and Valvatne_1) and the new cooperative pore-body filling model results. The best fit for Land's trapping model is plotted with a brown line.

imbibition process by injecting water. To mimic the experimental boundary conditions, oil is allowed to leave the network through both the inlet and outlet faces. The simulation stops when oil is no longer connected to the outlet faces.

Fig. 4 compares simulated trapping curves with the experimental measurements. Each data point of this *IR* curve corresponds to one simulation sequence. The stochastic models clearly over-estimate the amount of trapping (by more than 100% in several cases). This is similar to the results reported by Raeini et al. Raeini et al. (2015). In contrast, the results for the new PBF model match the experimental data with less than 10% deviation across the entire saturation range. The simulated trapping curve increases almost linearly with initial saturation until a maximum $S_{or} \simeq 0.14$ is reached at $S_{oi} \simeq 0.55$. The trapped saturation remains constant as S_{oi} increases further. As observed in Fig. 4, the best-fit to Land's trapping model does not predict this behavior Pentland et al. (2010a). The simulated results display percolation threshold effects at small initial saturations ($S_{oi} < 0.2$) as the distribution of S_{oi} is not uniform.

Generally, the new PBF model predicts lower capillary entry pressures than the stochastic models. This is supported by Fig. 5 which shows imbibi-

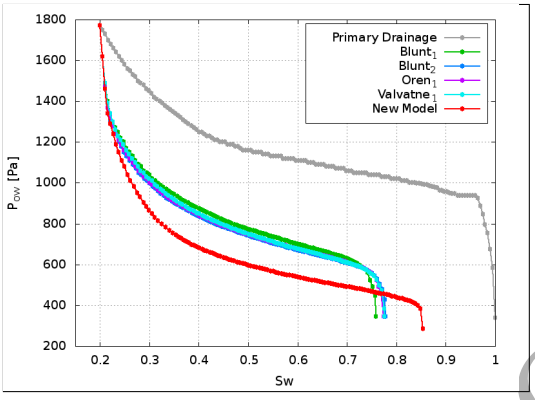

Figure 5: Capillary trapping during imbibition in a sandpack sample. Capillary pressure curves for the different pore-body filling models in the case of $S_{oi} = 0.8$.

tion capillary pressure curves for $S_{oi} \simeq 0.8$. The capillary pressure curve for the new PBF model is lower than those for the stochastic models, suggesting that the dominant pore-scale displacement mechanism is different. This is confirmed by analyzing the displacement statistics. At $S_{oi} \simeq 0.8$, the ratio of snap-off to PBF events is 9.4 for the new model. For the stochastic models this value is around 0.4. Snap-off is the dominant bond-breaking mechanism for the new model, while PBF dominates for the stochastic models. However, the residual saturation is considerably smaller for the new model. This is not in agreement with the commonly held view that snap-off leads to significant trapping while cooperative pore-body filling leads to very little trapping.

The key to understand these seemingly counter-intuitive results lies in how subtleties of the pore structure control the competition between snap-off and piston-like advance. The sandpack is well connected ($\bar{z} = 5.6$) and has a low aspect ratio ($\overline{AR} \simeq 2.0$). For most of the I_n configurations established, the maximum angle α between *nwp* filled throats is large and the PBF entry pressure is small. The wetting phase advance is arrested at pore bodies. It proceeds by snap-off in the smallest connecting throats until an I_1 configuration (PBF with only one *nwp* filled throat) is established. The remaining *nwp* filled throat is the largest of the connecting throats. It is this pore-throat aspect ratio that determines if trapping in the pore body will occur. For rocks with low aspect ratios, there is a subtle balance between

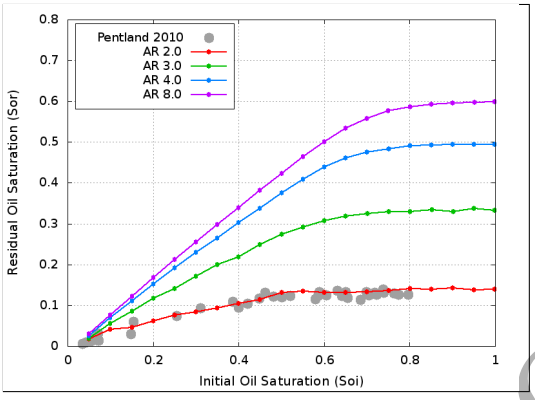

Figure 6: Sensitivity analysis of pore-throat aspect ratio on capillary trapping for a sandpack sample using the new PBF model.

I_1 invasion and snap-off in the connecting throats Øren et al. (1998); Valvatne & Blunt (2004). If the aspect ratio is small, the I_1 entry pressure is greater than for snap-off. In this case, the wetting phase invades the pore and adjoining throat by piston-like displacements and there is no trapping. If the aspect ratio is large, snap-off is the preferred displacement, resulting in trapping of the *nwp* in the pore-body.

This is confirmed in Fig. 6 which illustrates the effects of the average aspect ratio on the sandpack trapping curve. We changed the aspect ratio by uniformly reducing the throats sizes while keeping the pore sizes and the network topology unchanged. The maximum trapped saturation (at $S_{oi} \simeq 1$), increases from $S_{or} \simeq 0.14$ to $S_{or} \simeq 0.34$ as the $\overline{AR}$ increases from 2.0 to 3.0. For $\overline{AR} = 4.0$, the maximum trapped saturation increases to 0.5, clearly demonstrating that the competition between snap-off and piston-like I_1 advance strongly depends on the pore-throat aspect ratio.

Fig. 7 shows computed trapping curves for three sets of advancing contact angles: 15^o-20^o, 30^o-35^o and 45^o-50^o. The maximum trapped saturation depends on the contact angle and increases from $S_{or} \simeq 0.12$ to $S_{or} \simeq 0.17$ as the contact angle decreases from 45^o-50^o to 15^o-20^o. This is due to changes in the competition between snap-off and PBF displacements. Capillary entry pressures for snap-off decrease faster with increasing contact angles than the

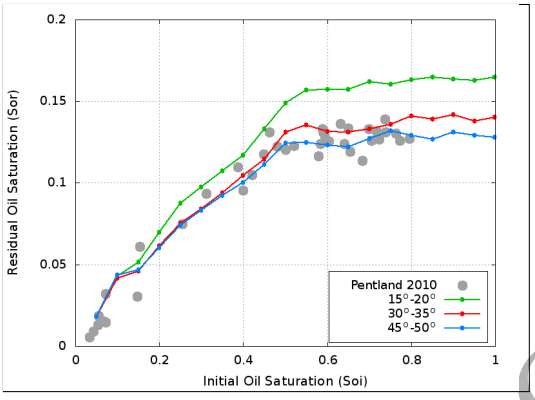

Figure 7: Sensitivity analysis of advancing contact angles on capillary trapping for the sandpack sample, compared with experimental data from Pentland et al. (2010a).

PBF entry pressures. Snap-off is impeded and I_1 and cooperative pore-body filling displacements (frontal advance) increase, reducing trapping.

5.2. Capillary trapping in Fontainebleau sandstone

Bourbie and Zinzner Bourbie & Zinzner (1985) measured trapped gas saturation S_{gr} as a function of porosity in Fontainebleau sandstone samples. In the experiments, clean dried samples were placed on a bed of glass beads filled with toluene. Toluene spontaneously imbibed in the core plug until it reached an equilibrium state. Toluene saturation was inferred from weight measurements before and after imbibition. The same technique was employed by Suzanne et al. Suzanne et al. (2003b) but the experimental set-up was placed in a closed system filled with liquid vapor saturated air.

We reconstructed nine process-based models of Fontainebleau sandstone. The porosity of the models ranged from 0.043 to 0.249. Details about the reconstruction algorithm are given elsewhere Bakke & Øren (1997); Øren & Bakke (2002). Input grain sizes were measured from micro-CT images of actual Fontainebleau samples Suzanne et al. (2003b); Suzanne (2003). Properties of the reconstructions and the extracted pore-networks are summarized in Tables 2 and 3. We use the same fluid properties as those reported by Suzanne et al. Suzanne et al. (2003b). S_{gi} was established by simulating a primary drainage process (injecting gas) in a network initially fully saturated

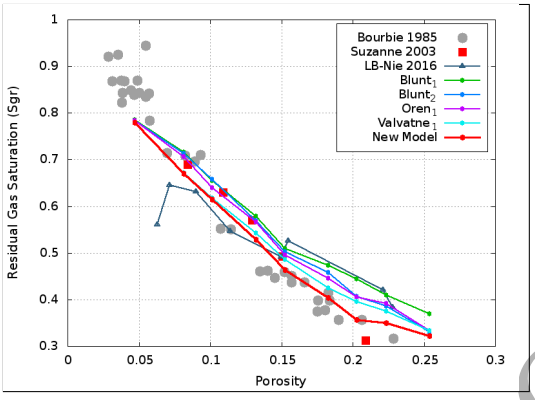

Figure 8: Capillary trapping as a function of porosity for Fontainebleau sandstone samples. Comparison between experimental results (Bourbie & Zinzner, 1985; Suzanne et al., 2003b), pore-network simulations (stochastic models and the new cooperative pore-body filling mechanism) and lattice-Boltzmann simulations Nie et al. (2016).

with brine until all the pores are invaded by gas. Then, the imbibition sequence was simulated.

Fig. 8 compares simulated and experimental S_{gr} values as a function of porosity for several Fontainebleau sandstones. The stochastic models overestimate trapping while the new PBF model describes more accurately the experimental data, especially at high porosities. The displacement statistics show that snap-off is the dominant bond-breaking mechanism for the new model. Snap-off and PBF have similar frequencies for the stochastic models. At low porosities ($\phi < 0.12$), there is little difference between the models. Nie et al. Nie et al. (2016) simulated imbibition directly on micro-CT images of Fontainebleau sandstone using a two-phase lattice Boltzmann method. As shown in Fig. 8, the discrepancies in S_{gr} for these direct simulations are larger than those for the network model simulations across the entire porosity range.

Fig. 9 shows the effects of contact angles on the simulated S_{gr} versus porosity curve. The variation in trapped gas saturation with contact angle is more pronounced at high porosities. Low contact angles favor snap-off Øren et al. (1998) and we see more trapping. At low porosities, changing the contact angle in the range considered here has little effect on trapping.

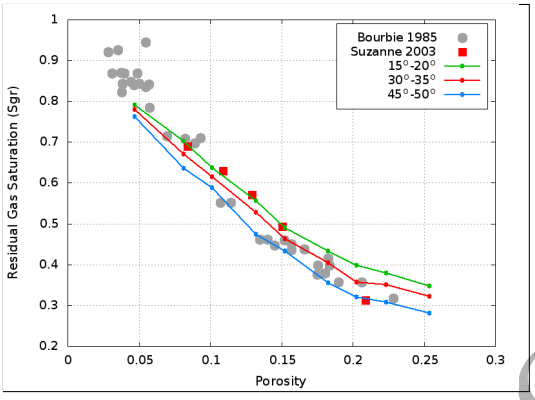

Figure 9: Sensitivity analysis of advancing contact angles on capillary trapping for different Fontainebleau sandstone samples, compared with experimental data from Bourbie & Zinzner (1985); Suzanne et al. (2003b).

The pore-throat aspect ratio for the Fontainebleau networks changes only slightly with porosity ($2.44 < \overline{AR} < 2.73$). This suggests that other geometrical properties of the pore structure control the significant effects of porosity on trapping. Obviously, the connectivity or average coordination number changes with porosity. For the nine networks analyzed here, $\bar{z}$ decreases strongly with porosity and varies in the range $3.02 < \bar{z} < 5.14$ (see Table 3). As shown in Fig 10, the average coordination number and trapped gas saturation are clearly correlated. The correlation coefficient between S_{gr} and $\bar{z}$ is 0.98.

Suzanne et al. Suzanne et al. (2003b,a); Suzanne (2003) measured relationships between trapped gas saturation and initial gas saturation using several samples of Fontainebleau sandstone. The results of two of those samples are used in this section. The porosities of the samples were 0.15 and 0.13, with corresponding permeabilities of 1660 and 880 mD, respectively. We compare the experimental data with simulated results using the Fontainebleau_6 network which has a porosity of 0.129.

Fig. 11 displays the simulated and measured trapping curves. The stochastic models over-predict S_{gr} across the entire saturation range. The results for the new PBF model are more consistent with the experimental data. The ratio of snap-off to I_n events is highest for the new PBF model

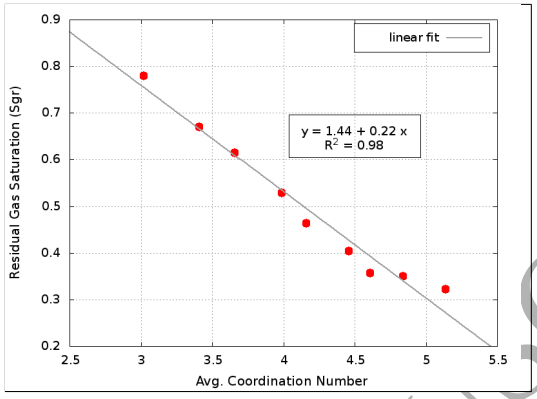

Figure 10: Simulated residual saturation versus average coordination number for Fontainebleau sandstone.

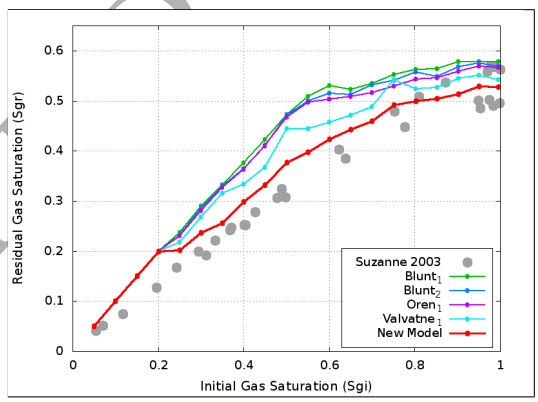

Figure 11: Comparison between experimental Suzanne et al. (2003b) and simulated trapping curves for Fontainebleau sandstone.

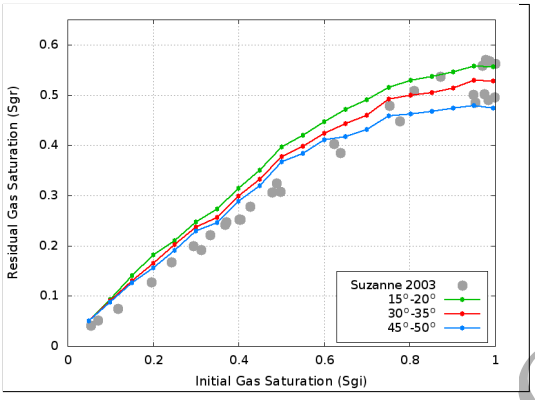

Figure 12: Sensitivity analysis of advancing contact angles on capillary trapping for Fontainebleau sandstone, compared with experimental data from Suzanne et al. (2003b).

and, similar to the sandpack results, the amount of trapping is smaller than for the stochastic models. Fig. 12 displays the effects of contact angles on the trapping curve. Contact angles have a clear effect on S_{gr} at high initial saturations with increased trapping at smaller contact angles.

5.3. Capillary trapping in Berea sandstone

In this section, we compare experimental trapping data for Berea sandstone Pentland et al. (2011); Akbarabadi & Piri (2013); Niu et al. (2015) with simulated results using the different PBF models. Pentland et al. Pentland et al. (2011) investigated capillary trapping in an n-decane/brine system. Akbarabadi and Piri Akbarabadi & Piri (2013) and Niu et al. Niu et al. (2015) reported capillary trapping in CO_2/brine systems. The properties of the rocks and the fluids used in these experiments are presented in Table 1. A process-based model with analogous properties to the Berea sandstone sample described in Pentland et al. Pentland et al. (2011) was generated. Tables 2 and 3 list properties of the extracted pore-network.

Fig. 13 compares the simulated and measured trapping curves. As before, the stochastic models over-predict trapping while the new PBF model predicts the measured data more accurately. The stochastic models perform better for Berea sandstone than for the sandpack presented earlier. This is in agreement with the finding of Raeini et al. Raeini et al. (2015) and Pentland et al. Pentland et al. (2010b). Compared to the sandpack, the Berea network

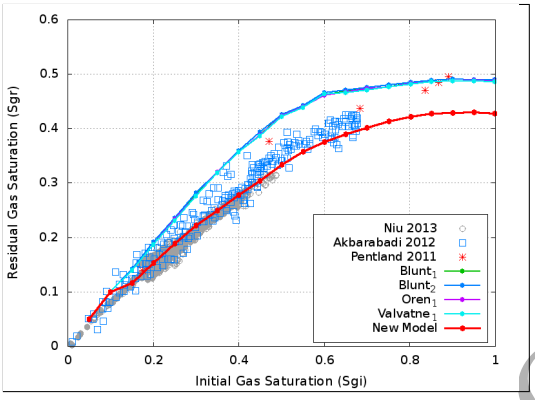

Figure 13: Comparison between experimental data Pentland et al. (2011); Akbarabadi & Piri (2013); Niu et al. (2015) and simulated trapping curves for Berea sandstone.

has a wider range of pore and throat sizes and displays a larger average aspect ratio (2.7 vs. 2.0). Snap-off is the dominant trapping mechanism both for the new PBF model and for the stochastic ones. This reduces the differences between the models. The effect of contact angles on the Berea trapping curve is shown in Fig. 14. Trapping increases with decreasing contact angles. The maximum trapped saturation ranges from $S_{gr} \simeq 0.38$ to $S_{gr} \simeq 0.46$ for the contact angles considered here.

5.4. Relative permeability in Berea and Bentheimer sandstones

In this section, the effects of the new PBF model on the relative permeability curves are analyzed. Oak Oak (1990) presented experimental relative permeability curves for three different water-wet Berea sandstone samples. In this work, only the results of the most permeable sample are used (referred to as sample 13 in Oak (1990)). We use the pore-network model described previously in the literature Lerdhal et al. (2000); Valvatne & Blunt (2004); Raeesi et al. (2013). This network is a good representation of the Berea sandstone sample used in the experiments. The porosity and permeability of the pore-network are similar to the experimentally reported values. Primary drainage simulations are performed with receding angles in the range 0^o-10^o. For the imbibition simulation, we assign advancing contact angles in the range 25^o-35^o, corresponding to the values presented in Section 4.

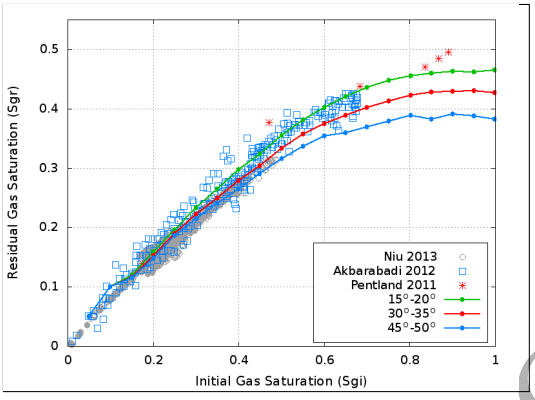

Figure 14: Sensitivity analysis of advancing contact angles on capillary trapping for a Berea sandstone sample, compared with experimental data from Pentland et al. (2011); Akbarabadi & Piri (2013); Niu et al. (2015).

Fig. 15 compares simulated and measured imbibition relative permeability curves. A significant difference in the trapped oil saturation is observed between the stochastic models and the new PBF model. The stochastic models over-estimate the residual saturation by at least 15 %. The new model describes more accurately the residual saturation and the experimental relative permeability curves. Several works have used the same pore-network and reproduced the experimental data by adjusting the advancing contact angle to unrealistically high values: 30^o-57^o in Lerdhal et al. (2000), 62^o-81^o in Valvatne & Blunt (2004) and 63^o-80^o in Piri & Blunt (2005). In this work, the advancing angles are chosen according to the *in-situ* contact angle measurements for a water-wet Berea sandstone reported in Aghaei & Piri (2015).

Alizadeh and Piri Alizadeh & Piri (2014) reported steady state relative permeability curves for two- and three-phase systems in a water-wet Bentheimer sandstone sample. An end-cut of the core plug was scanned in a micro-CT scanner at 2.03 μm voxel size. A pore-network representation of the Bentheimer sample was extracted from the micro-CT volume. Properties of the images and pore-network are given in Tables 2 and 3. In the primary drainage simulations, receding contact angles are distributed between 10^o-32^o, while for imbibition the advancing contact angles are in the range 20^o-42^o. These contact angles were measured by Aghaei et al. Aghaei & Piri (2015) in the same sample of Bentheimer sandstone as used for the

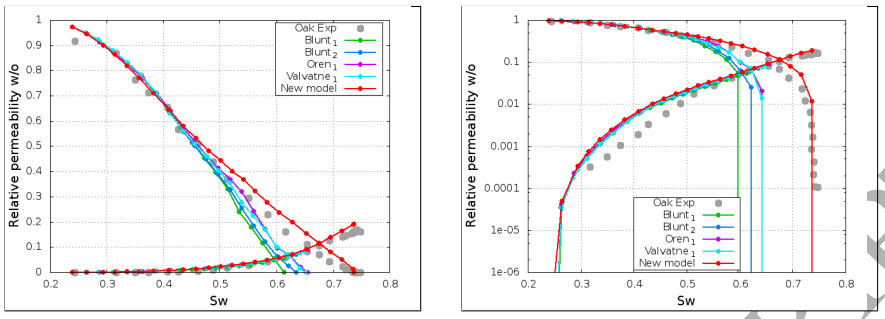

Figure 15: Comparison of Berea imbibition relative permeability curves for the different PBF models and the experimental results (Oak (1990)).

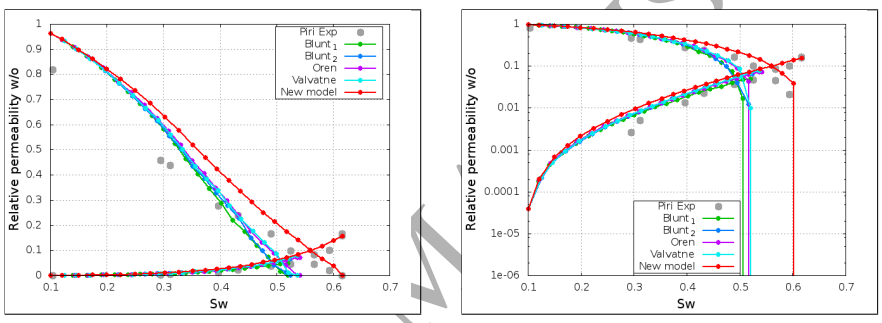

Figure 16: Comparison of Bentheimer imbibition relative permeability curves for the different PBF models and experimental results Alizadeh & Piri (2014).

relative permeability measurements.

Fig. 16 shows the simulated and measured imbibition relative permeability curves. All the stochastic models over-estimate the trapped oil saturation with about 25 %. In addition, the shape of the oil relative permeability curves do not describe the trend observed in the experimental data. The new PBF model predicts more accurately the residual oil saturation and gives a better description of the oil relative permeability shape at high Sw. A general over-prediction of the oil relative permeability is observed at low water saturations for all the models. The new model describes the water relative permeability with less than 5% deviation.

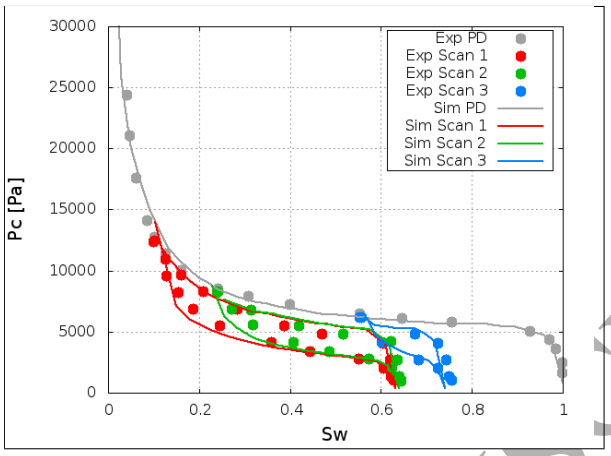

Figure 17: Comparison of experimental and simulated capillary pressures scanning curves for Bentheimer sandstone

5.5. Capillary pressure scanning curves in Bentheimer sandstone

Raeesi et al. Raeesi (2012); Raeesi et al. (2013) presented capillary pressure hysteresis curves for two-phase air-water systems in a strongly water-wet Bentheimer sandstone. The experiments included primary drainage, imbibition and secondary drainage scanning curves for different initial saturations. As there are no available pore-space images of the sample used in the experiments, the pore-network described in Idowu et al. (2013), for a Bentheimer sandstone, is used in this section. The properties of this sample are similar to the experimental values reported in Raeesi et al. (2013). The pore-network porosity is 22% while the permeability is 2200 mD. We assign contact angles in the range 0^o-10^o, 25^o-30^o and 15^o-20^o for the primary drainage, imbibition and secondary drainage, respectively.

Simulated capillary pressure scanning curves for three different initial saturations are compared with experimental data in Fig. 17. We note that the simulated primary drainage curve closely follows the experimental one, confirming that throat sizes are captured accurately in the pore-network. The simulated scanning curves reproduce the trapped *nwp* saturations as well as the shape and level of hysteresis seen in the experimental data. Capillary pressure hysteresis is governed by contact angle hysteresis ($\theta_a > \theta_r$), different displacement mechanisms between drainage and imbibition, and trapping of

the non-wetting phase. All the stochastic PBF models over-estimated the trapped saturations by at least 20%. Similar findings were reported by Raeesi et al. Raeesi et al. (2013).

5.6. Non-wetting phase ganglia size distribution

The pore-scale distribution of trapped non-wetting phase has important implications to enhanced oil recovery, CO_2 storage and gas entrapment in the capillary fringe. Direct 3D micro-CT imaging allows *in-situ* observation of the distribution of the trapped non-wetting phase Favetto et al. (2010); Iglauer et al. (2011); Andrew et al. (2013); Geistlinger & Mohammadian (2015). In these experiments, trapped *nwp* clusters, or ganglia, of all sizes are observed, from single pore ganglia to multi-pore ganglia that almost span the system. Percolation theory is typically invoked to explain the observed cluster size distribution Geistlinger & Mohammadian (2015). As described in Stauffer & Aharony (1994), the cumulative cluster size distribution (CDF) is given by

$$CDF(s) = \sum_{1}^{s} PDF(s) = 1 - \left(\frac{k}{s}\right)^{(\tau-1)} \tag{29}$$

where $PDF(s)$ is the probability that a cluster contains s pores, τ is the Fisher exponent and k is a constant. In this work, following percolation theory Stauffer & Aharony (1994), s corresponds to the number of sites (pores) in each cluster and not the volume of the cluster as described in Favetto et al. (2010); Iglauer et al. (2011).

The simulated ganglia size distributions after imbibition for the Berea, Bentheimer, Fontainebleau sandstones and the sandpack are shown in Fig. 18. The three sandstones have similar cluster size distributions. We see a truncated power-law distribution with scaling over approximately three orders of magnitude in ganglion size. A least-square fit to the data yields Fisher exponents in the range $1.89 < \tau < 1.96$ for advancing contact angles between 15^o and 20^o, as reported in Table 5. These values are smaller than the theoretical value for bond percolation in three-dimensions ($\tau = 2.189 \pm 0.002$ Lorenz & Ziff (1998)). As discussed earlier, imbibition in these sandstones proceeds by a combination of snap-off and frontal advance. Piston-like I_1 displacements and cooperative pore-body filling leads locally to well-swept regions of the pore space with little trapping. Physically, this introduces a

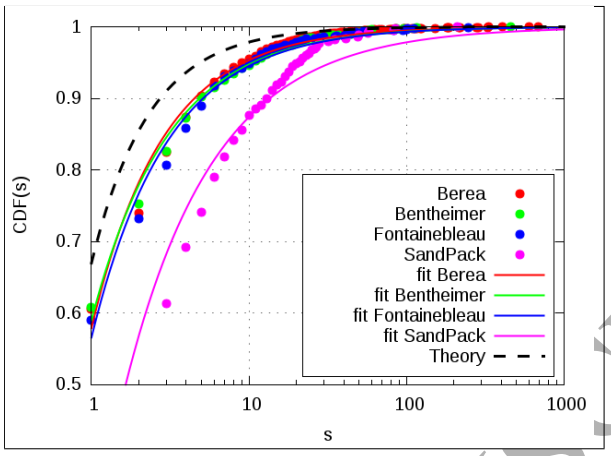

Figure 18: Cumulative cluster size distribution after imbibition and power law fitting functions for four different samples: Berea, Bentheimer, Fontainebleau_6 sandstones and sandpack.

lower correlation length or cut-off length for the onset of percolation-type behavior Blunt & Scher (1995).

As shown in Fig. 18, the behavior of the sandpack is different from the other samples. The cluster size distribution is not well described by a power law. There are considerably fewer smaller blobs than would be predicted by percolation theory and most of the residual non-wetting phase saturation is dominated by the largest clusters. Imbibition in the sandpack advances by a subtle balance between snap-off and I_1 piston-like displacements which leads to a flat frontal advance with very little trapping. Snap-off (bond percolation) is not the main trapping mechanism and the process cannot be described by percolation theory. This is reflected by a lower Fisher exponent, $\tau = 1.76$.

Table 5: Sensitivity analysis of advancing contact angles on the simulated residual saturations S_{nwr} and the Fisher exponents τ.

	$15^o - 20^o$		$30^o - 35^o$		$45^o - 50^o$	
Sample	S_{nwr}	τ	S_{nwr}	τ	S_{nwr}	τ
Berea	0.46	1.96	0.42	1.92	0.38	1.90
Bentheimer	0.45	1.89	0.38	1.86	0.33	1.85
Fontainebleau_6	0.55	1.90	0.52	1.87	0.47	1.79
Sandpack	0.17	1.76	0.14	1.73	0.13	1.72

The results presented in the previous sections demonstrated that the relative importance of snap-off and cooperative pore-body filling depends on the contact angle. This implies that the distribution of the trapped non-wetting phase, and therefore the exponent τ, are sensitive to the contact angle. This is confirmed by the results listed in Table 5. For all the samples, the value of the residual *nwp* saturation S_{nwr} and the Fisher exponent τ decrease as the contact angles increase. The frequency of small clusters gradually decreases with increasing contact angles. Higher contact angles impede snap-off and local disconnection of the non-wetting phase is suppressed by frontal advance and cooperative pore-body filling.

6. Conclusion

We present a new model to describe cooperative pore-body filling in geologically realistic pore-networks. The model accounts for geometrical characteristics of the pore-body, the spatial locations of the connecting throats and the local fluid topology. The main geometrical assumption is that the center-line of the throats connected to a pore meet in the center of the pore.

We validate the model by comparing simulated capillary trapping curves with published data for four water-wet samples (sandpack, Berea, Fontainebleau and Bentheimer). The simulations are performed on pore-networks extracted from micro-CT images or process-based reconstructions of the actual rock samples used in the experiments. Published *in-situ* measured contact angle distributions are used as input to the pore-scale simulations.

We predict capillary trapping curves that are in good agreement with the experimental data for all of the four samples. The new PBF model predicts more accurately residual non-wetting phase saturations compared with commonly used stochastic models. In particular, we successfully compute the trapping curve for a sandpack which could not be matched previously using stochastic pore-body filling models, regardless of the contact angle assumed Raeini et al. (2015). We attribute this to a more accurate description of the cooperative pore-body filling displacement mechanism. We show that trapping in the sandpack is controlled by a subtle balance between snap-off events and frontal I_1 piston-like advance. These subtleties are not captured when using the stochastic pore-body filling models. The new model successfully predicts capillary pressure scanning curves and imbibition relative

permeability for Bentheimer sandstone using *in-situ* measured contact angles as input to the simulations.

The non-wetting phase is trapped in clusters of all sizes, from single pore blobs to large multi-pore blobs. The amount and distribution of trapped non-wetting phase is determined by the relative importance of snap-off (bond percolation) and frontal advance. The simulated cluster size distributions have a lower Fisher exponent than predicted by percolation theory. Cooperative pore-body filling and piston-like I_1 displacements introduce a lower cut-off length for percolation-like behavior. The simulated frequency of small blobs is less than the theoretical value predicted from percolation theory.

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Appendix A. The effects of ϵ on predicted trapping

We performed a sensitivity analysis of the amount of trapping predicted by the new PBF model to the exact value of the parameter ϵ in Eq. (12). Three different cases were analyzed: *non-invasive* $\epsilon = 0.0$, *full-invasive* $\epsilon = 1.0$, and $\epsilon = 0.5$. We note that in the *non-invasive* limit, $\gamma = \gamma_{max}$ and Eq. (16) simplifies to

$$R_n = \frac{\tan(\frac{\alpha}{2})}{\sin(\beta)} \left(\frac{r_t}{\sin(\frac{\alpha}{2})} + r_p \cos(\frac{\gamma}{2}) \right) \tag{A.1}$$

where the R_n is the radius of curvature of the interface.

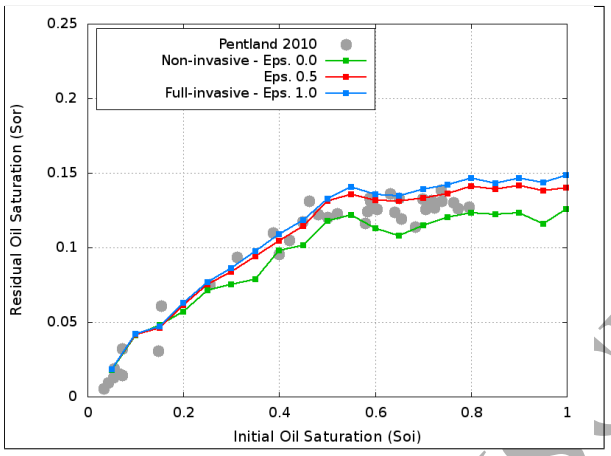

Figure A.19: Sensitivity analysis of the parameter ϵ, in Eq. (12), on capillary trapping for a sandpack. Experimental capillary trapping data from Pentland et al. (2010a).

The differences in predicted residual saturations between the three cases are smaller than 5 % for most of the samples. However, larger differences can be observed in samples with a fine balance between snap-off and PBF. This is illustrated in Fig. A.19 which shows the sensitivity of the sandpack trapping curve to the value of ϵ. There is little difference in trapping between the cases $\epsilon = 1.0$ and $\epsilon = 0.5$. Generally, the amount of trapping varied less than 2 % between these cases. However, in the limiting case of $\epsilon = 0.0$, the simplified Eq. (A.1) can predict up to 15 % less trapping at high initial saturations, as shown in Fig. A.19.

For all the simulations in this work we used $\epsilon = 0.5$. Geometrically, this corresponds to the case where the invading interface becomes unstable at the mid-point of the throat (i.e. between point P_w and L_w in Fig. 1).

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